

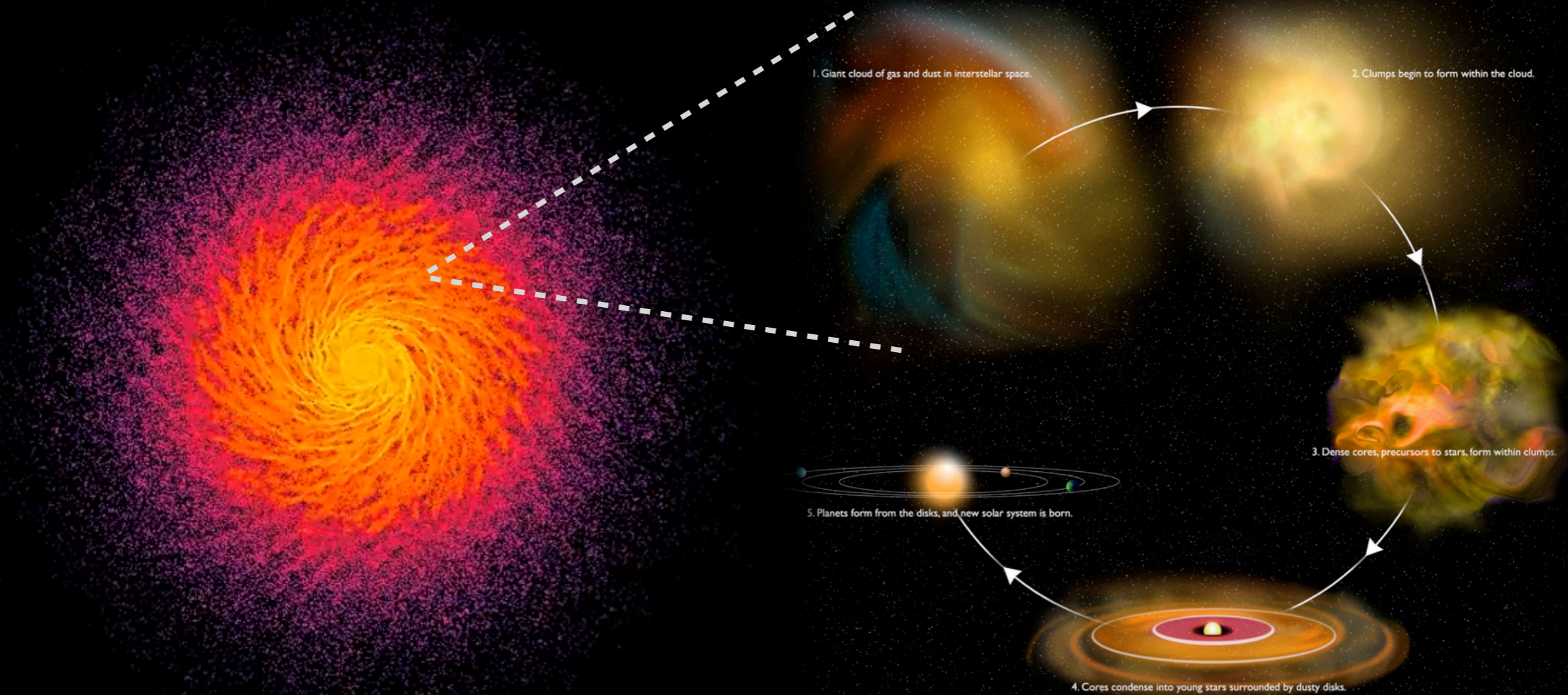
Star Formation in Galaxies and the “Bathtub” Model

ASTR:6782

Hai Fu

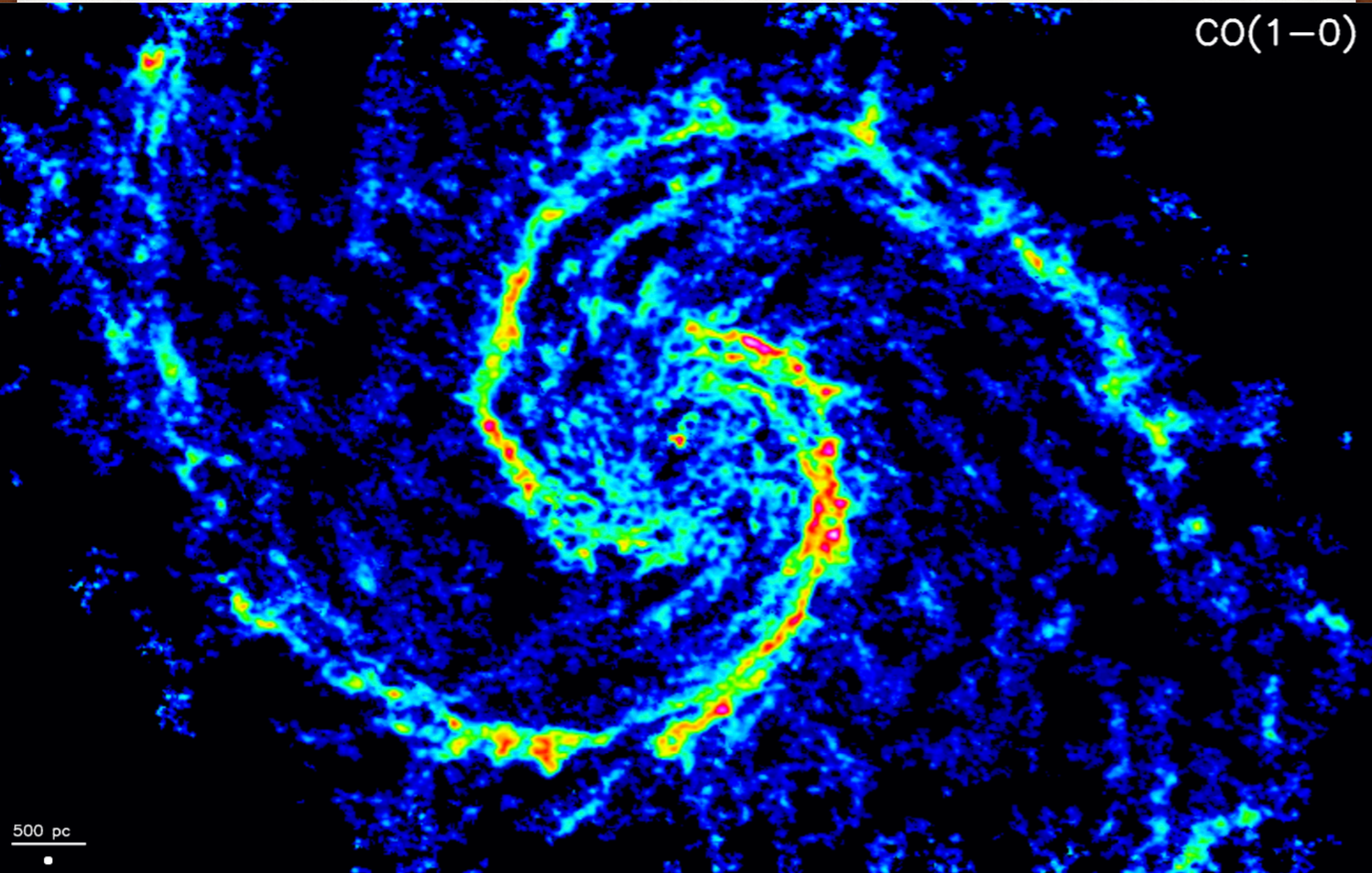
Star-Forming Regions in M51, a
nearby grand-design spiral galaxy

Formation of Molecular Clouds and Stars in a Disk Galaxy



M51 - WHIRLPOOL GALAXY

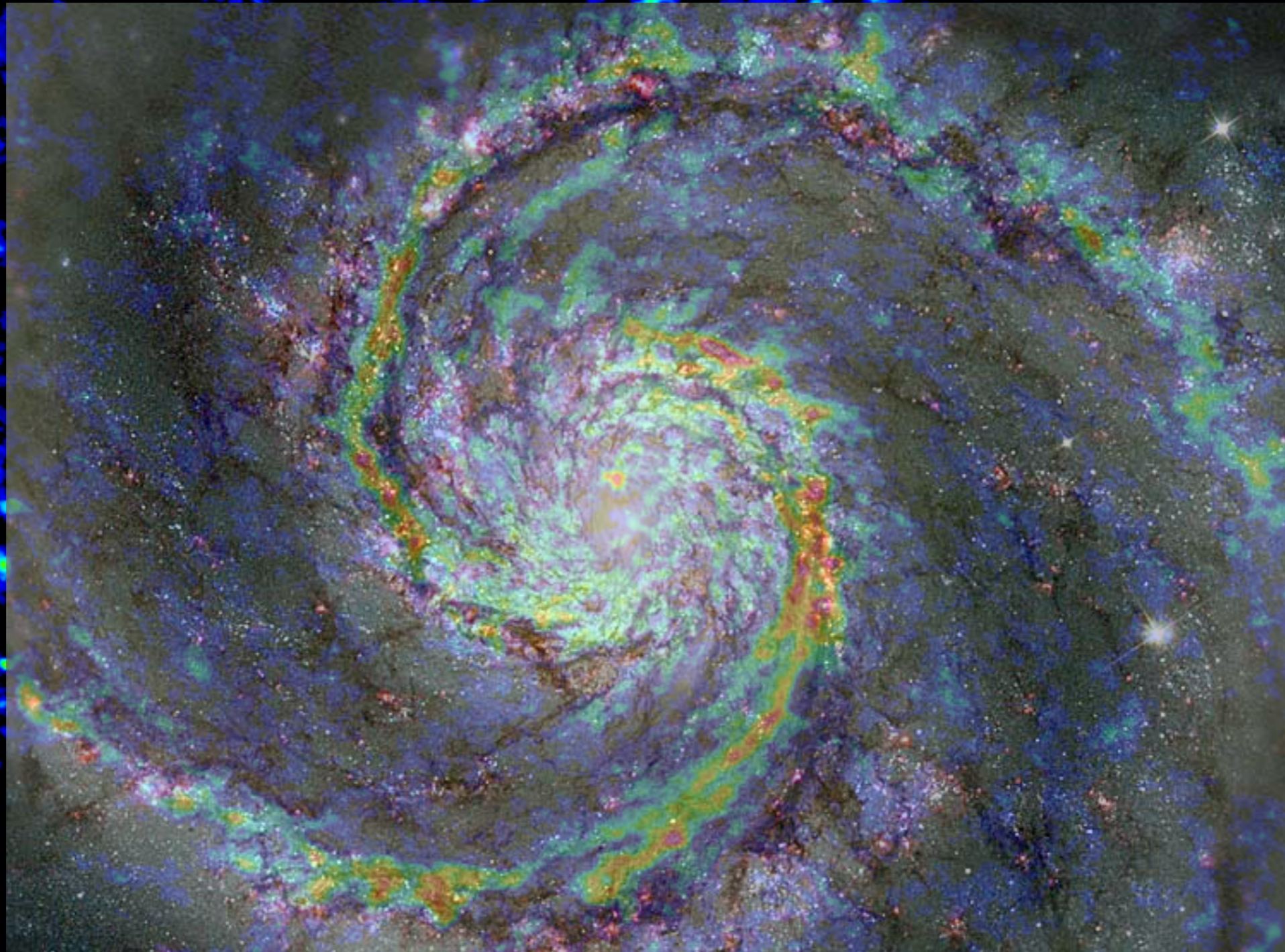
CO(1-0)



500 pc

M51 - WHIRLPOOL GALAXY

CO(1-0)



500 pc



The Orion Star Forming Region

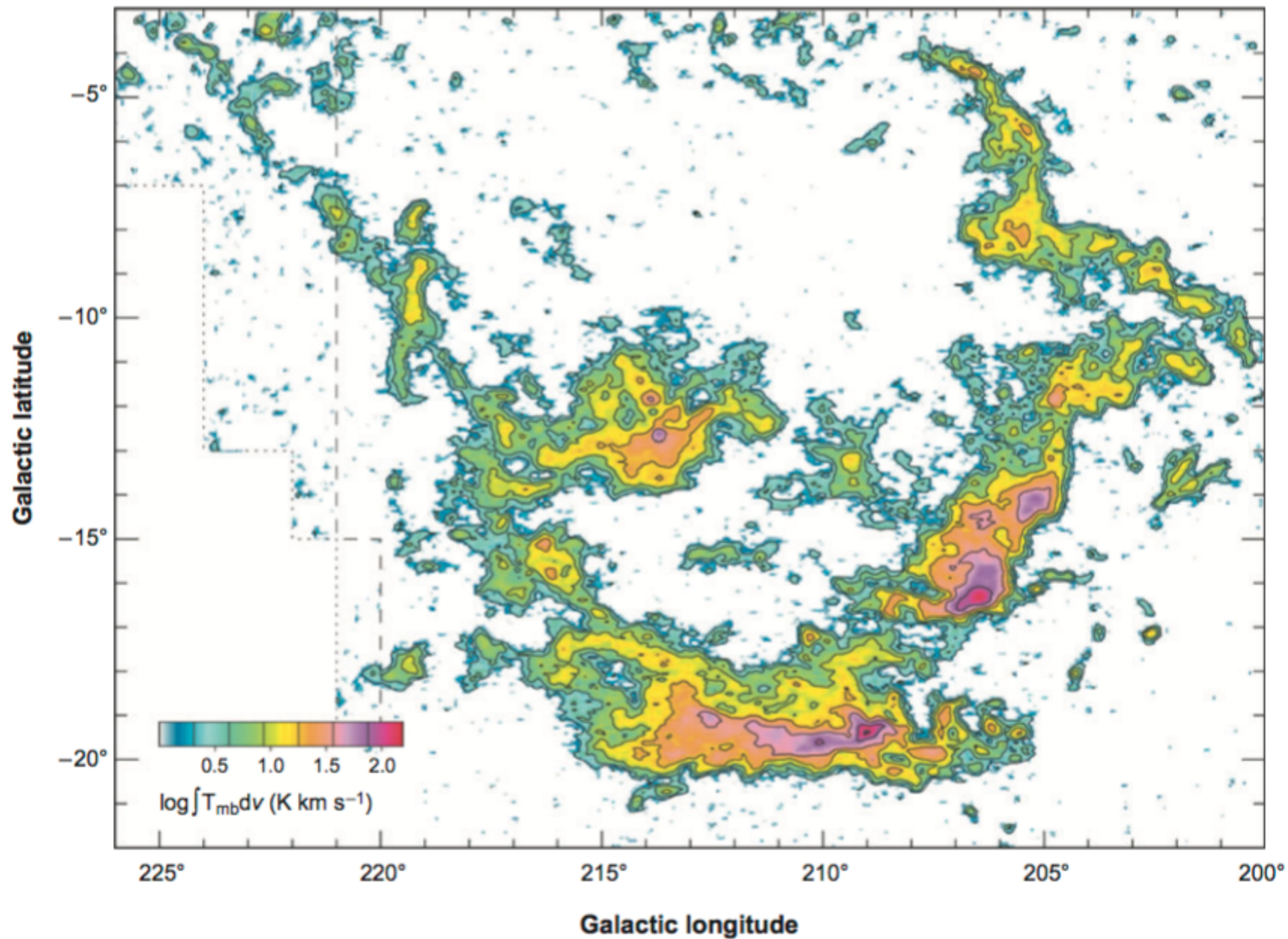
The Orion Star-Forming Region
(Optical Image)



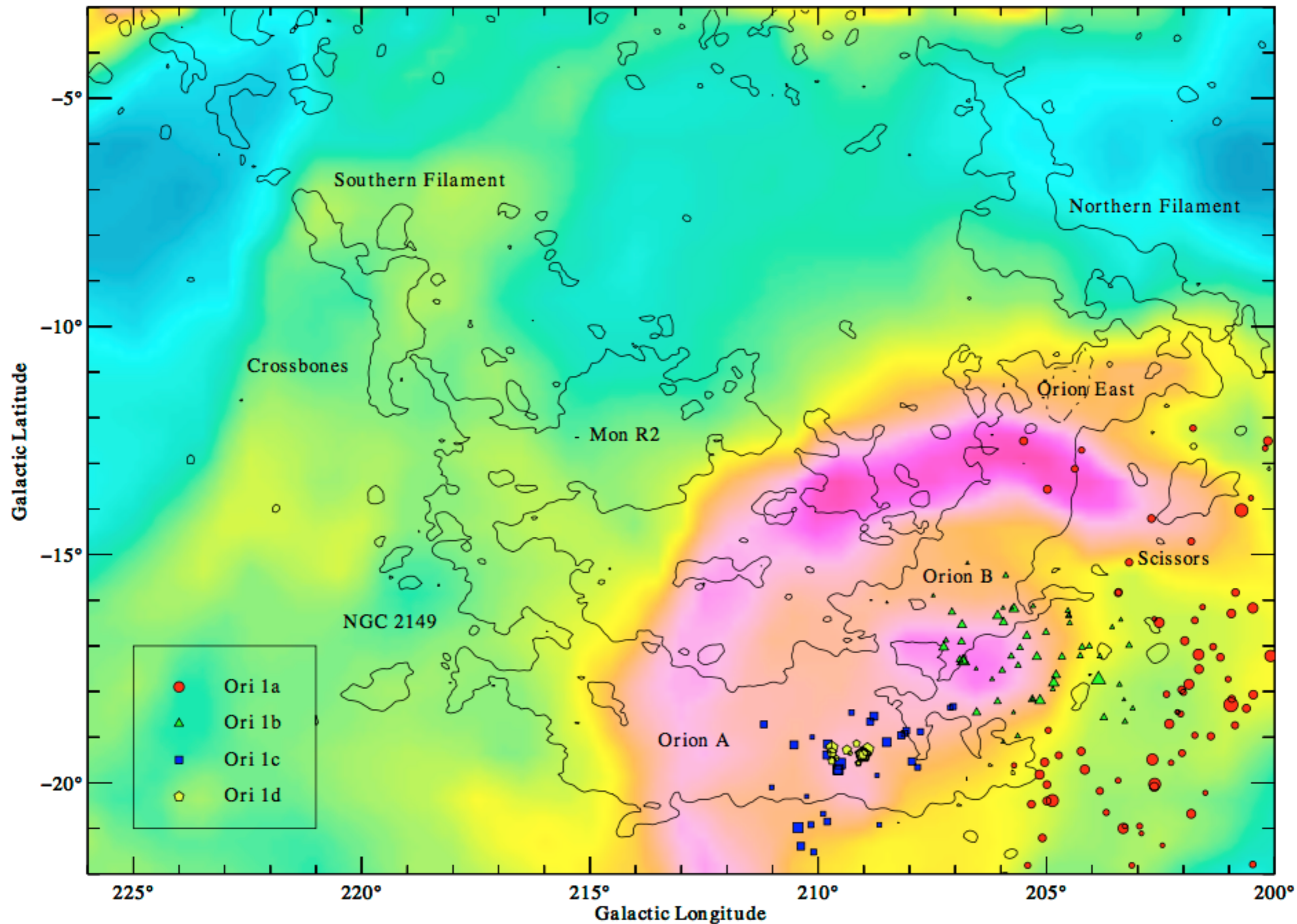
The Orion Star-Forming Region
(Continuum + H-alpha)



Molecular Gas seen in CO J=1-0 transition

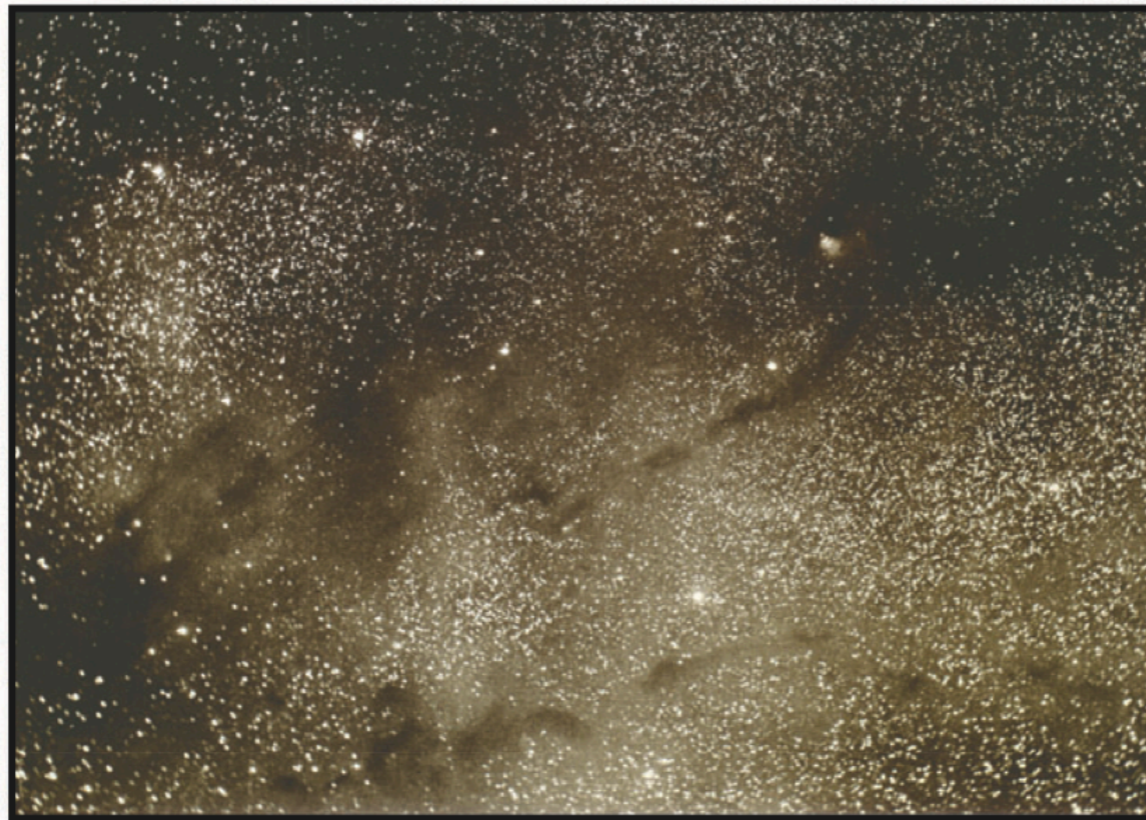


Molecular Gas (contours) vs. Ionized Gas (hue map)



Cold Molecular Cores (Boner-Elbert Spheres)

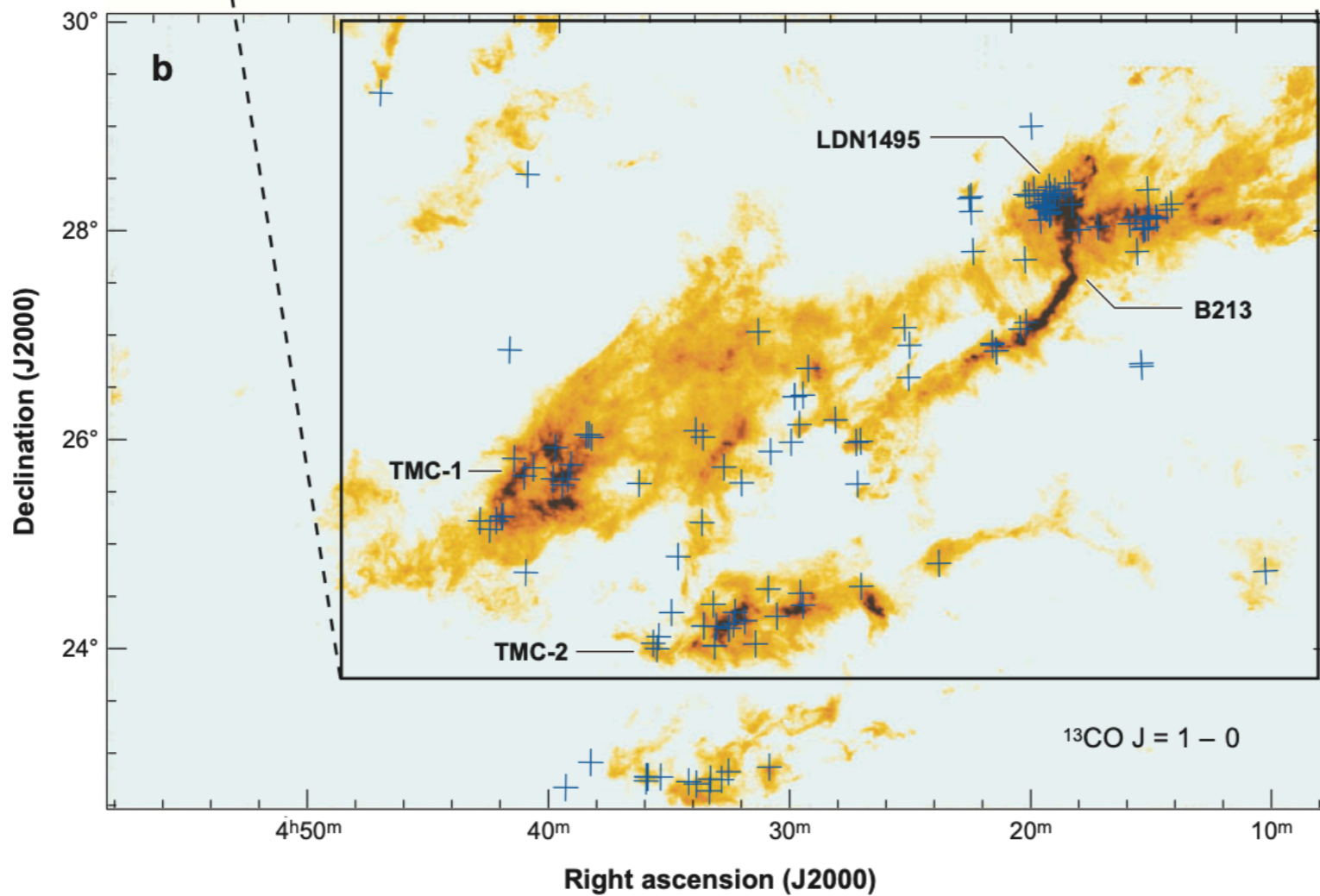
a



Bergin & Tafalla 2007

**Optical photographic
image of the Taurus
molecular cloud,
taken in 1907**

E.E. Barnard: Nebulous Region in Taurus (January 1907)



**CO(1-0) emission
crosses indicate
known stellar and
protostellar objects**

Table 1 Properties of dark clouds, clumps, and cores

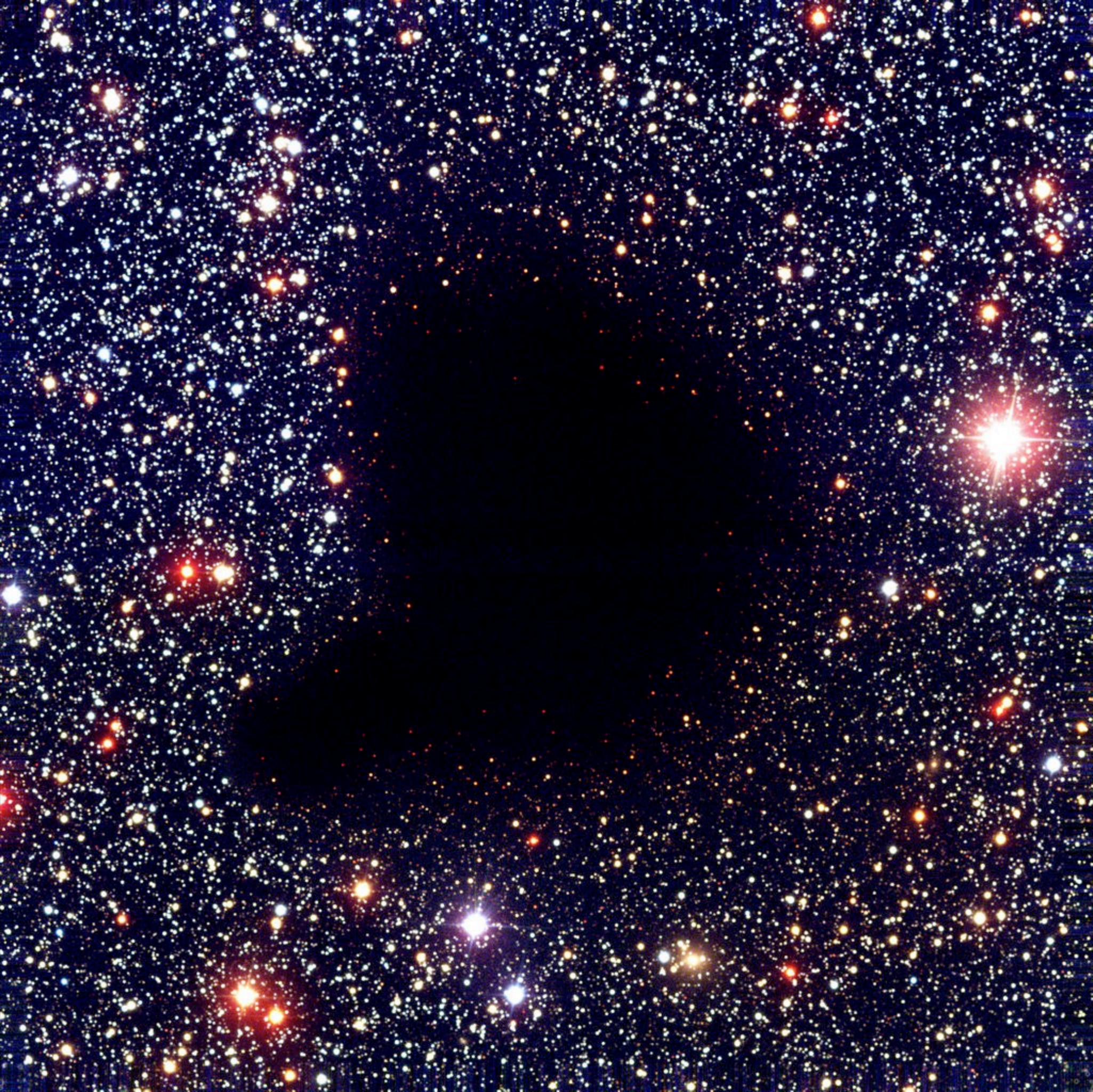
	Clouds ^a	Clumps ^b	Cores ^c
Mass (M_{\odot})	$10^3 - 10^4$	50–500	0.5–5
Size (pc)	2–15	0.3–3	0.03–0.2
Mean density (cm^{-3})	50–500	$10^3 - 10^4$	$10^4 - 10^5$
Velocity extent (km s^{-1})	2–5	0.3–3	0.1–0.3
Crossing time (Myr)	2–4	≈ 1	0.5–1
Gas temperature (K)	≈ 10	10–20	8–12
Examples	Taurus, Oph, Musca	B213, L1709	L1544, L1498, B68

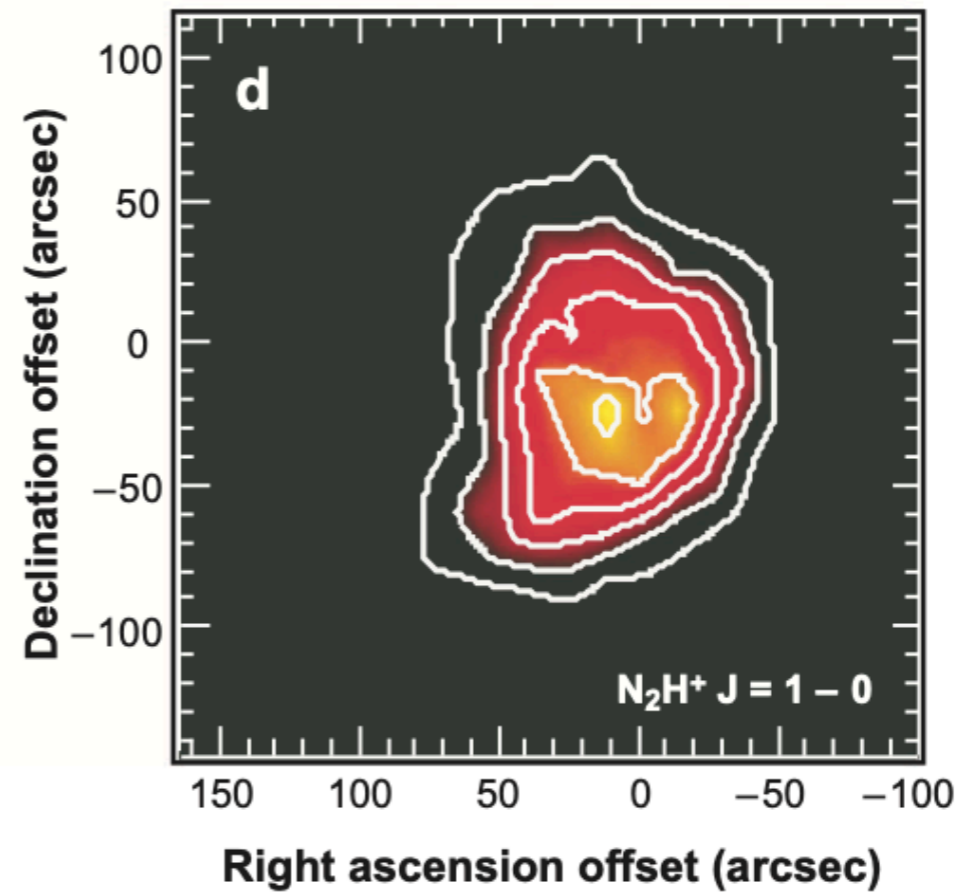
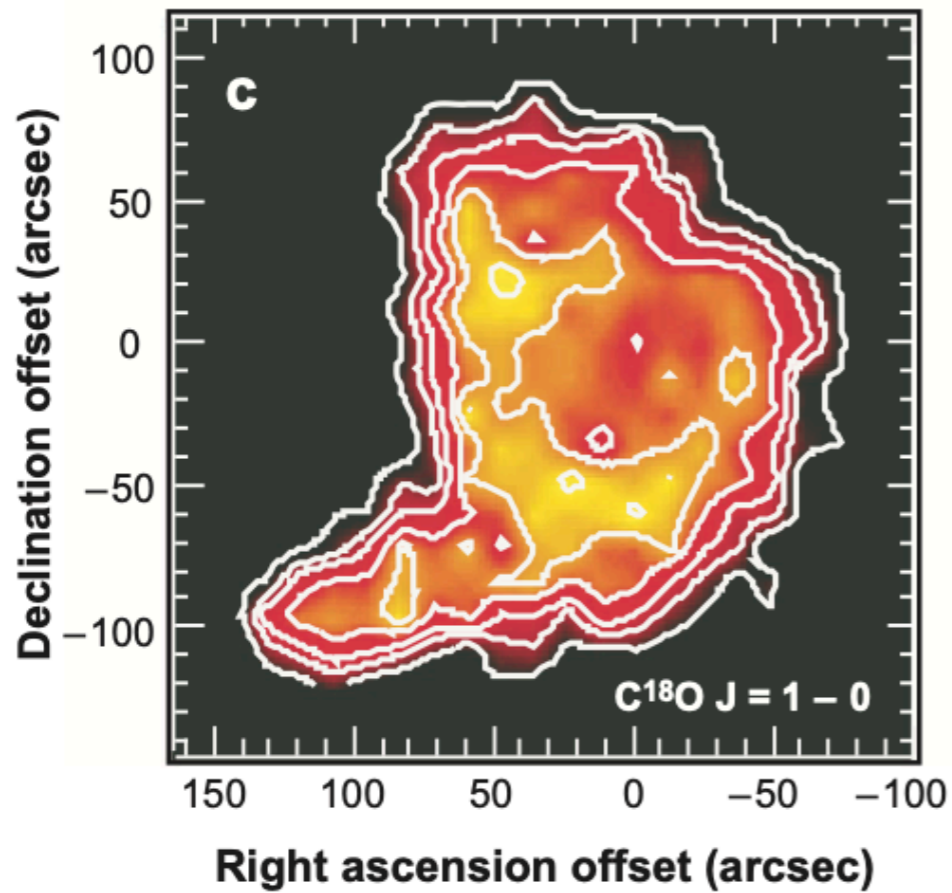
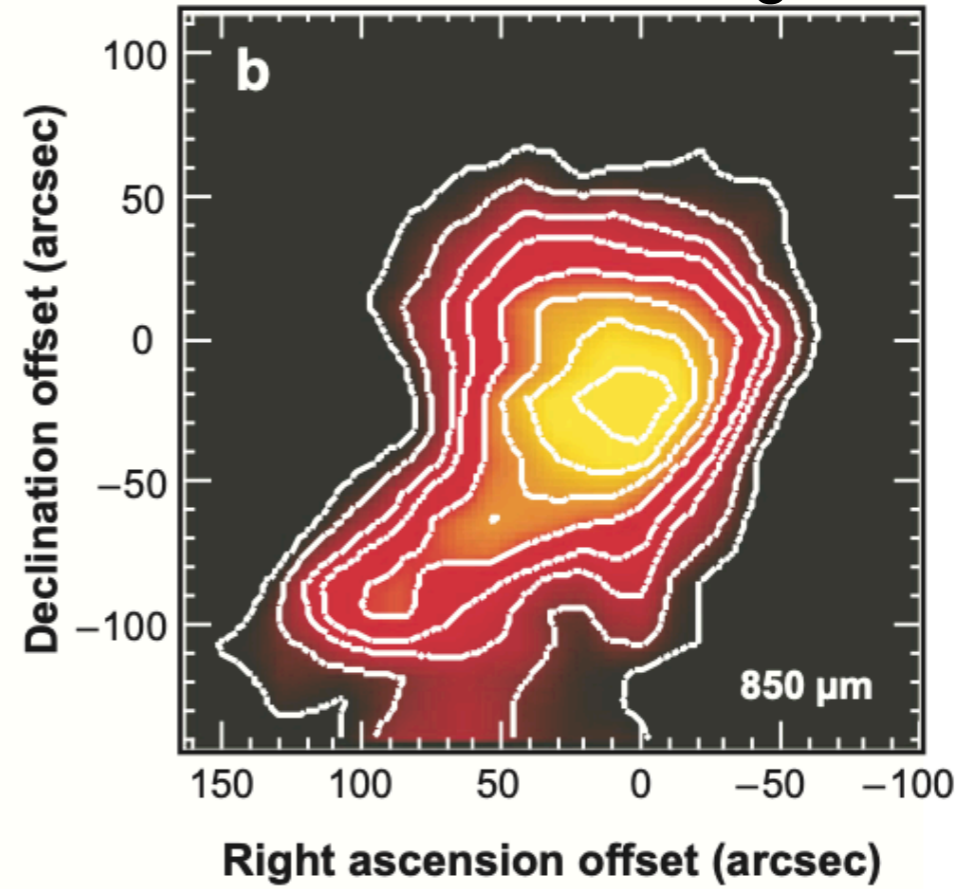
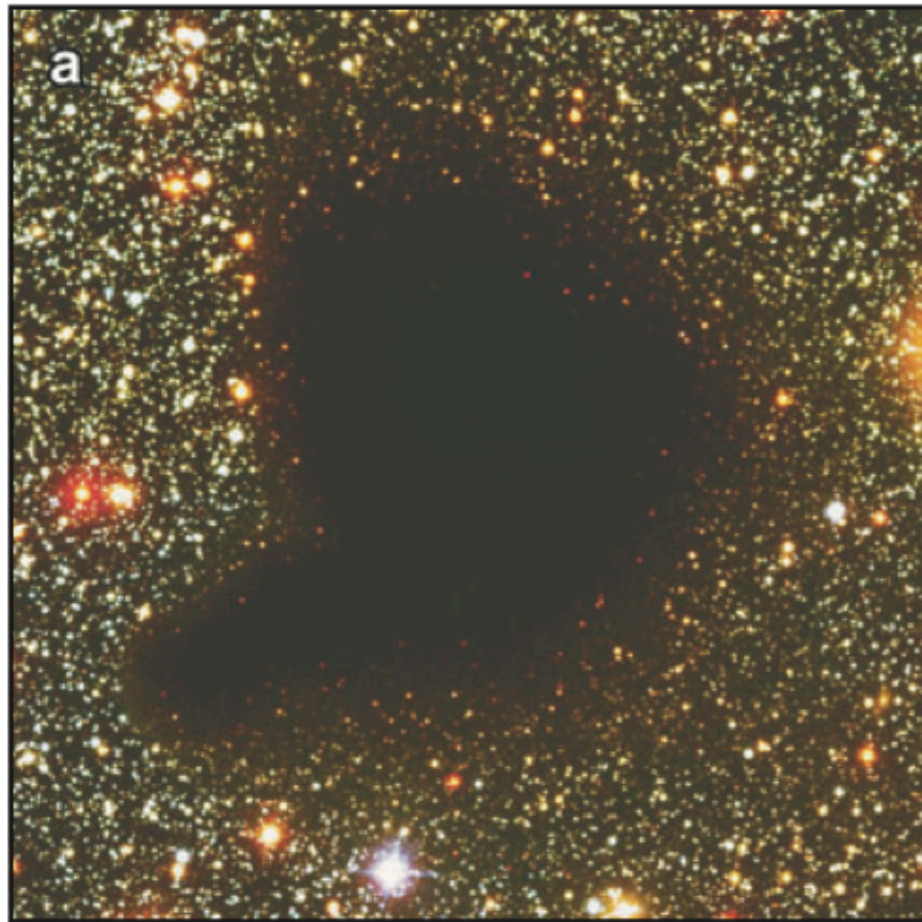
^aCloud masses and sizes from the extinction maps by Cambr esy (1999), velocities and temperatures from individual cloud CO studies.

^bClump properties from Loren (1989) (^{13}CO data) and Williams, de Geus & Blitz (1994) (CO data).

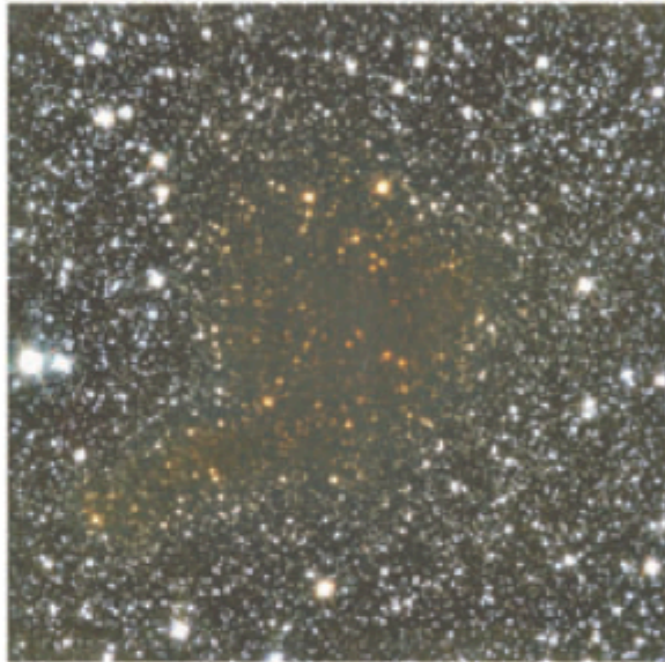
^cCore properties from Jijina, Myers & Adams (1999), Caselli et al. (2002a), Motte, Andr e & Neri (1998), and individual studies using NH_3 and N_2H^+ .

Barnard 68
dark core





a Barnard 68 K band

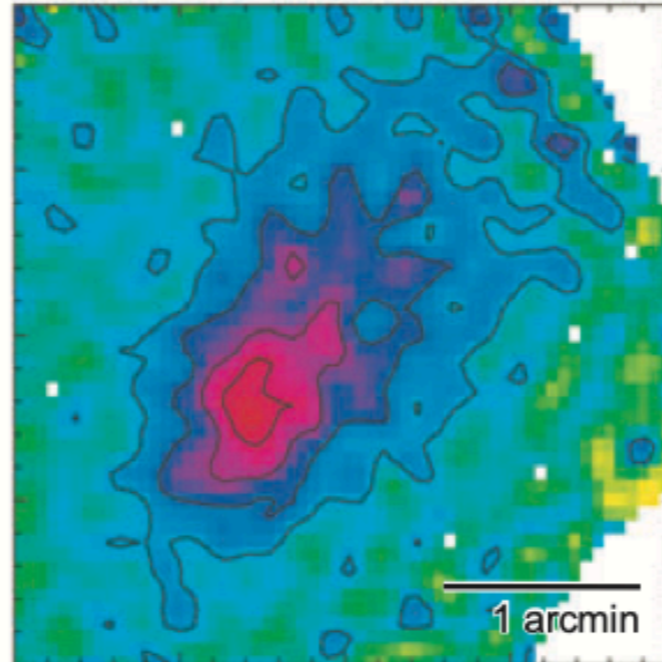


$$A_V = r_V^{H,K} E(H-K)$$

$$A_V = f N_H$$

$$N_H = (r_V^{H,K} f^{-1}) \cdot E(H-K)$$

b L1544 1.2 mm continuum



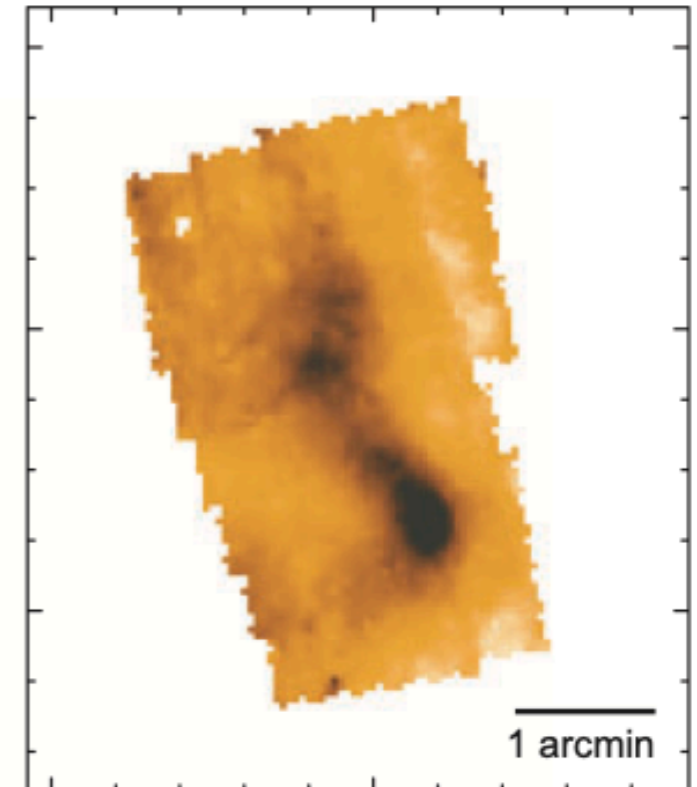
For optically thin emission:

$$I_\nu = \int \kappa_\nu \rho B_\nu(T_d) dl$$

$$I_\nu = m \langle \kappa_\nu B_\nu(T_d) \rangle N_H$$

$$N_H = I_\nu [\langle m \kappa_\nu B_\nu(T_d) \rangle]^{-1}$$

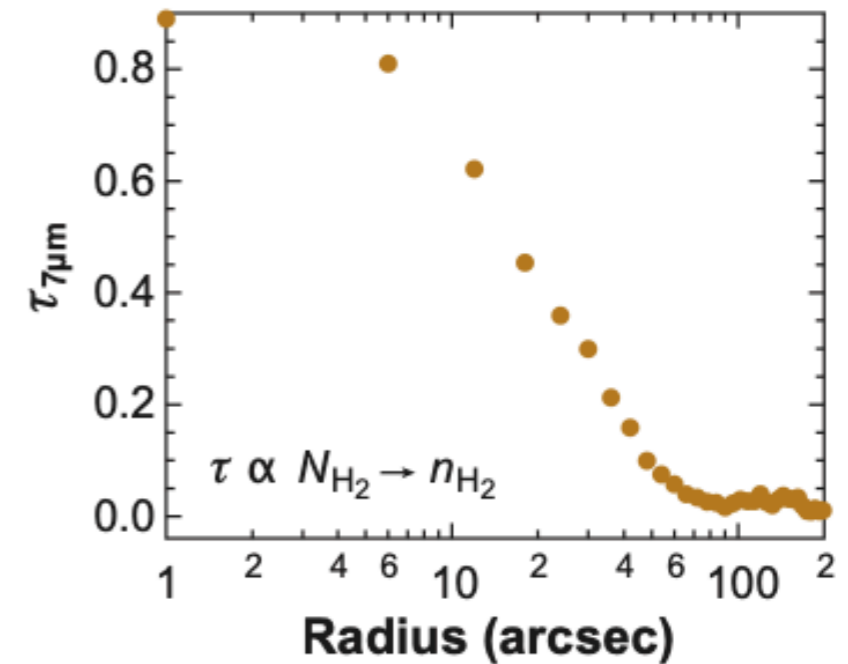
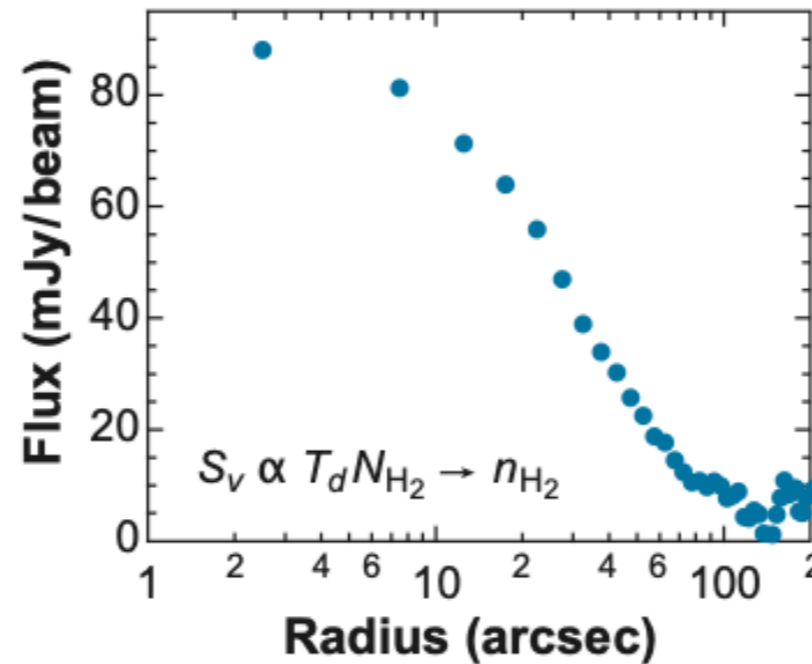
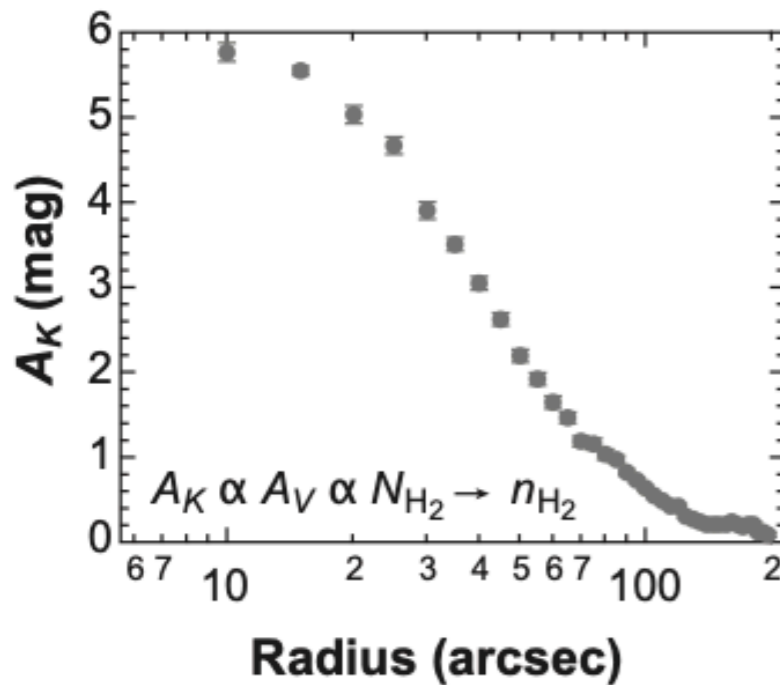
c ρ Oph core D 7 μ m image



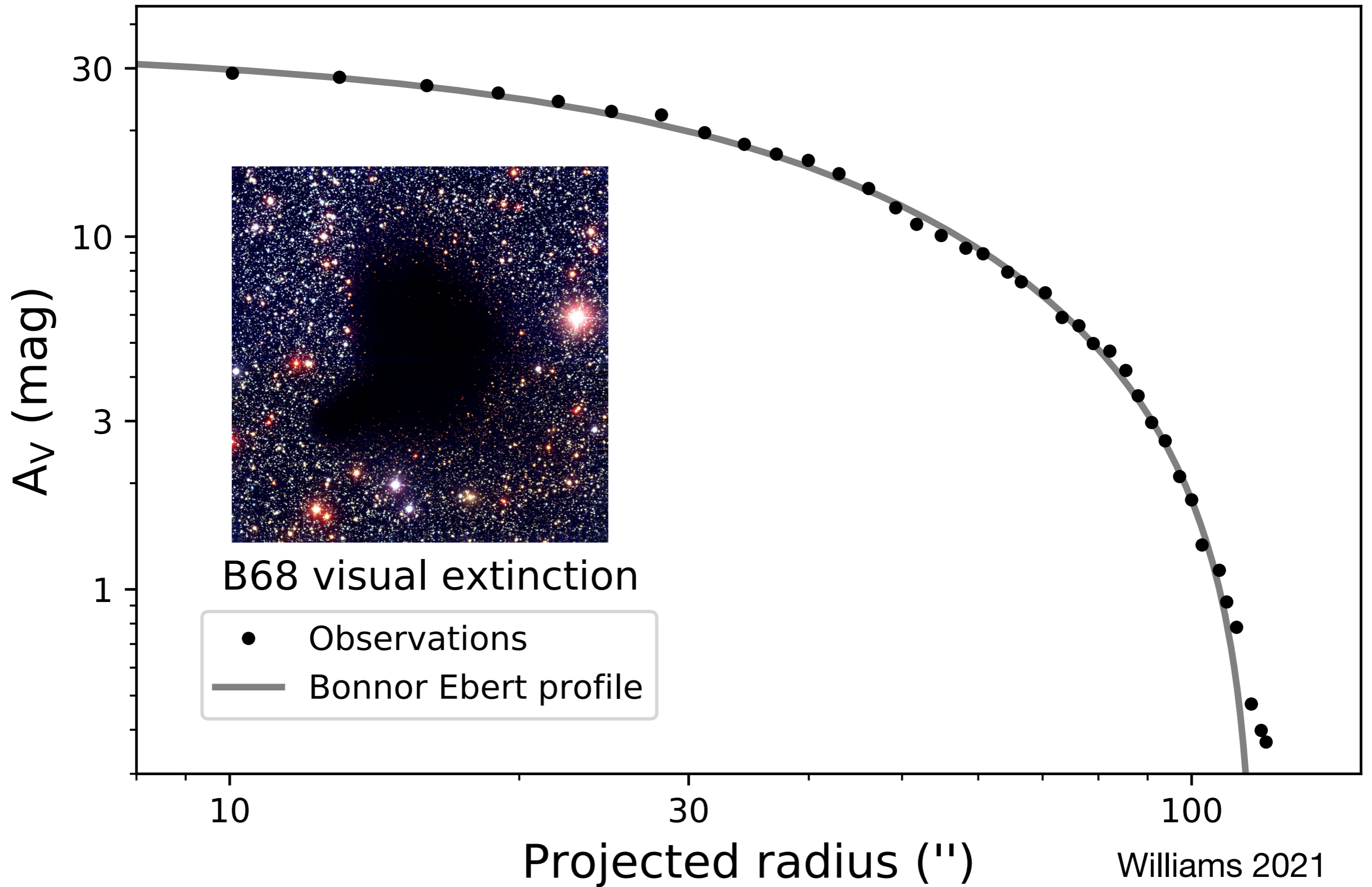
$$I_\nu = I_\nu^{bg} \exp(-\tau_\lambda) + I_\nu^{fg}$$

$$\tau_\lambda = \sigma_\lambda N_H$$

$$N_H = \frac{1}{\sigma_\lambda} \ln \left[\frac{I_\nu^{bg}}{I_\nu - I_\nu^{fg}} \right]$$



Bonnor-Ebert Sphere Fit to Extinction Data of the Barnard 68 Core



Isothermal Lane-Emden Equation

hydrostatic equilibrium: $\frac{dP}{dr} = c_s^2 \frac{d\rho}{dr} = -\rho \frac{d\Phi}{dr} \quad \Rightarrow \rho = \rho_c \exp\left(-\frac{\Phi - \Phi_c}{c_s^2}\right)$

ideal gas law: $P = \rho \frac{kT}{\mu m_p} = \rho c_s^2$ isothermal sound speed: $c_s = \sqrt{\frac{dP}{d\rho}} = \sqrt{\frac{kT}{\mu m_p}}$

Poisson Equation: $\nabla^2 \Phi = \frac{1}{r^2} \frac{d}{dr} \left(r^2 \frac{d\Phi}{dr} \right) = 4\pi G \rho$

Define dimensionless radius and potential: $x = \left(\frac{4\pi G \rho_c}{c_s^2}\right) r$ $y \equiv \frac{\Phi - \Phi_c}{c_s^2} = \ln(\rho_c / \rho)$

one obtains LEE: $\frac{1}{x^2} \frac{d}{dx} \left(x^2 \frac{dy}{dx} \right) = e^{-y}$

or: $\frac{d^2 y}{dx^2} = e^{-y} - \frac{2}{x} \frac{dy}{dx}$

Bonnor-Ebert Spheres: Non-Singular Solution of LEE

Define dimensionless radius and potential:

$$x = \left(\frac{4\pi G\rho_c}{c_s^2}\right)r$$

$$y \equiv \frac{\Phi - \Phi_c}{c_s^2} = \ln(\rho_c/\rho)$$

one obtains LEE:

$$\frac{1}{x^2} \frac{d}{dx} \left(x^2 \frac{dy}{dx} \right) = e^{-y} \quad \text{or} \quad \frac{d^2y}{dx^2} = e^{-y} - \frac{2}{x} \frac{dy}{dx}$$

boundary condition:

$$\text{at } x = 0, y = 0, \frac{dy}{dx} = 0, \rho = \rho_c \text{ at a finite value}$$

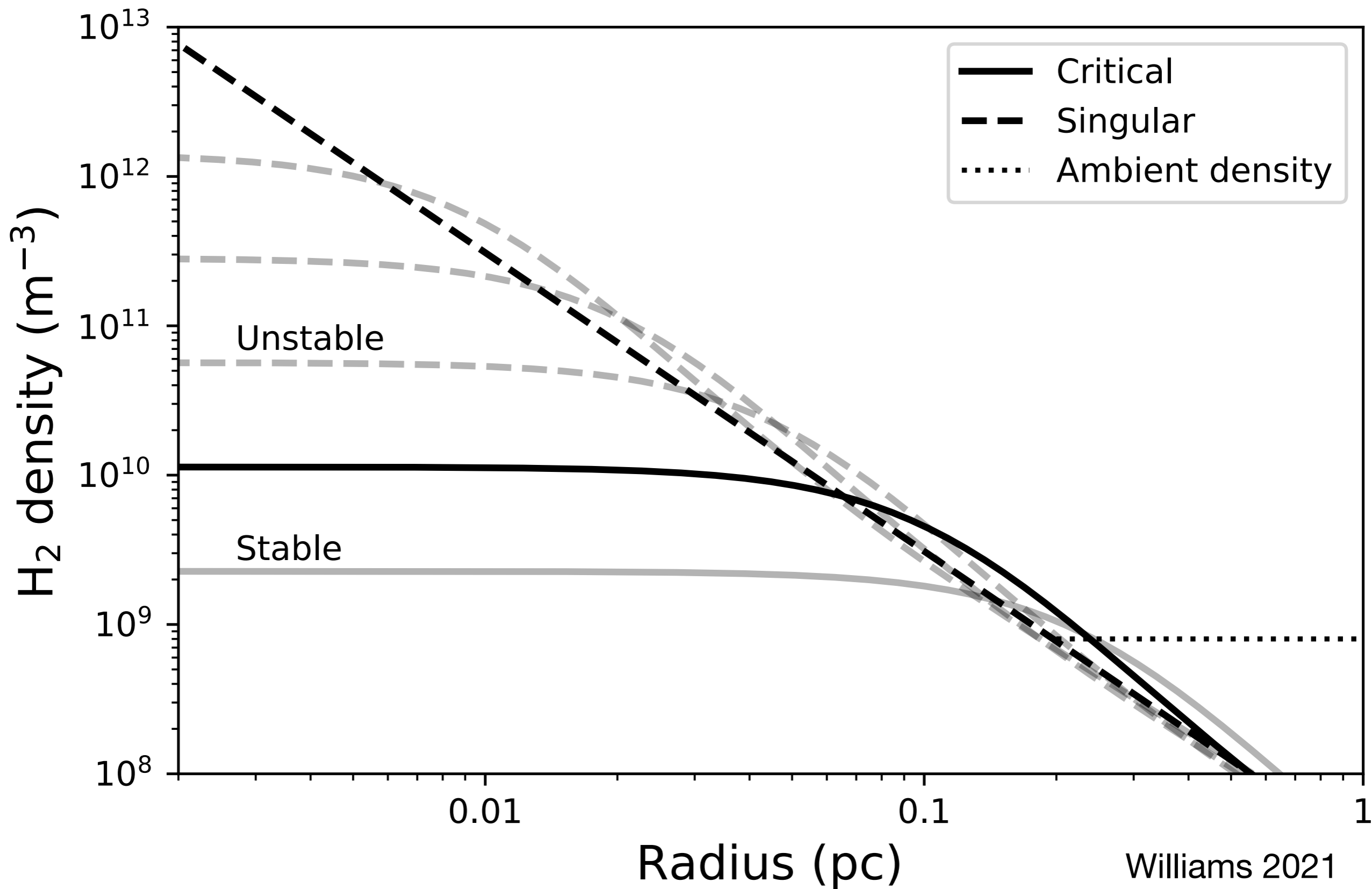
Taylor expansion:

$$y(x_0 + h) = y(x_0) + hy'(x_0) + \frac{h^2}{2}y''(x_0)$$

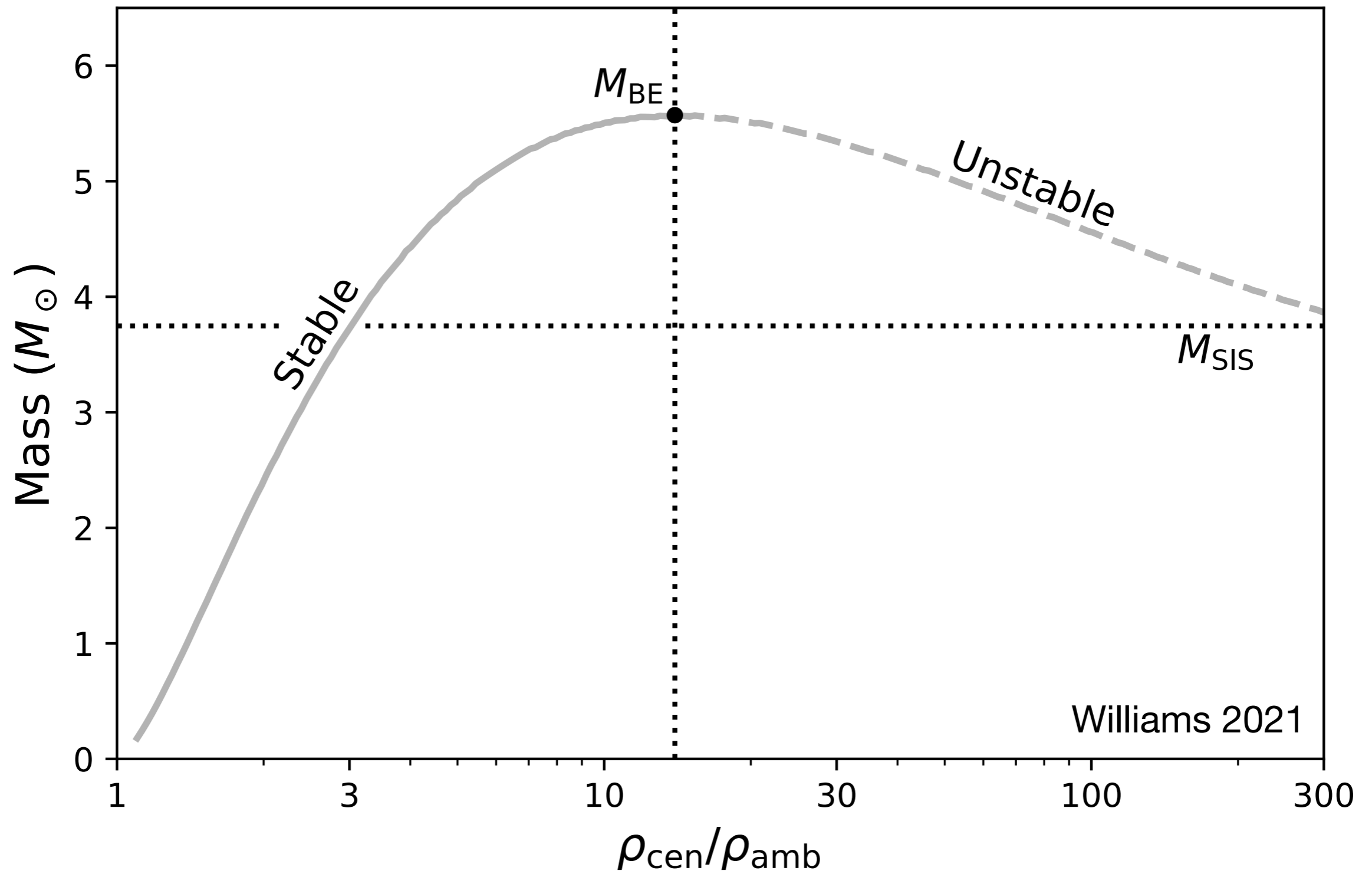
Solve by applying **Euler's method** to the LEE:

- $x_i = x_{i-1} + h$
- $y_i = y_{i-1} + y'_{i-1}h + y''_{i-1}h^2/2$
- $y'_i = y'_{i-1} + y''_{i-1}h$
- $y''_i = e^{-y_i} - 2y'_i/x_i$

Bonnor-Ebert Spheres



The Maximum Mass and the Stability of Bonnor-Ebert Sphere



Constructing a simple analytical model

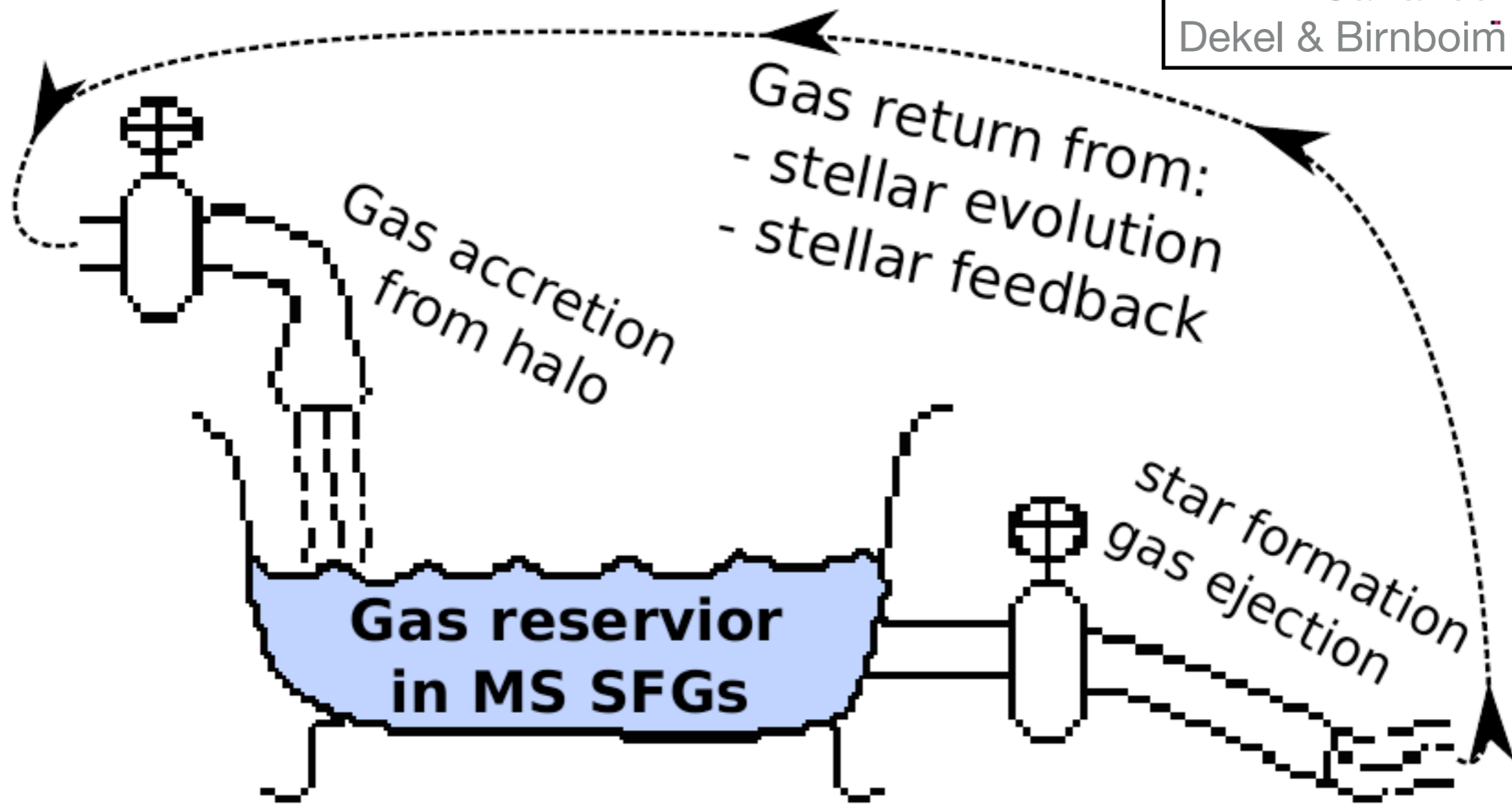
Gas accretion

Feedback:
Ejecting gas

Star Formation:
Converting gas
into stars

The “Bathtub” Model

Bouche+2010
see also Lilly+2013
Cattaneo+2006
Dekel & Birnboim 2006



A Simple Analytical Model

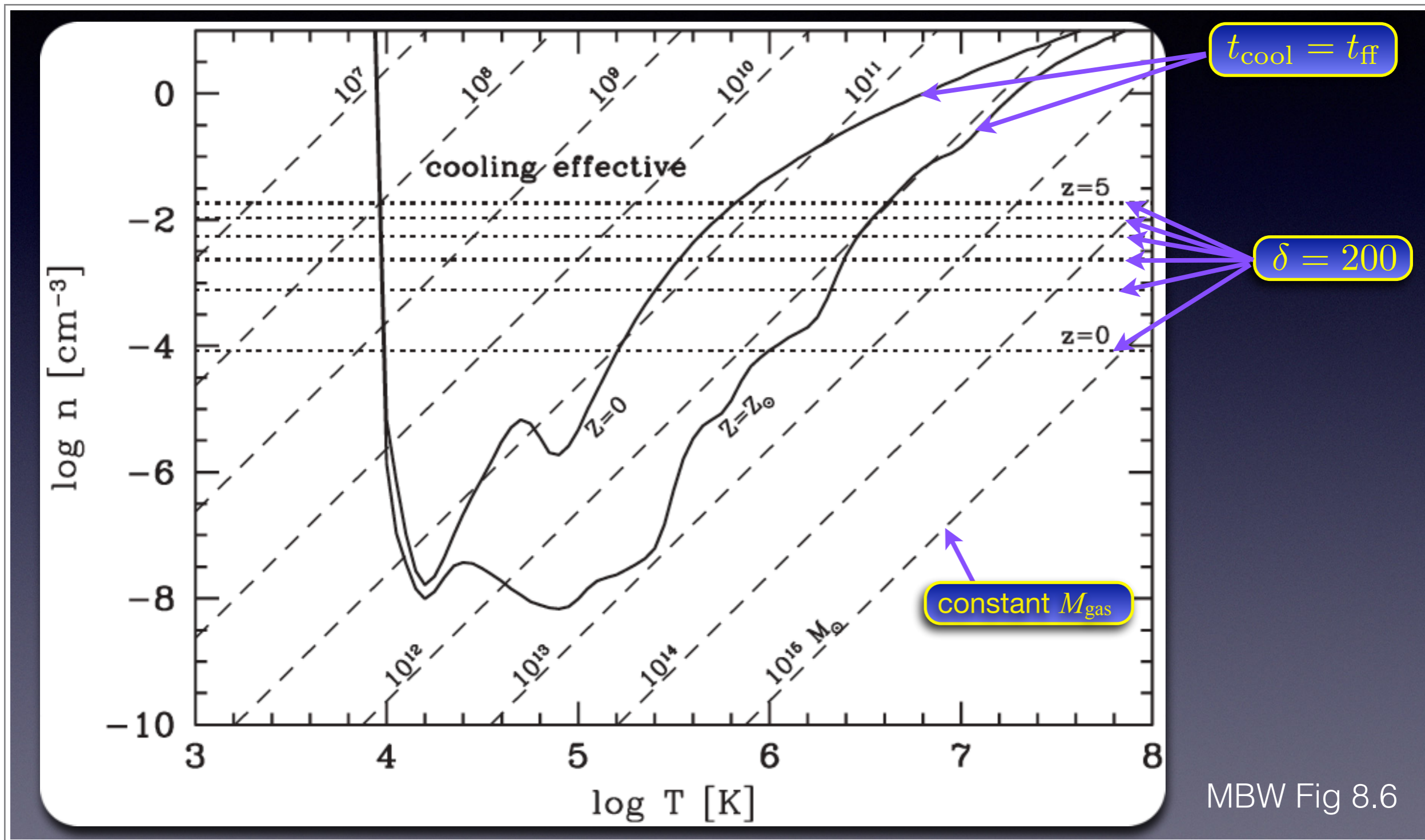
(1) a continuity equation:

Change in Cold Gas Reservoir **Accretion Rate** \propto **Halo Growth Rate** **Gas Consumption Rate** \propto **Star Formation Rate**

$$\frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \frac{dM_{\text{star}}}{dt}$$

where stellar growth decouples from halo growth, as specified by the cold gas accretion efficiency (ϵ_{cold}) that depends on halo mass

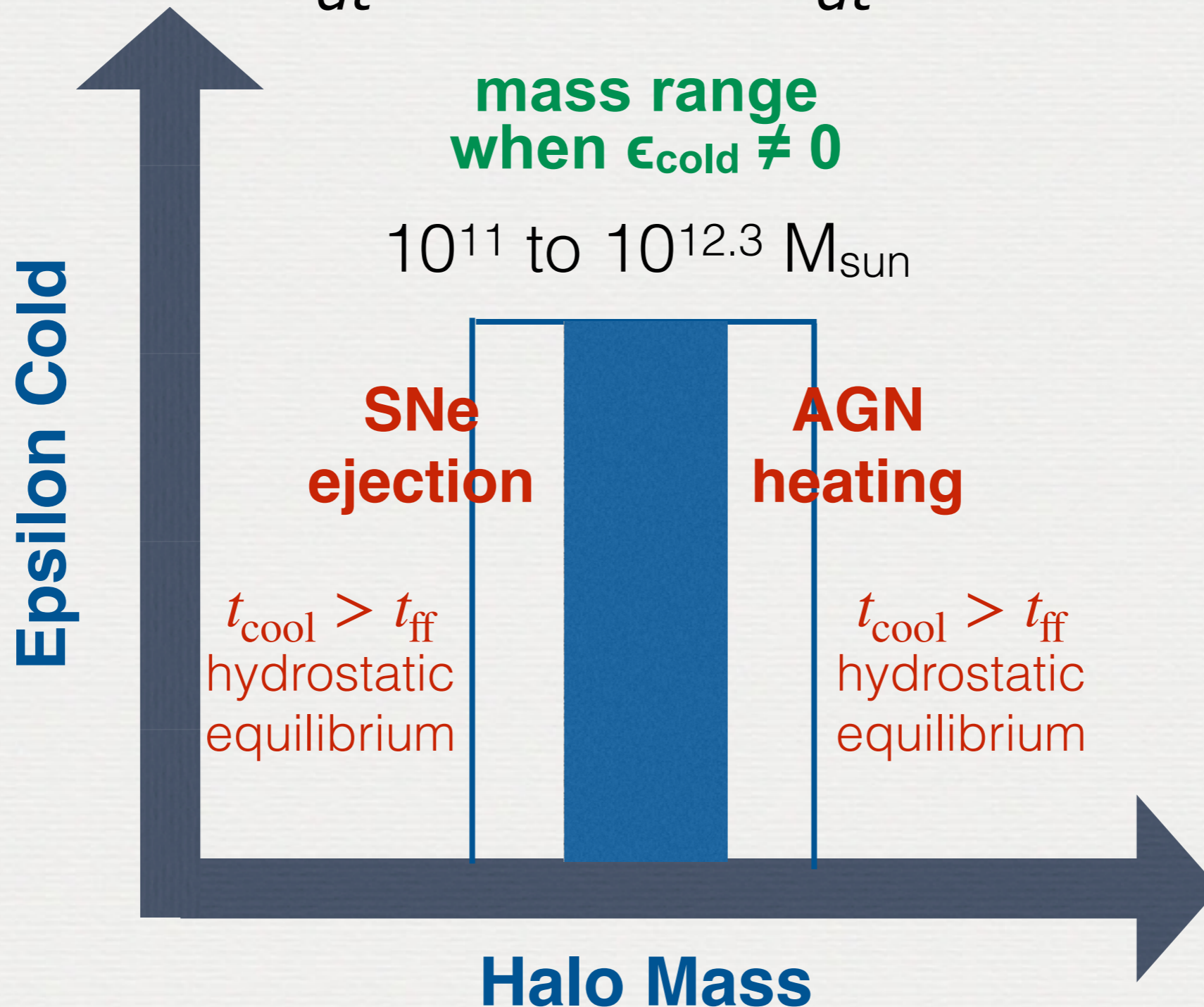
Virialized halo gas cools effectively only in the mass range where $t_{\text{cool}} < t_{\text{ff}}$



MBW Fig 8.6

The Cold Gas Accretion Rate

$$\frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt}$$



The "Bathtub" Model

(1) a continuity equation:

**Change in Cold
Gas Reservoir**

**Accretion Rate \propto
Halo Growth Rate**

**Gas Consumption Rate \propto
Star Formation Rate**

$$\frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \frac{dM_{\text{star}}}{dt}$$

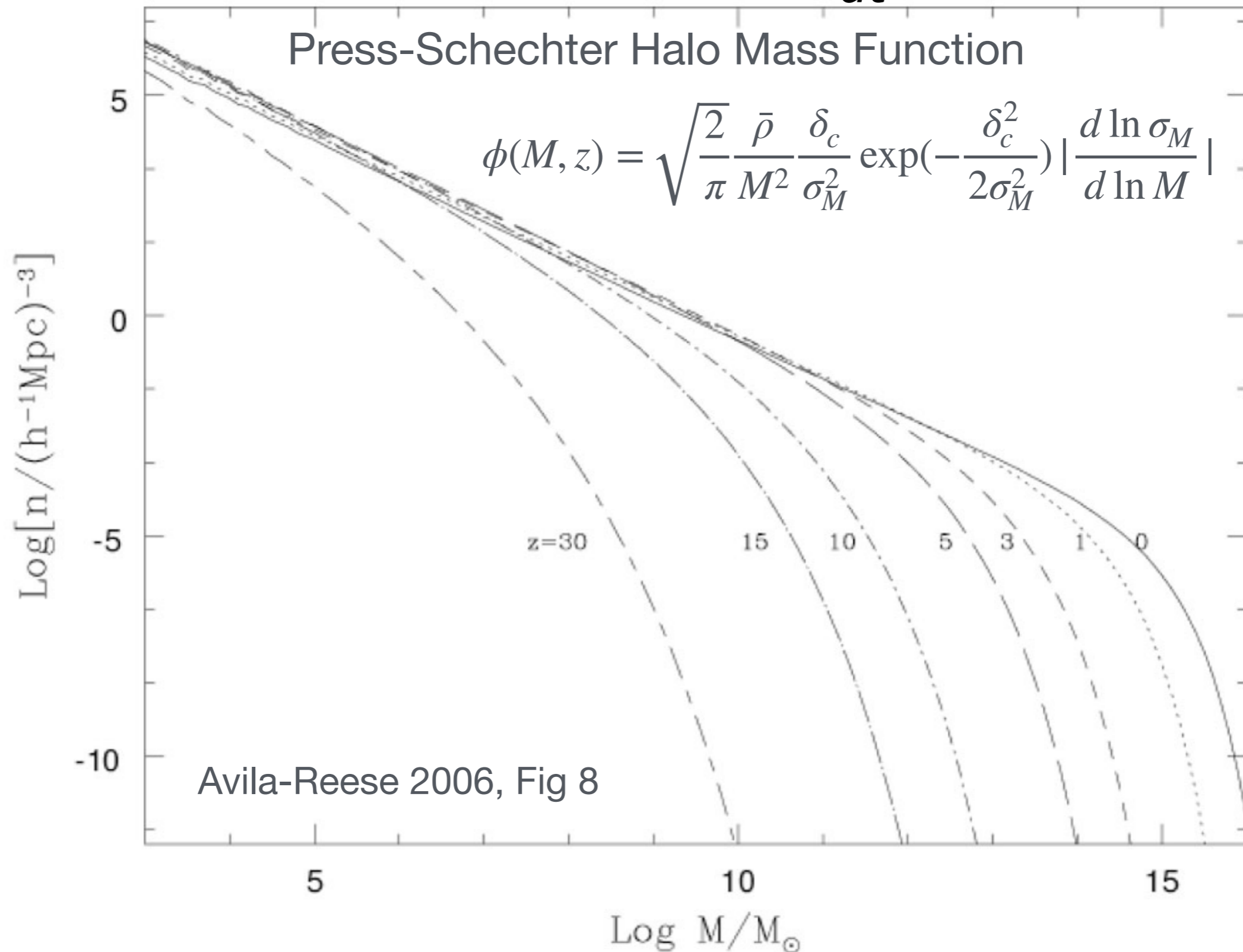
Where stellar growth decouples from halo growth is specified by the cold gas accretion efficiency (ϵ_{cold})

$$\left\{ \begin{array}{l} \epsilon_{\text{cold}} = 0.0 \text{ if } M_{\text{halo}} < 10^{11} M_{\odot} \\ \epsilon_{\text{cold}} = 0.7 \text{ if } 10^{11} < M_{\text{halo}} < 10^{12.3} M_{\odot} \\ \epsilon_{\text{cold}} = 0.0 \text{ if } M_{\text{halo}} > 10^{12.3} M_{\odot} \end{array} \right.$$

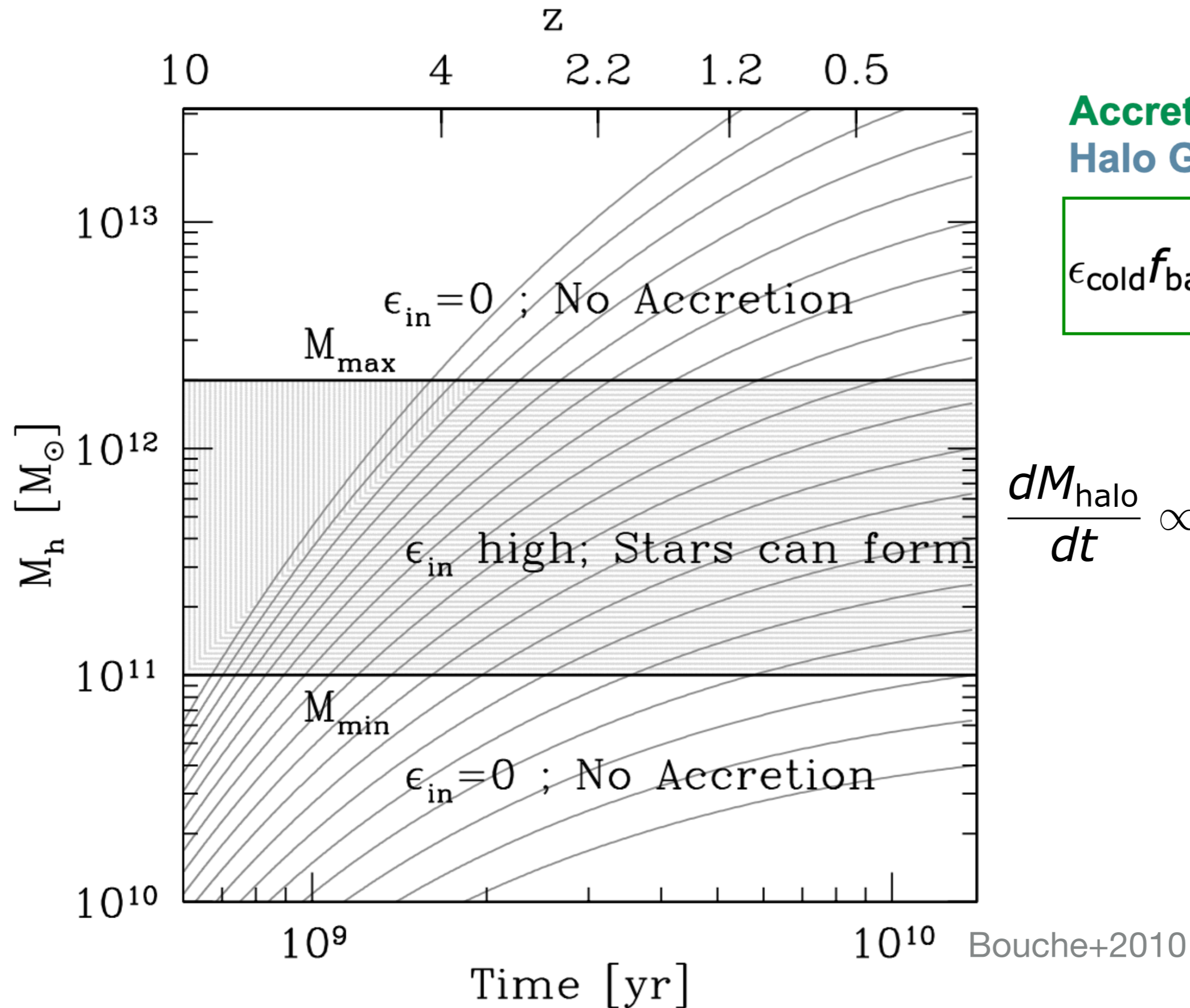
But we need two additional equations to solve the continuity equation.

The "Bathtub" Model

(2) halo growth from PS formalism: $\frac{dM_{\text{halo}}}{dt} \propto M_{\text{halo}}^{1.1} (1+z)^{2.2}$



Halo mass vs. redshift & time



Accretion Rate \propto
Halo Growth Rate

$$\epsilon_{cold} f_{baryon} \frac{dM_{halo}}{dt}$$

$$\frac{dM_{halo}}{dt} \propto M_{halo}^{1.1} (1+z)^{2.2}$$

The "Bathtub" Model

(3) a star formation law, $\dot{M}_{\text{star}} \propto M_{\text{gas}}$

Change in Cold Gas Reservoir \propto **Accretion Rate** \propto **Halo Growth Rate**

Gas Consumption Rate \propto **Star Formation Rate**

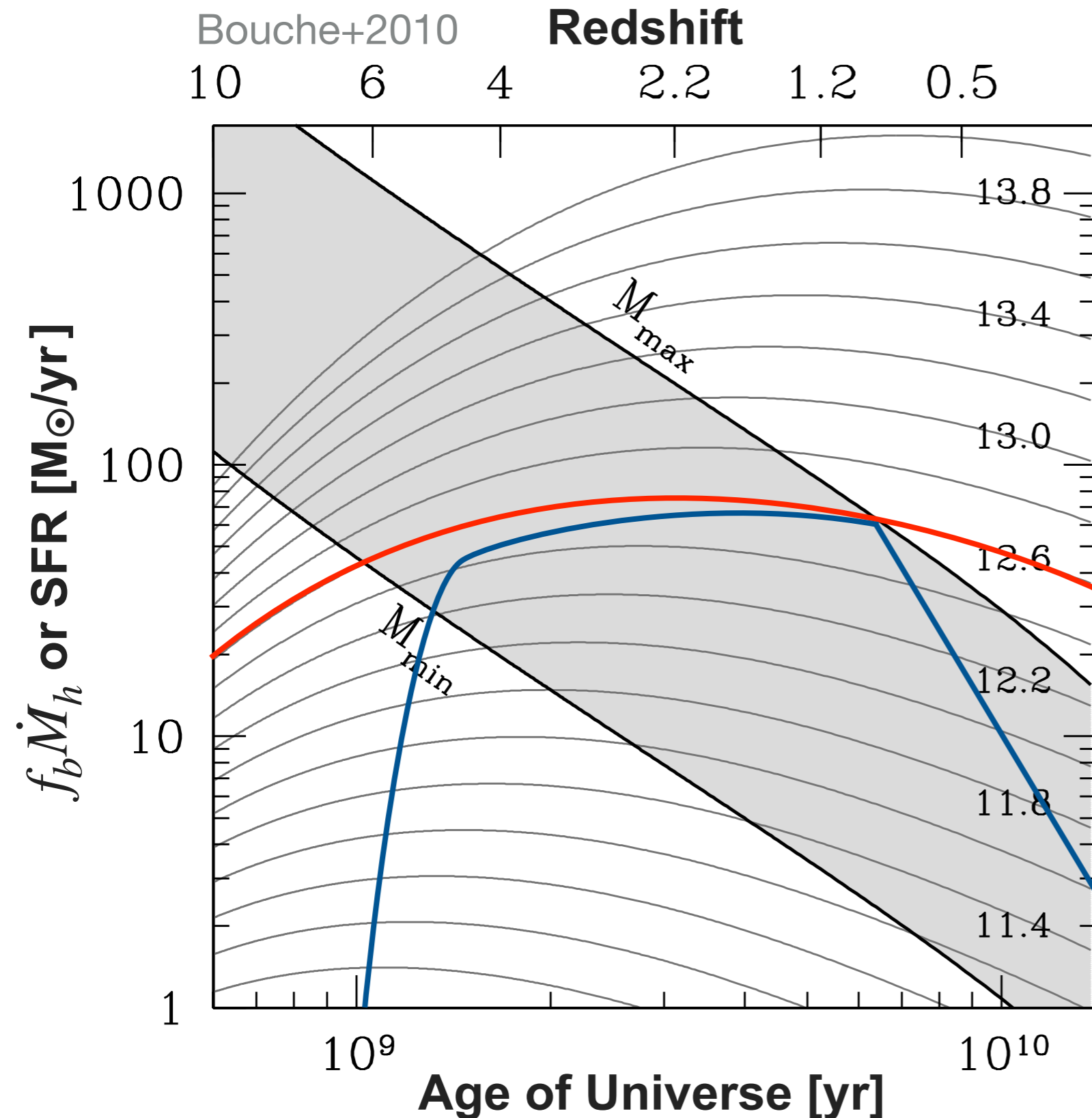
$$\left\{ \begin{array}{l} \frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \frac{dM_{\text{star}}}{dt} \\ \frac{dM_{\text{halo}}}{dt} \propto M_{\text{halo}}^{1.1} (1+z)^{2.2} \quad \leftarrow \text{Halo Growth Rate from EPS} \\ \frac{dM_{\text{star}}}{dt} = \text{SFR} = \epsilon_{\text{SF}} \frac{M_{\text{gas}}}{\tau_{\text{dyn}}} \quad \leftarrow \text{Star Formation Law} \end{array} \right.$$

cold gas accretion efficiency:

recycle & feedback:

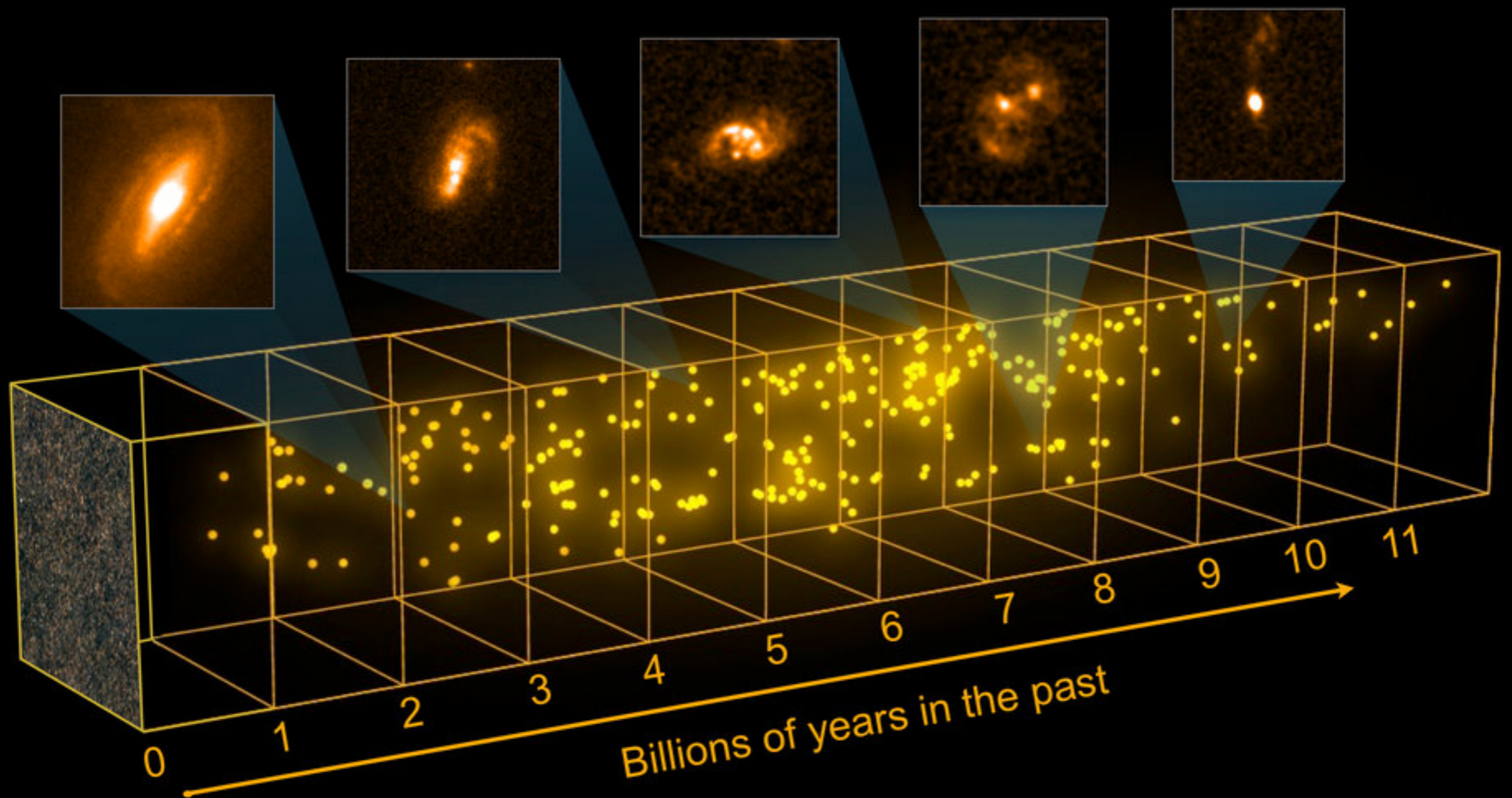
$$\left\{ \begin{array}{l} \epsilon_{\text{cold}} = 0.0 \text{ if } M_{\text{halo}} < 10^{11} M_{\odot} \\ \epsilon_{\text{cold}} = 0.7 \text{ if } 10^{11} < M_{\text{halo}} < 10^{12.3} M_{\odot} \\ \epsilon_{\text{cold}} = 0.0 \text{ if } M_{\text{halo}} > 10^{12.3} M_{\odot} \end{array} \right. \quad \left\{ \begin{array}{l} f_{\text{recycle}} = 0.5 \\ f_{\text{outflow}} = 0.6 \end{array} \right.$$

Accretion-Driven Star Formation History

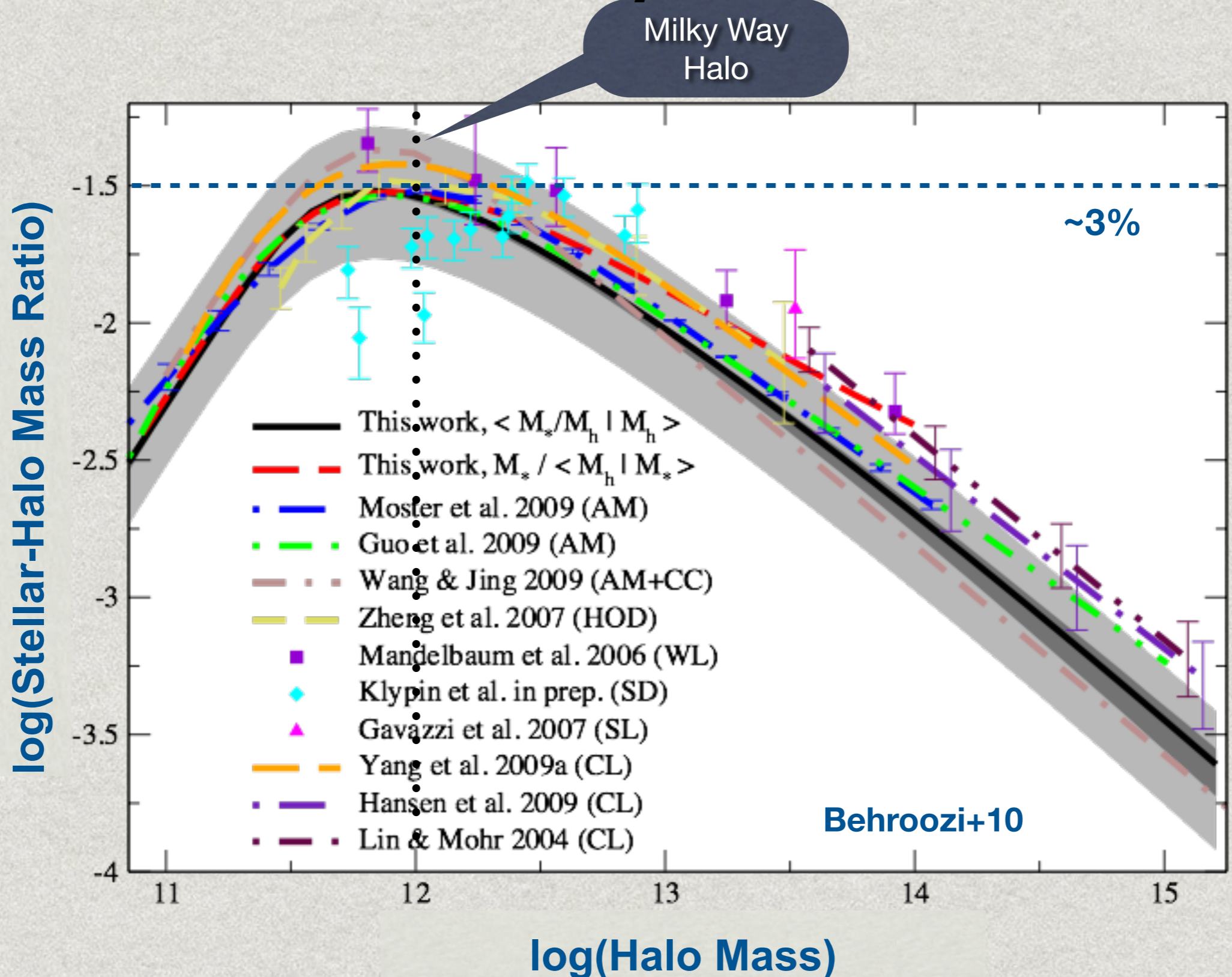


- ▶ **Grey region:** efficient cold gas accretion
 $10^{11} < M_{\text{Halo}} < 1.5 \times 10^{12} M_\odot$
- ▶ **Gas accretion history** of a $10^{12.6} M_\odot$ halo (mass at $z = 0$)
- ▶ **Star formation history** from the continuity equation:
 1. Once the halo crosses the minimum mass ($10^{11} M_\odot$), the SFR rapidly rises to reach a steady state;
 2. As the halo mass reaches $10^{12.3} M_\odot$, cold gas accretion is choked and the SFR starts to decline with an e-folding time of **2-3 Gyr** ($= 2 \tau_{\text{dyn}} / \epsilon_{\text{SF}}$).

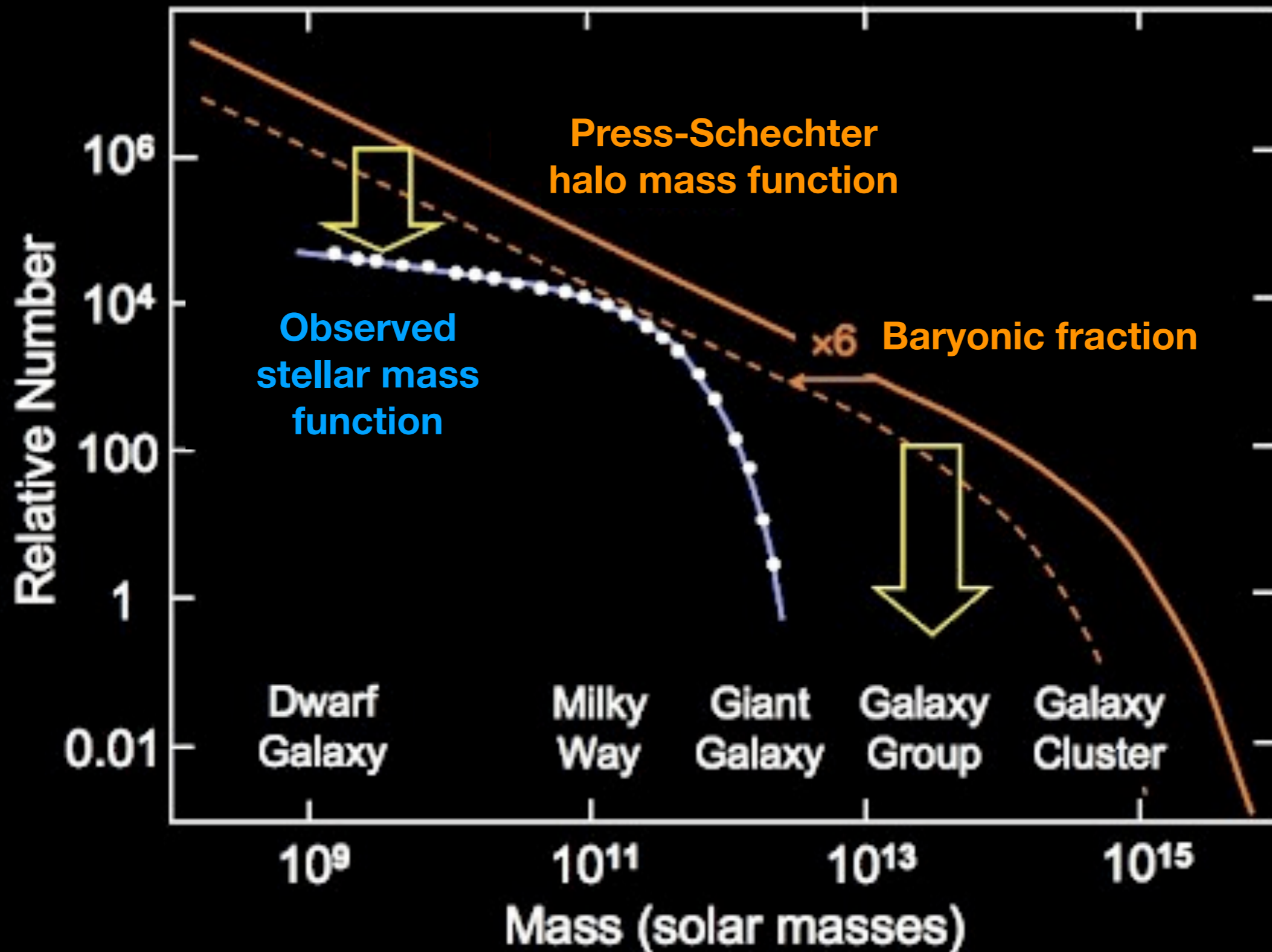
The simple “bathtub” model needs to explain key observational results



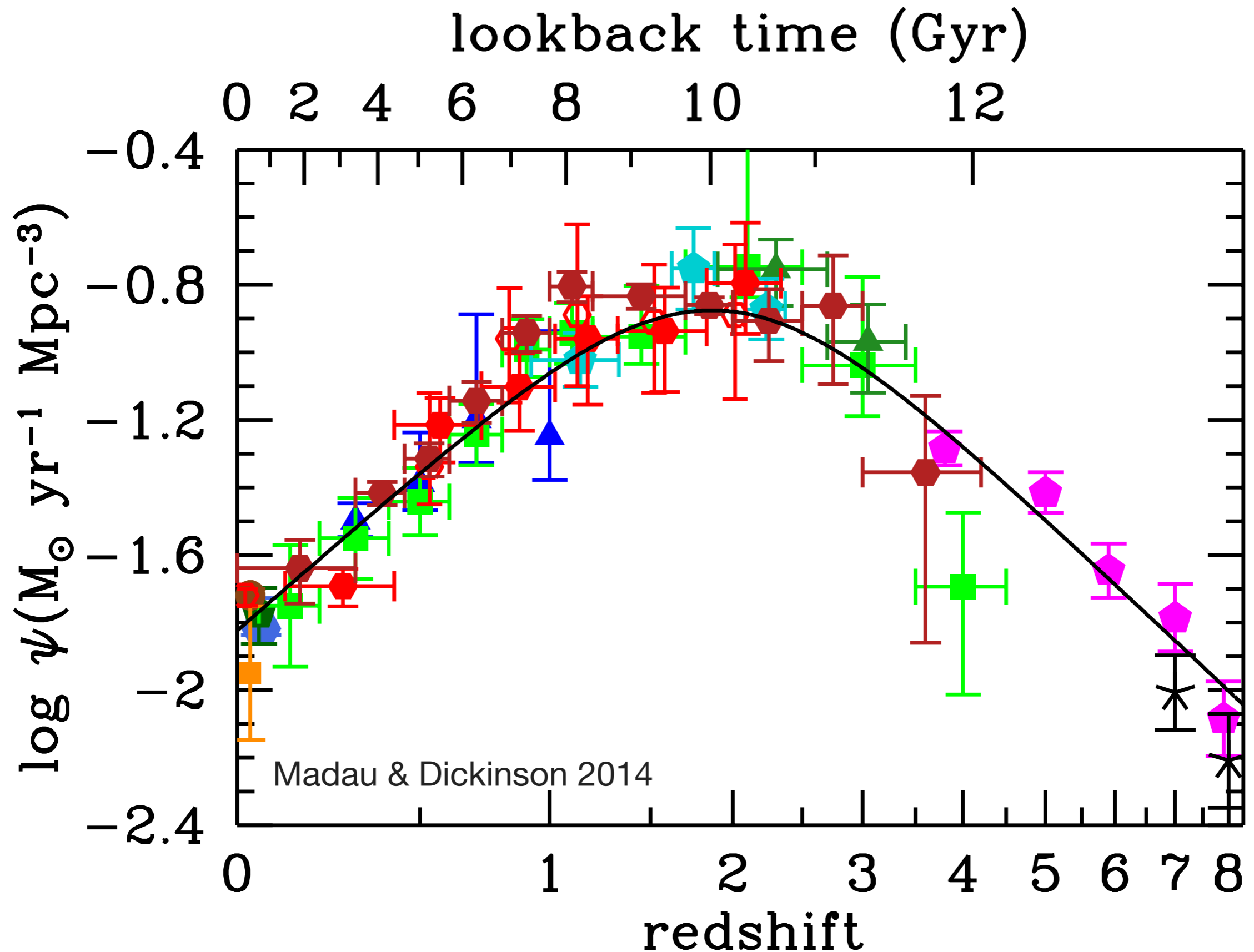
Stellar Mass Fraction Today = Stellar Mass/Halo Mass



Problem: Stellar mass is a biased tracer of halo mass

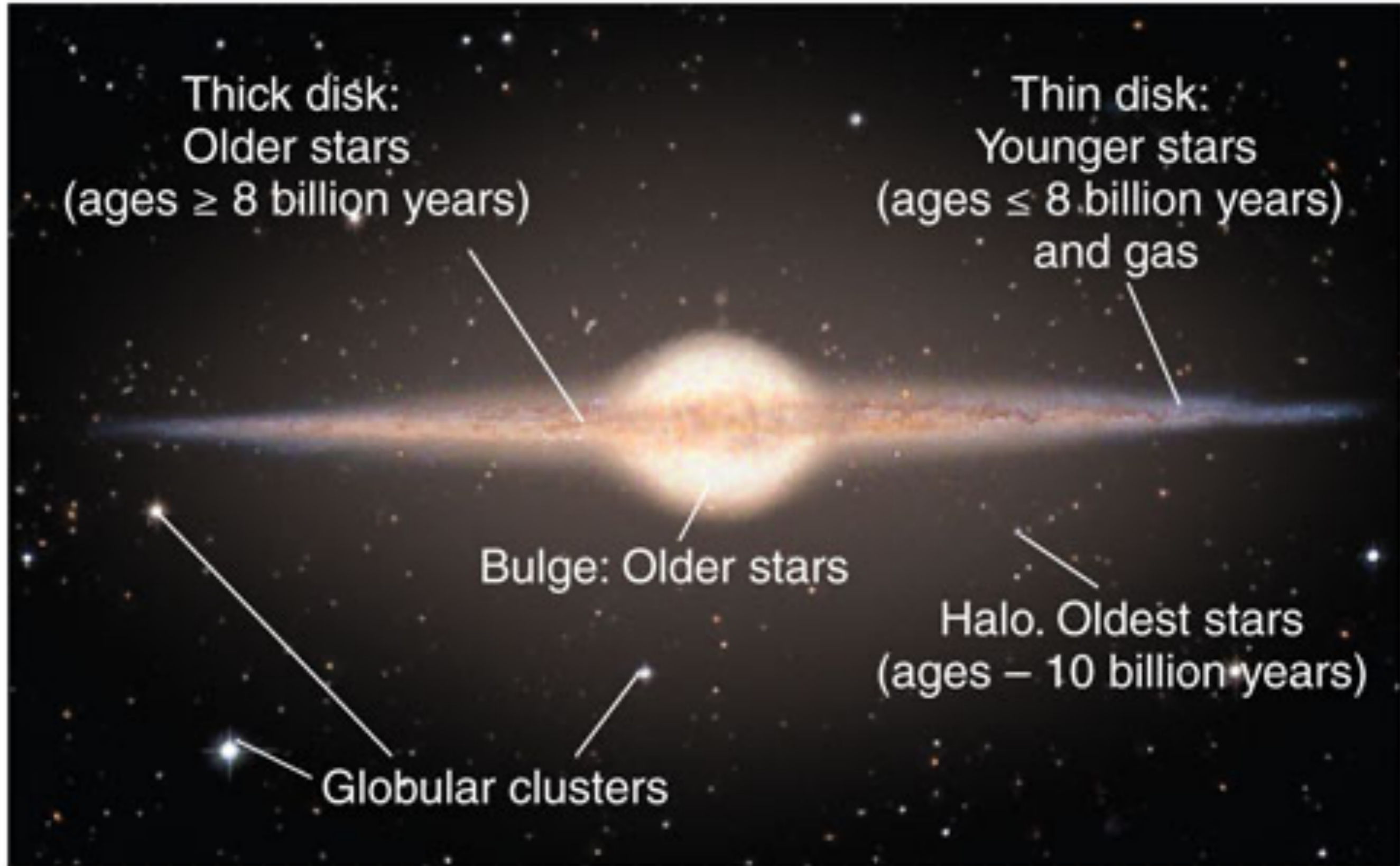


Cosmic Star Formation History



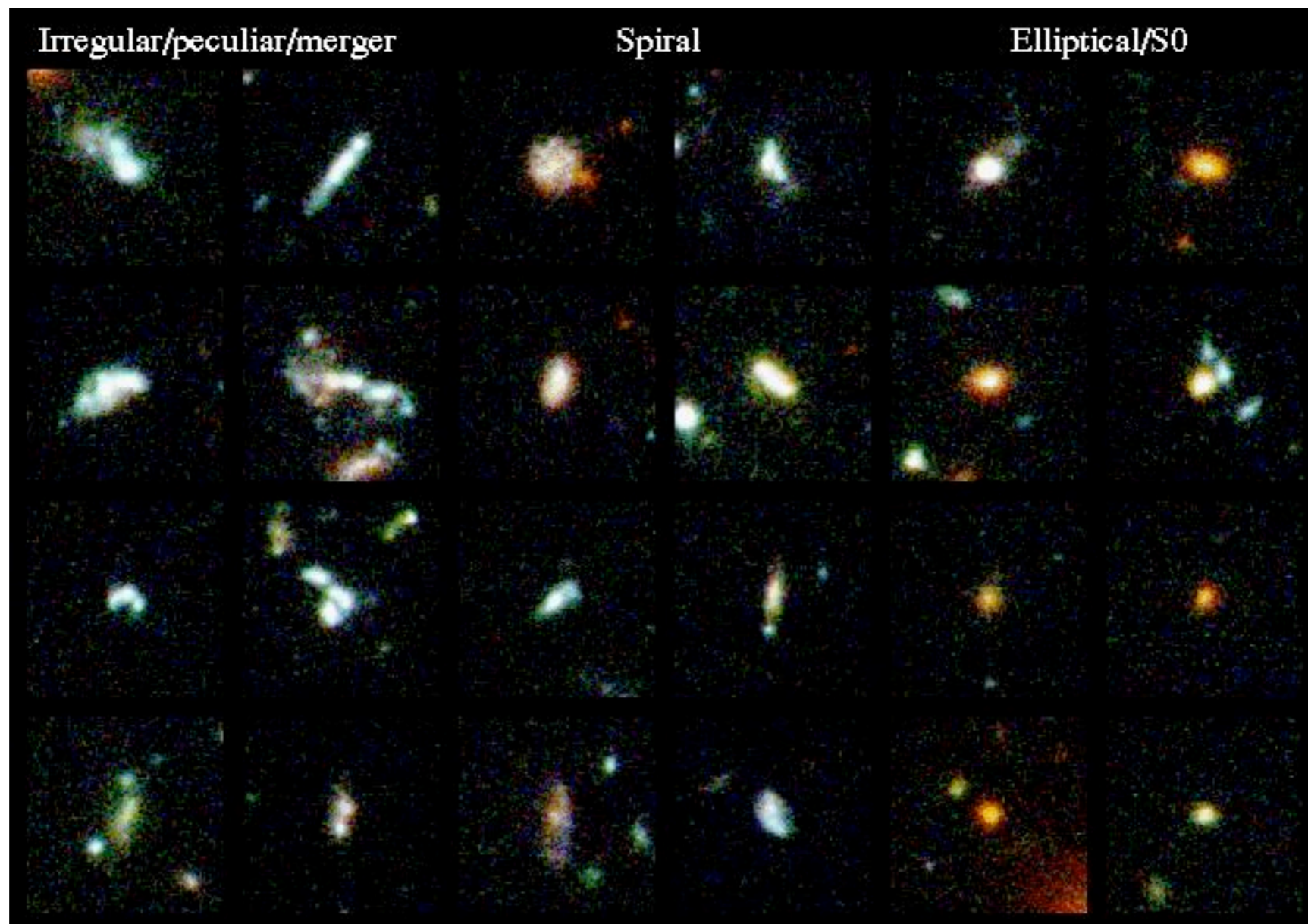
**How to measure stellar mass and
star formation rates in distant
galaxies?**

The Milky Way: A Mixture of Stellar Populations

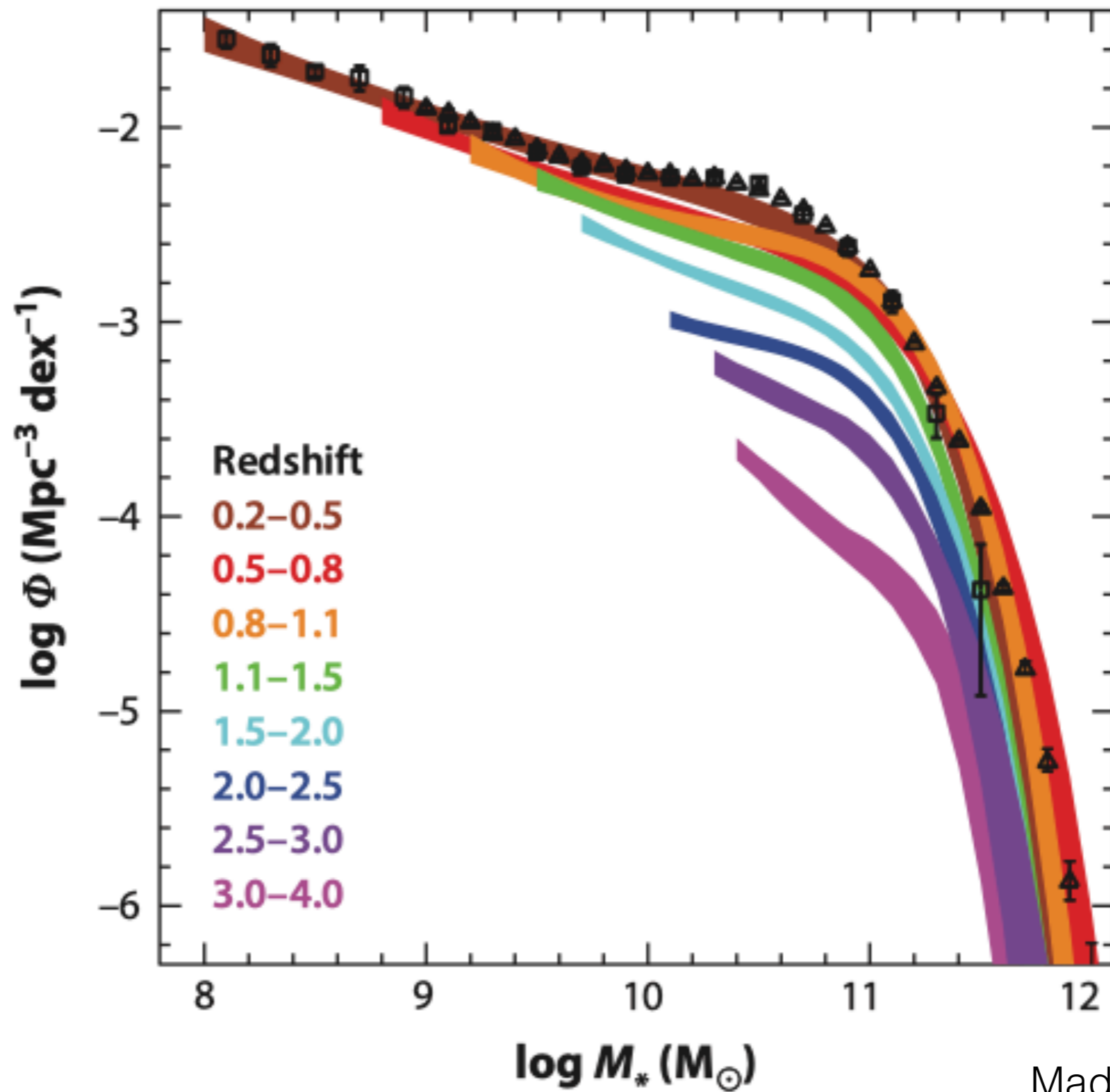


Non-resolved Populations

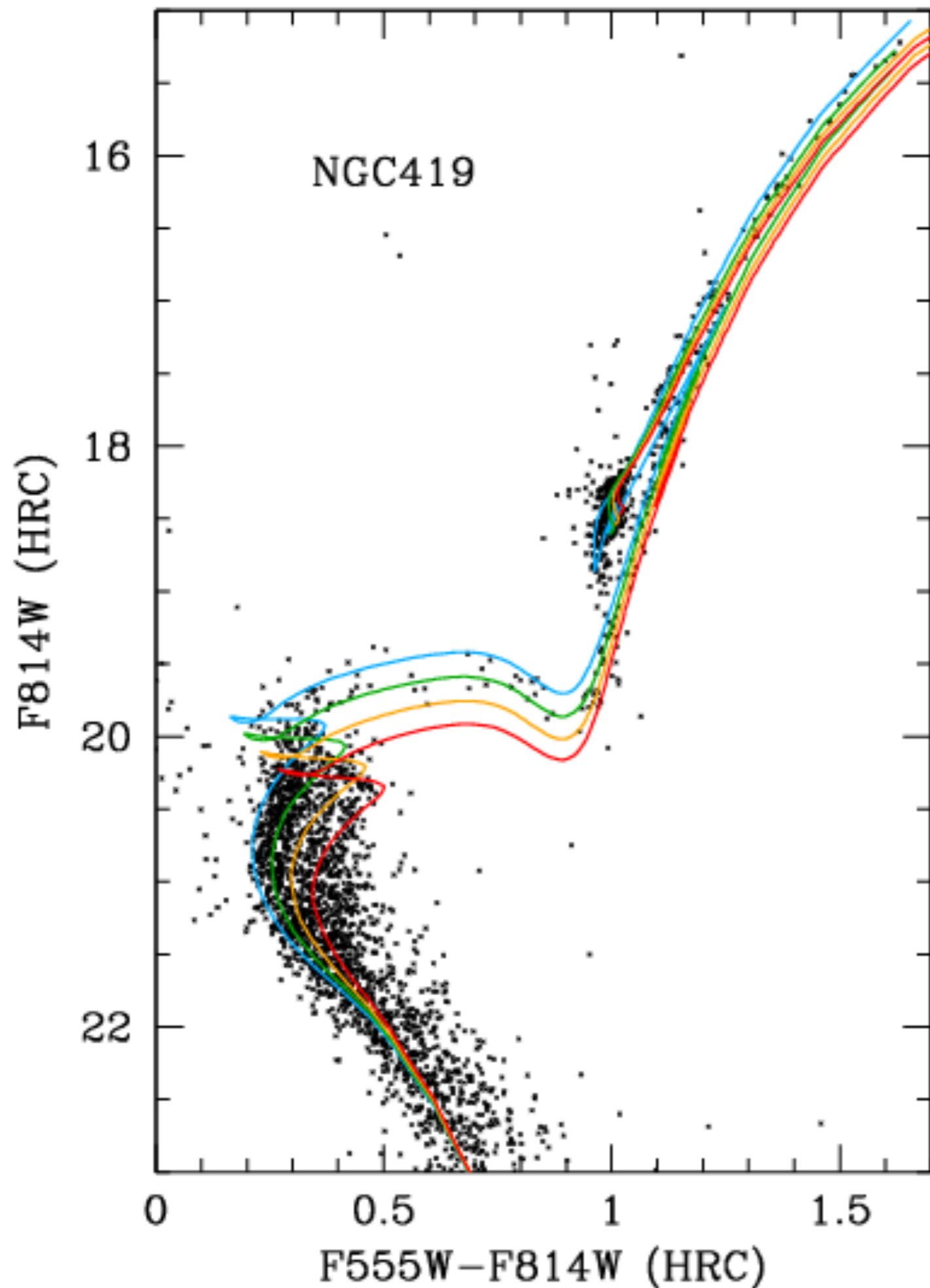
- Galaxies formed by several SSPs, sometimes we only know their integrated light spectra.
- Integrated light of a galaxy: colours, SED, spectra



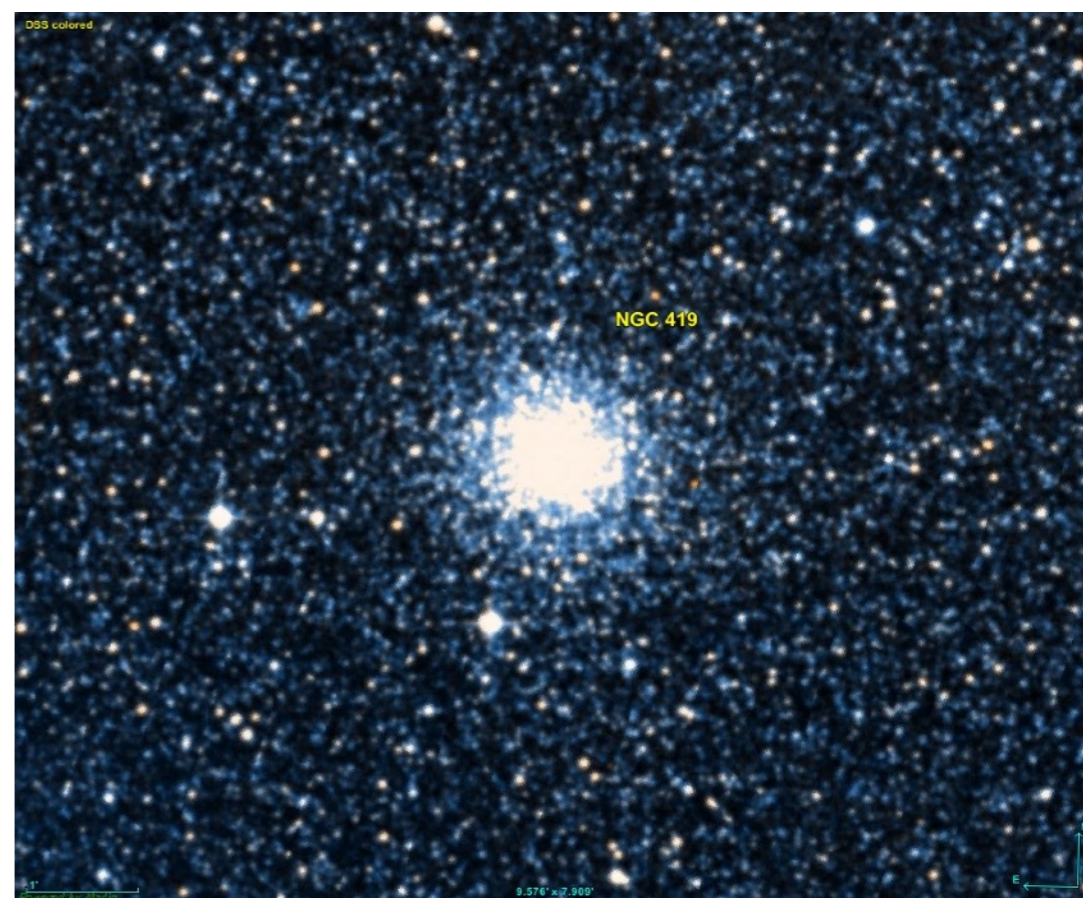
Evolution of Stellar Mass Function between $0 < z < 4$



Simple Stellar Population (SSP)



- Bressan+2012
- The star cluster NGC 419
- The isochrones are for $Z = 0.004$, ages $\log(t/\text{yr}) = 9.15, 9.20, 9.25, 9.30$



Isochrones of stellar populations vs. evolution tracks of individual stars

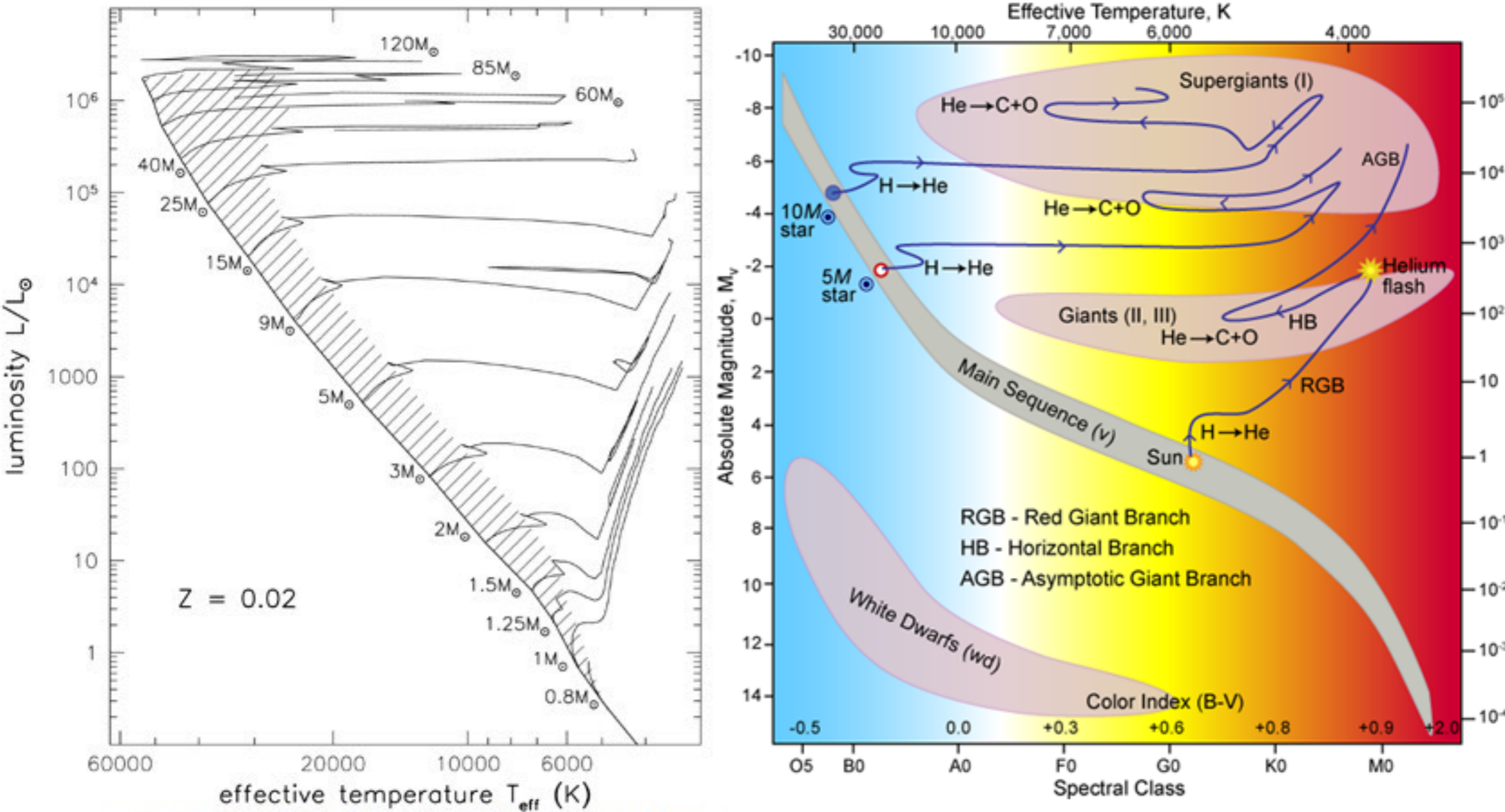


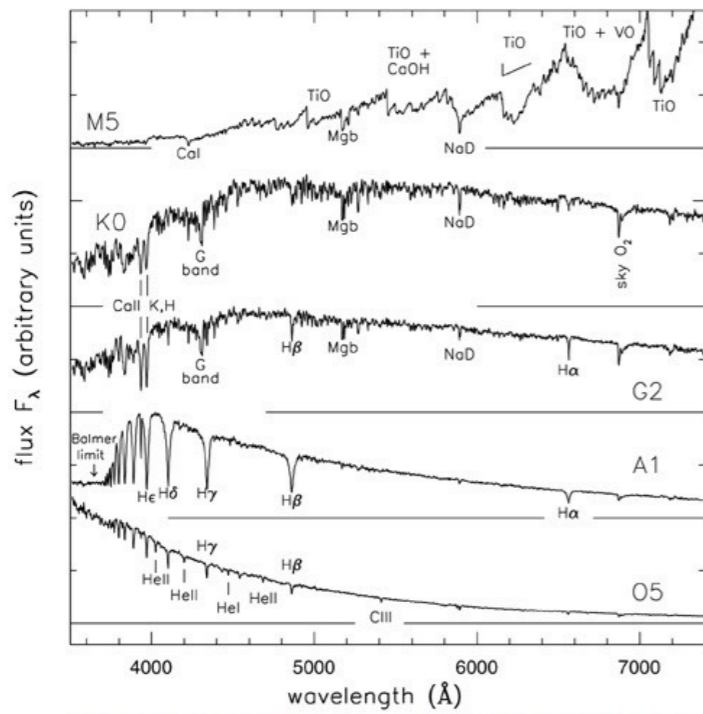
Fig 1.4 'Galaxies in the Universe' Sparke/Gallagher CUP 2007

Spectra of Simple Stellar Populations (SSPs)

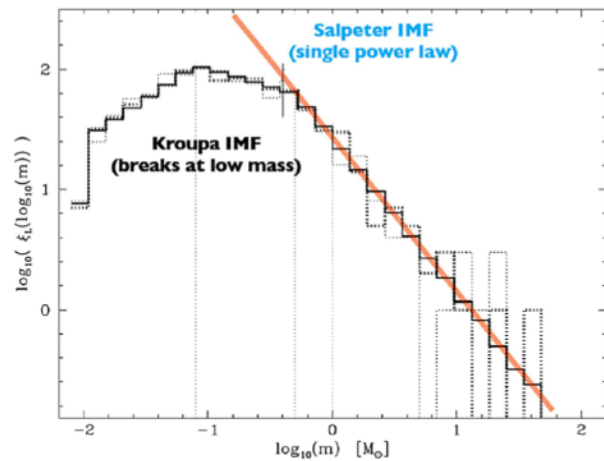
$$l_{\lambda}^{\text{SSP}}(t, [M/H]) = \iint l_{\lambda}^*(L, T) p(L, T | t, [M/H], \text{IMF}, \text{SEM}) dL dT$$

simple means single age & metallicity

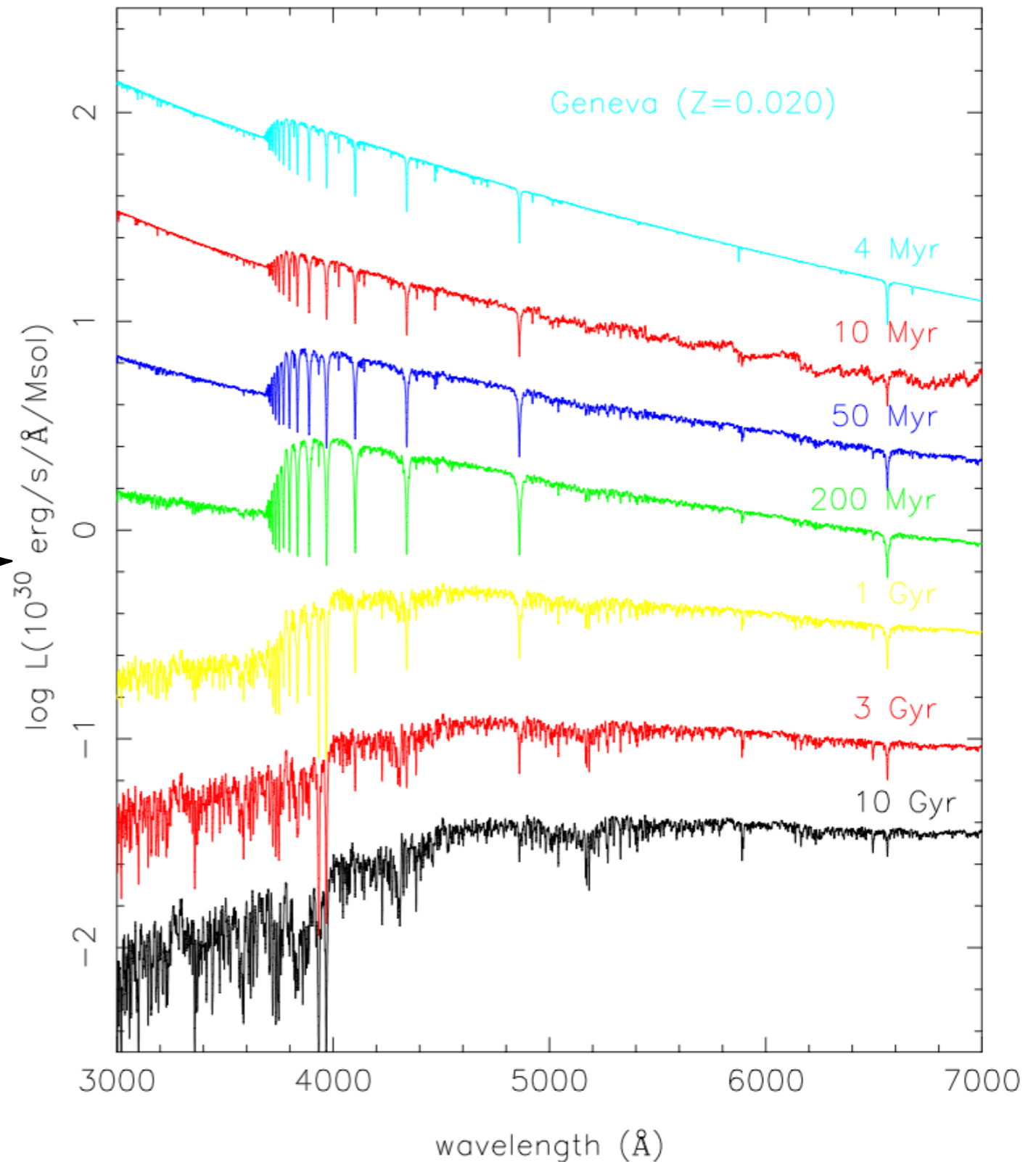
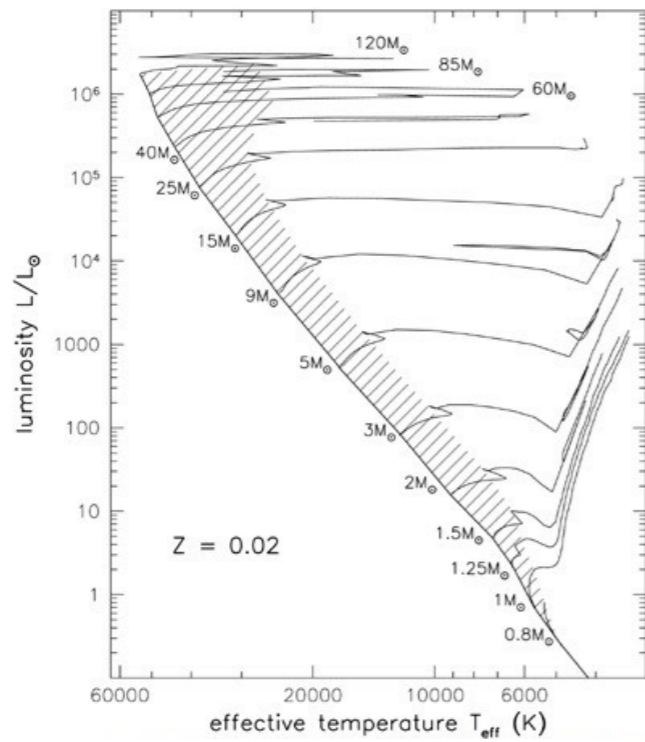
spectral library of individual stars:
 $l_{\lambda}^*(L, T)$



initial mass function (IMF):
 $p(m) = p(L) \frac{dL}{dm}$



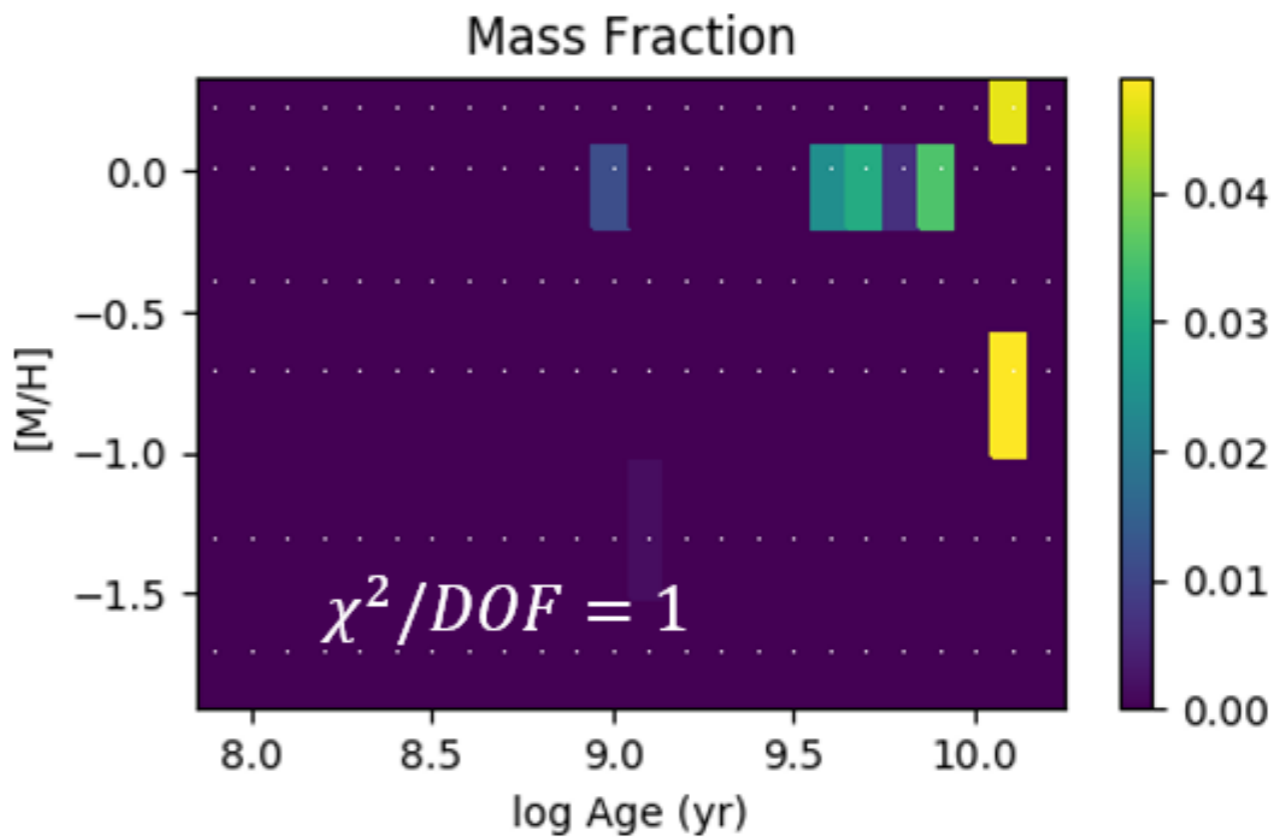
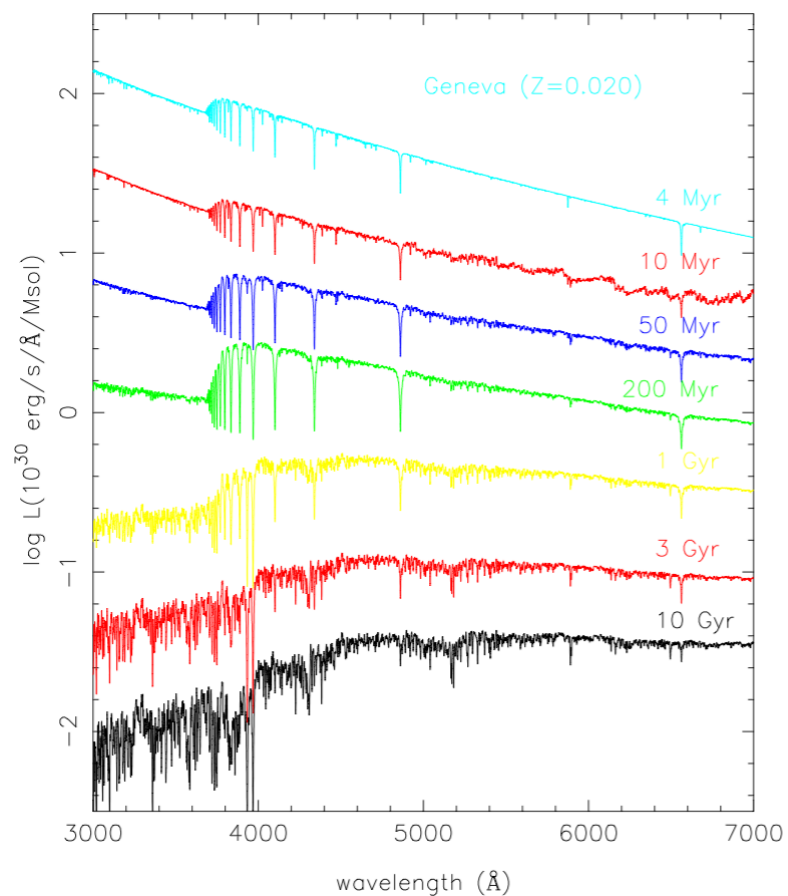
stellar evolution models (SEM)



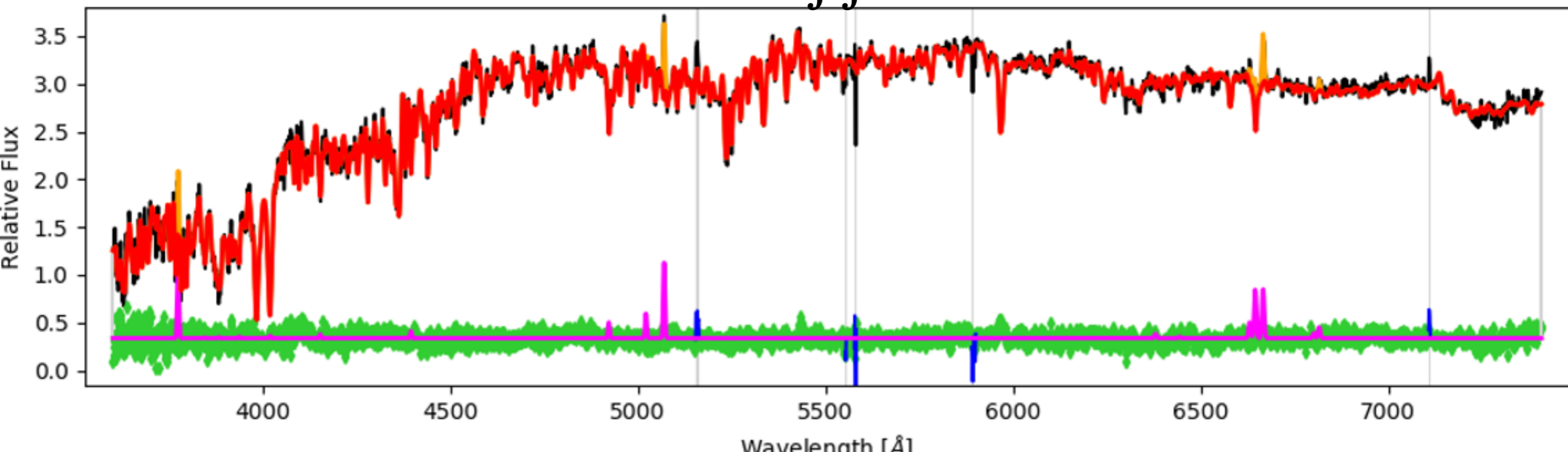
Complex Stellar Population (CSP)

SSP library: $l_\lambda(t, [M/H])$

Weights of SSPs: $p(t)p([M/H])$



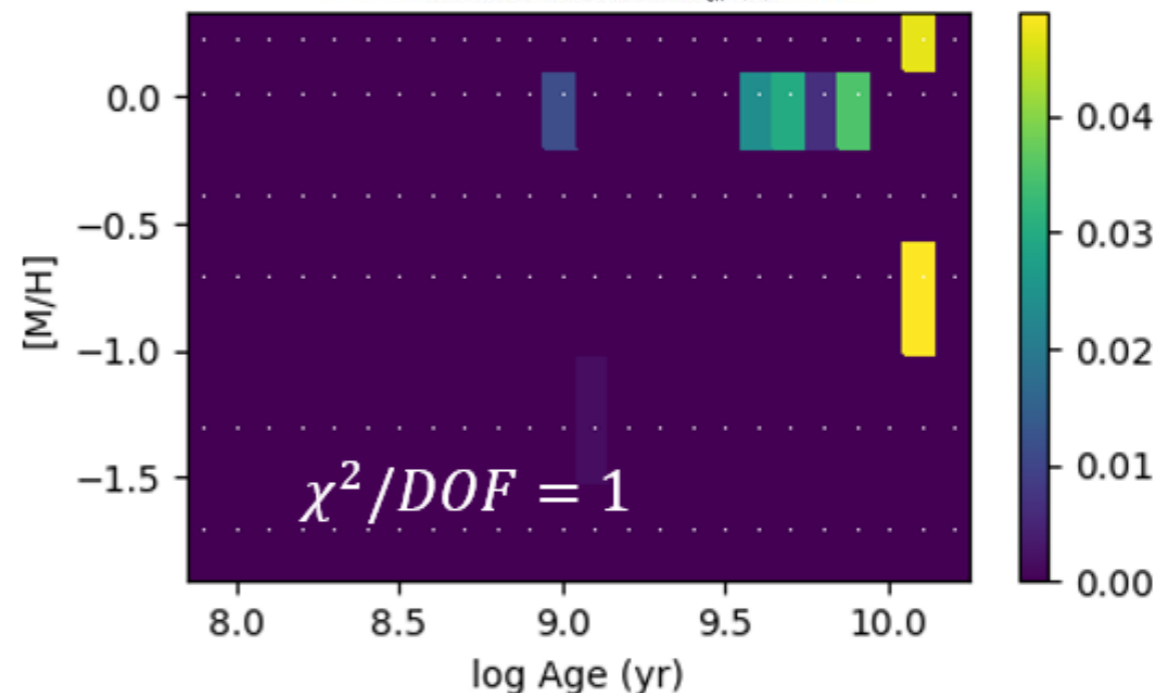
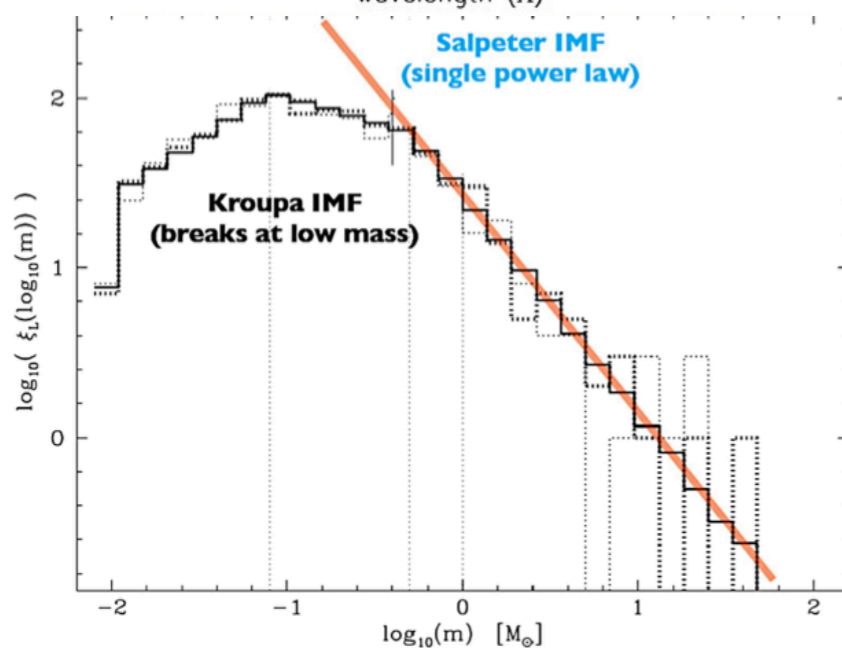
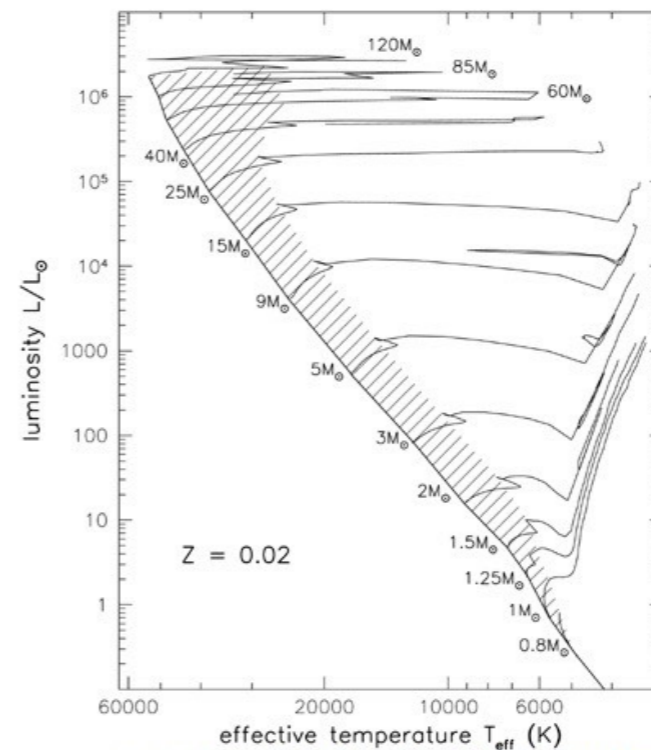
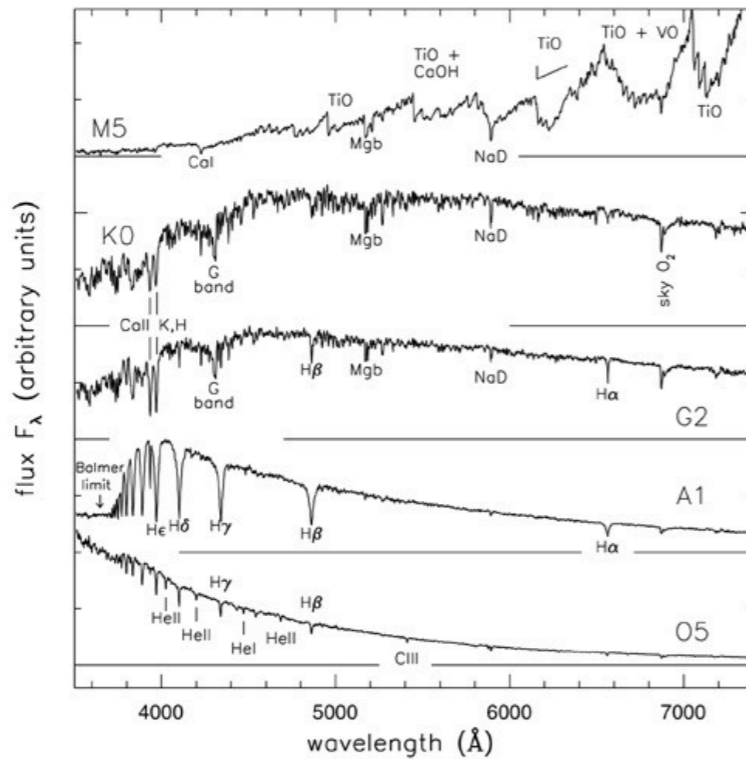
Complex Stellar Population (CSP): $\int \int l_\lambda(t, [M/H]) p(t) p([M/H]) dt d[M/H]$



Spectra of Complex Stellar Population (CSP):

$$l_{\lambda}^{\text{CSP}} = \iint l_{\lambda}^{\text{SSP}}(t, [M/H]) p(t) p([M/H]) dt d[M/H]$$

$$= \iint \left(\iint l_{\lambda}^*(L, T) p(L, T | t, [M/H], \text{IMF}, \text{SEM}) dL dT \right) p(t) p([M/H]) dt d[M/H]$$

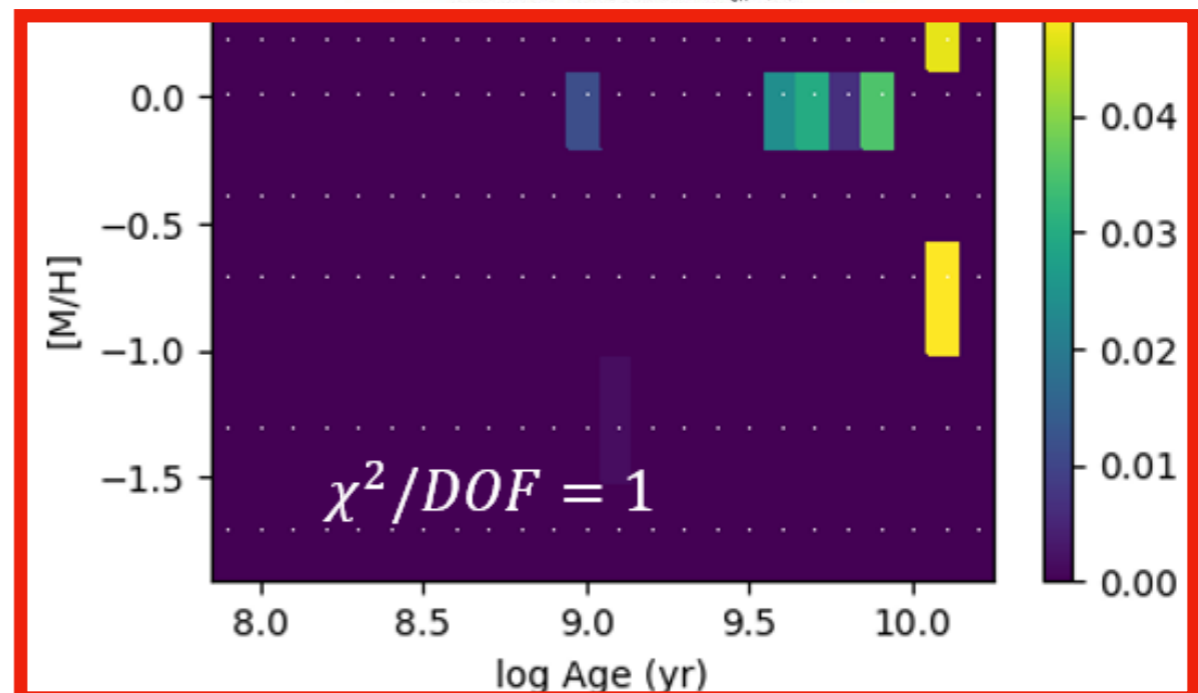
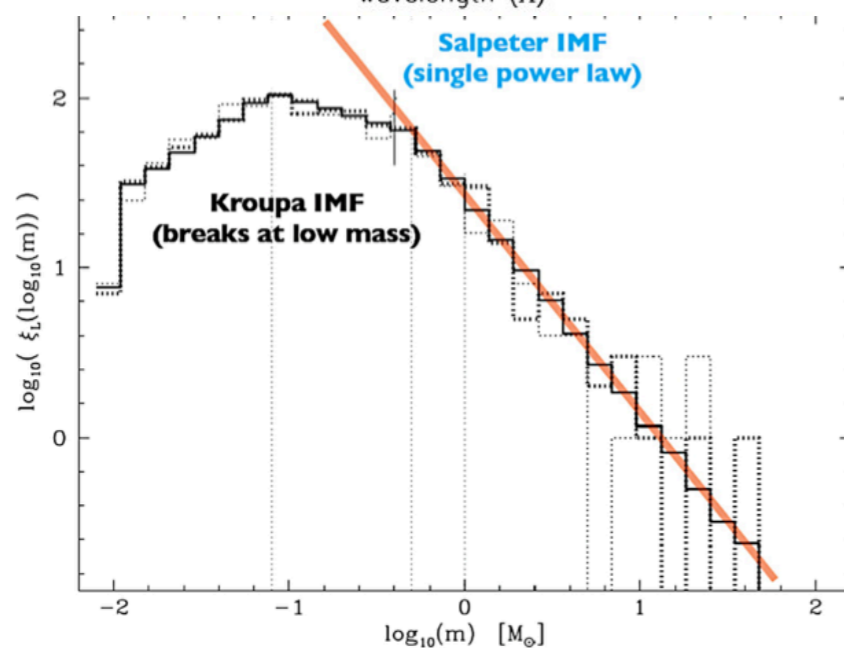
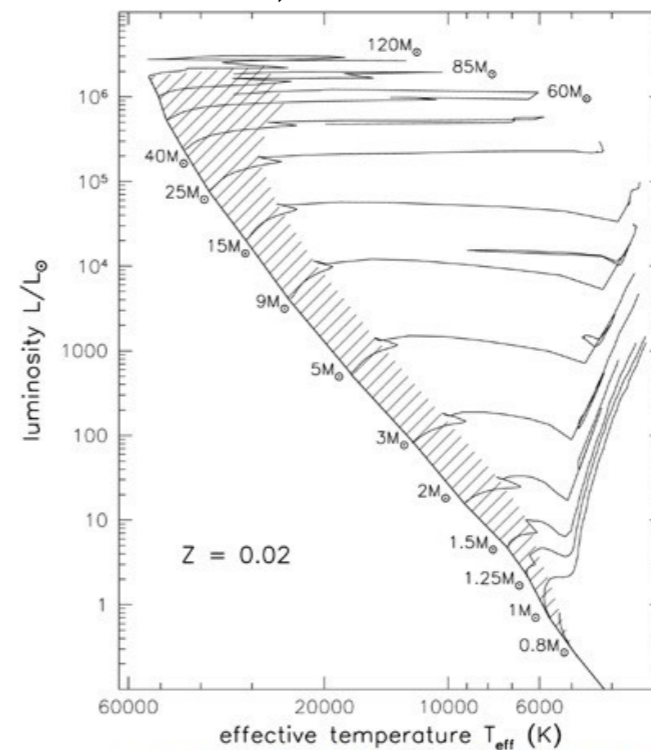
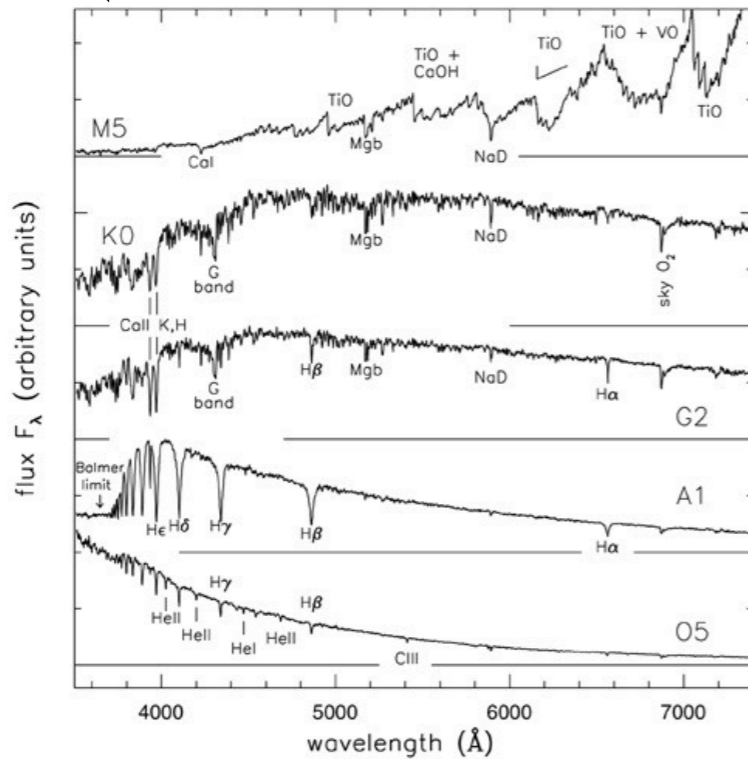


Stellar Mass from Spectral Fitting

Modeling an Observed Spectrum with Model CSP Spectra Requires Solving the Mass Weights: $M \cdot p(t) \cdot p([M/H])$

$$l_{\lambda}^{\text{csp}} = \iint l_{\lambda}^{\text{ssp}}(t, [M/H]) p(t) p([M/H]) dt d[M/H]$$

$$= \iint \left(\iint l_{\lambda}^*(L, T) p(L, T | t, [M/H], \text{IMF}, \text{SEM}) dL dT \right) p(t) p([M/H]) dt d[M/H]$$

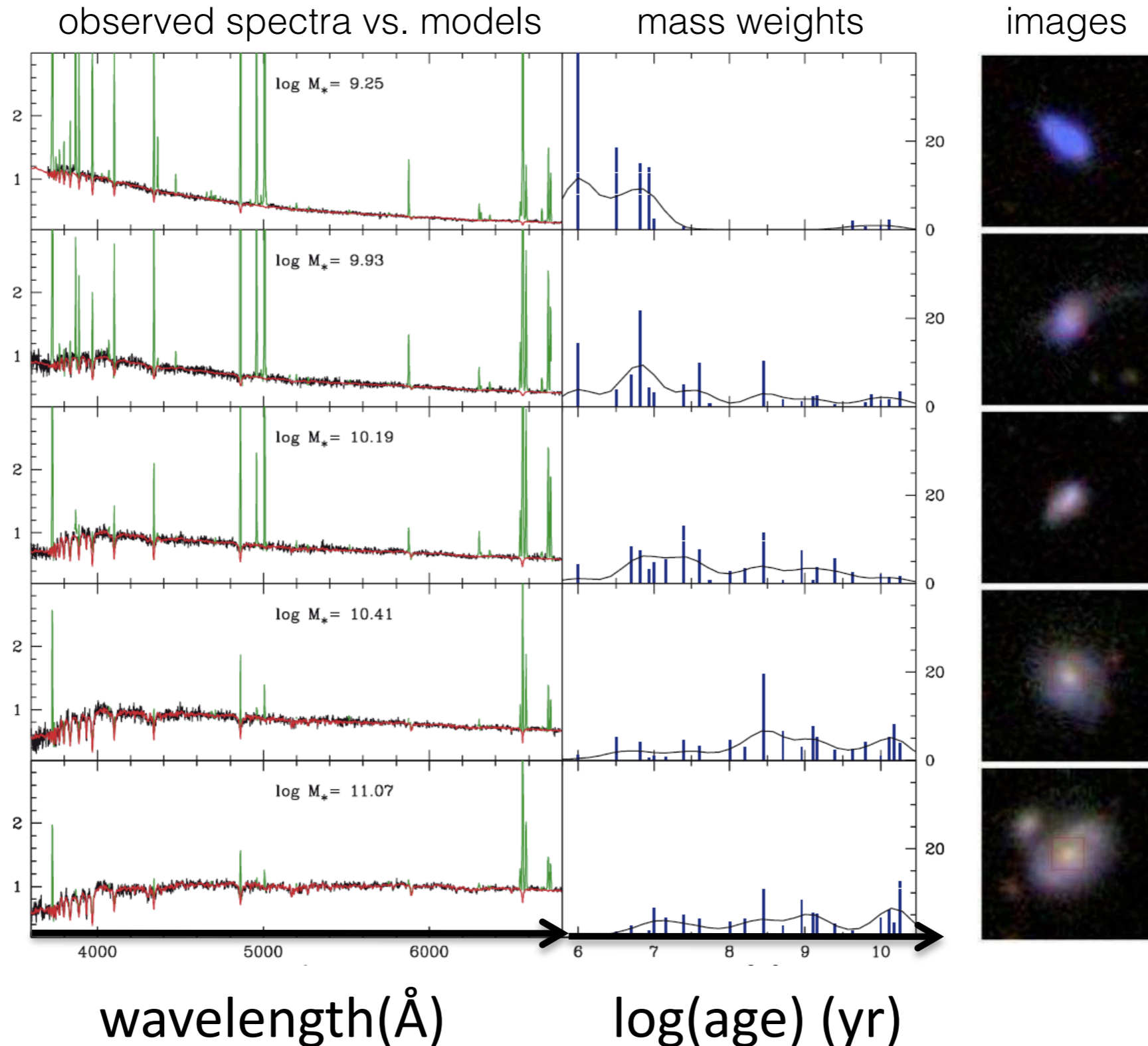


Solving for mass weights is a bounded-variables linear least squares problem (BVLS algorithm by Stark & Parker 1995)

$$\frac{M}{4\pi D_L^2} \sum l_{\lambda}^{\text{SSP}}(t, [M/H]) \times p(t, [M/H]) \approx f_{\lambda}$$

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 2 & 1 \end{bmatrix} \times \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \approx \begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix}$$

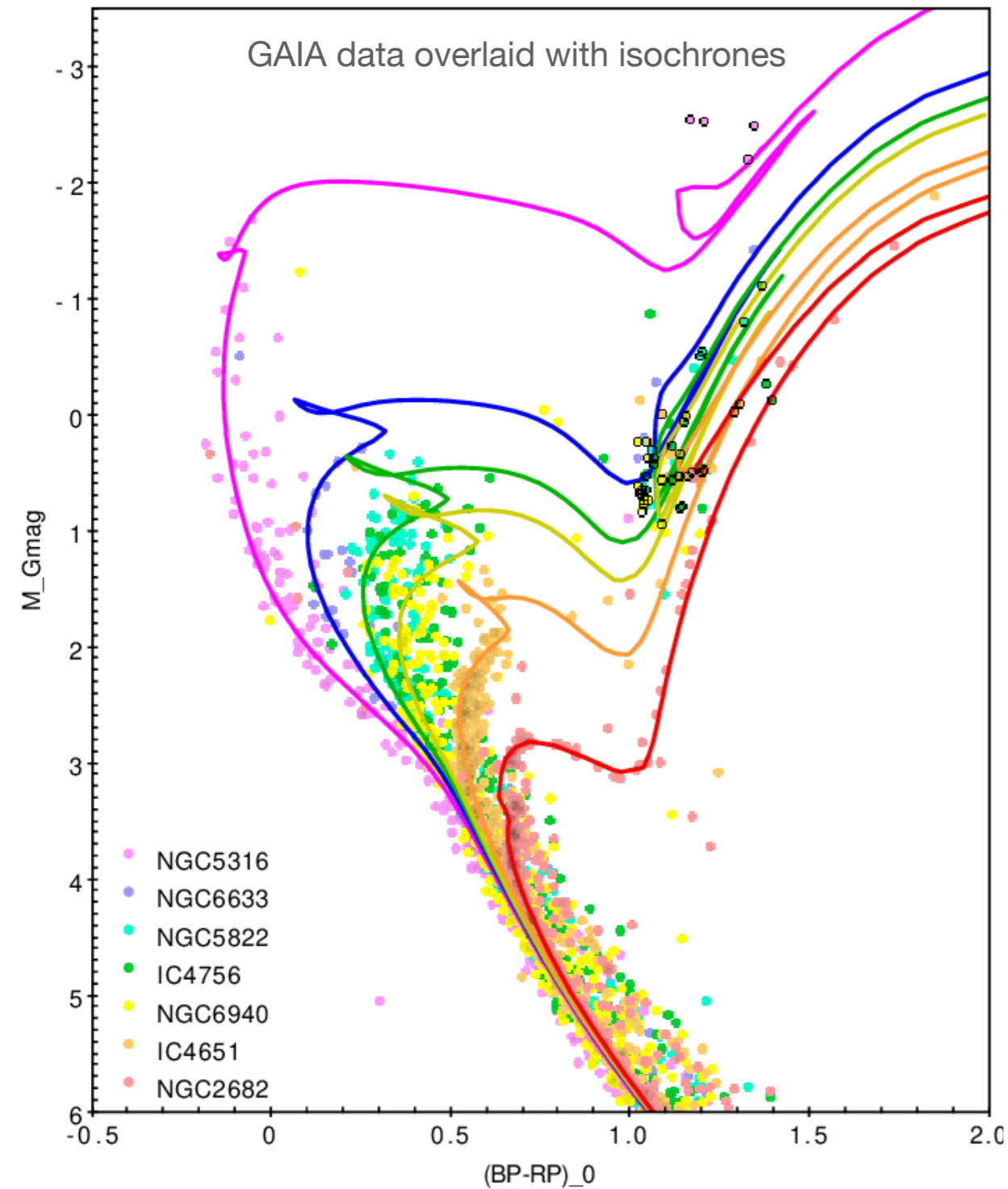
Spectroscopic masses using SPS spectral models



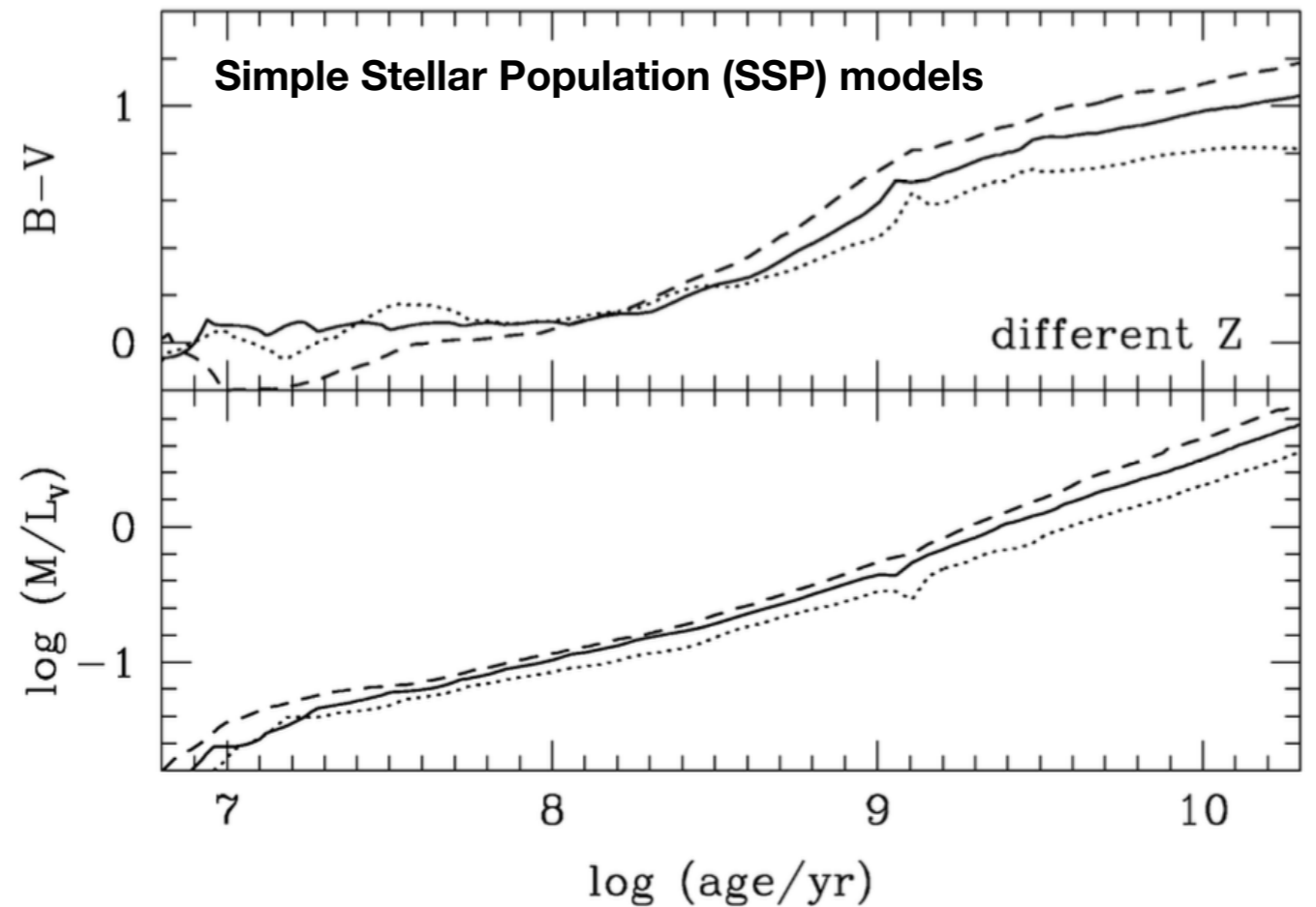
Stellar Mass from Photometry

As a stellar population ages, it becomes redder and fainter

HR diagram of clusters covering a range of ages



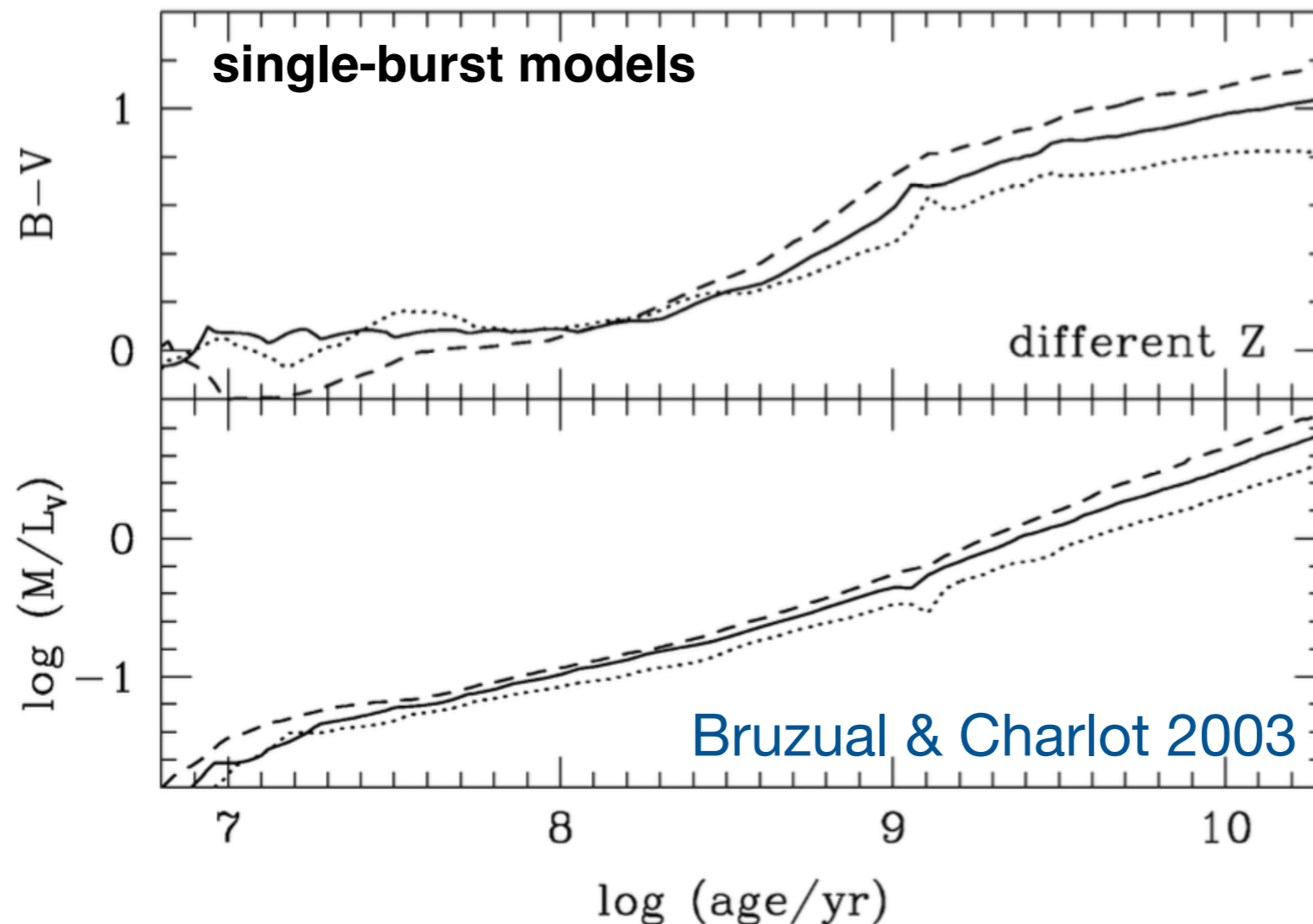
- Stellar population synthesis models follow the **isochrone evolution** of stellar populations and predict the **integrated color** and the **total luminosity** as a function of age.
- The **mass-to-light ratio (M/L)** increases because luminosity decreases faster than mass loss.



Photometric masses using mass-to-light ratio

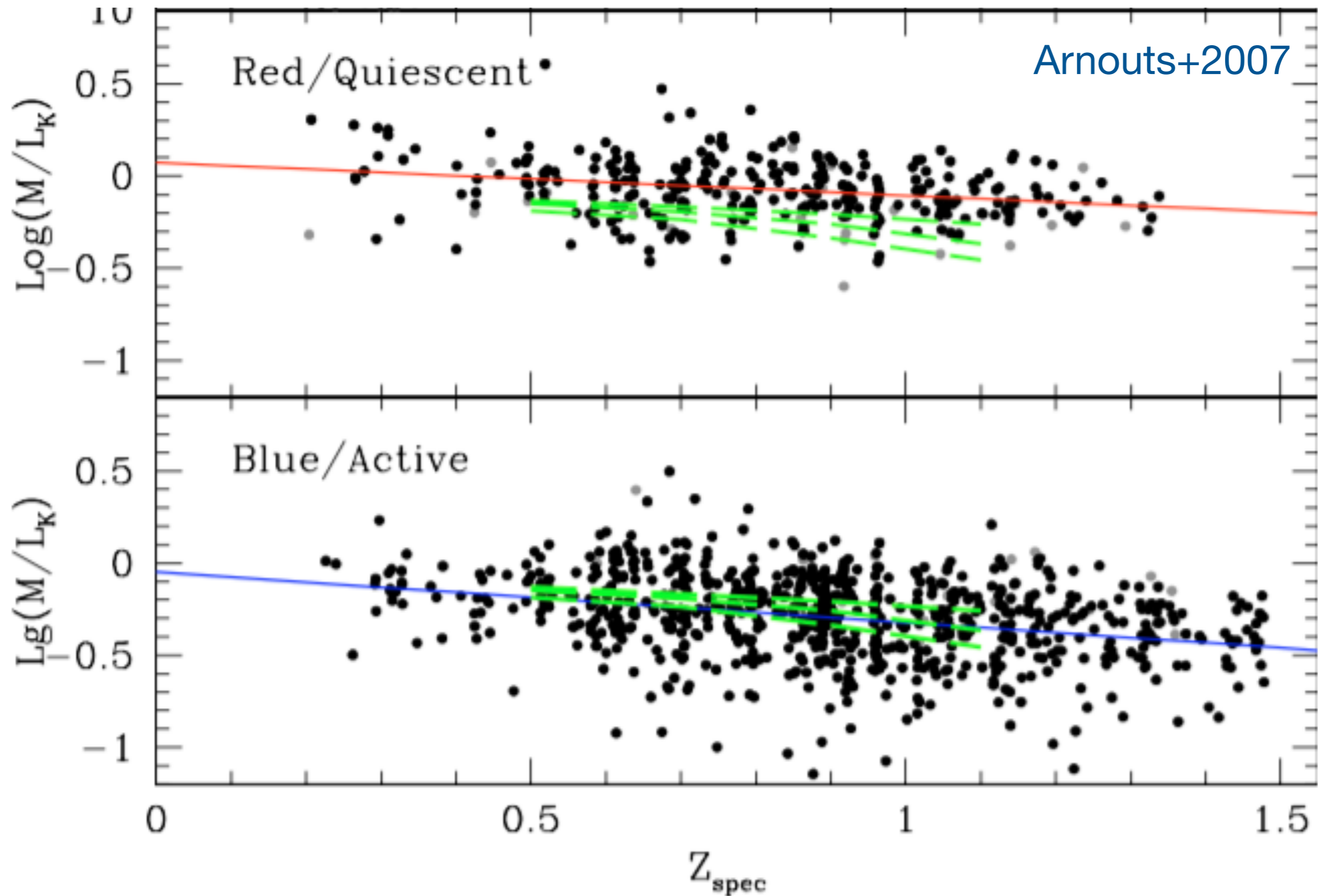
$$\begin{aligned}\log \mathcal{M} &= \log L_\lambda / L_{\lambda, \odot} + \log(\mathcal{M} / L_\lambda) \\ &= 0.4(M_{\lambda, \odot} - m_\lambda + 25 + 5 \log D_L) + \log(\mathcal{M} / L_\lambda)\end{aligned}$$

- * In practice, this approach is problematic because the mass-to-light ratio of a CSP depends on the **weights in age and metallicity**, just like the spectra of a CSP.
- * When high S/N spectra are available, one can solve for $p(t) \cdot p([M/H])$ with BVLS.
- * When only photometry is available, the weights can not be solved, so they must be **prescribed** as if known a priori. e.g., the SSP models below assume δ functions.

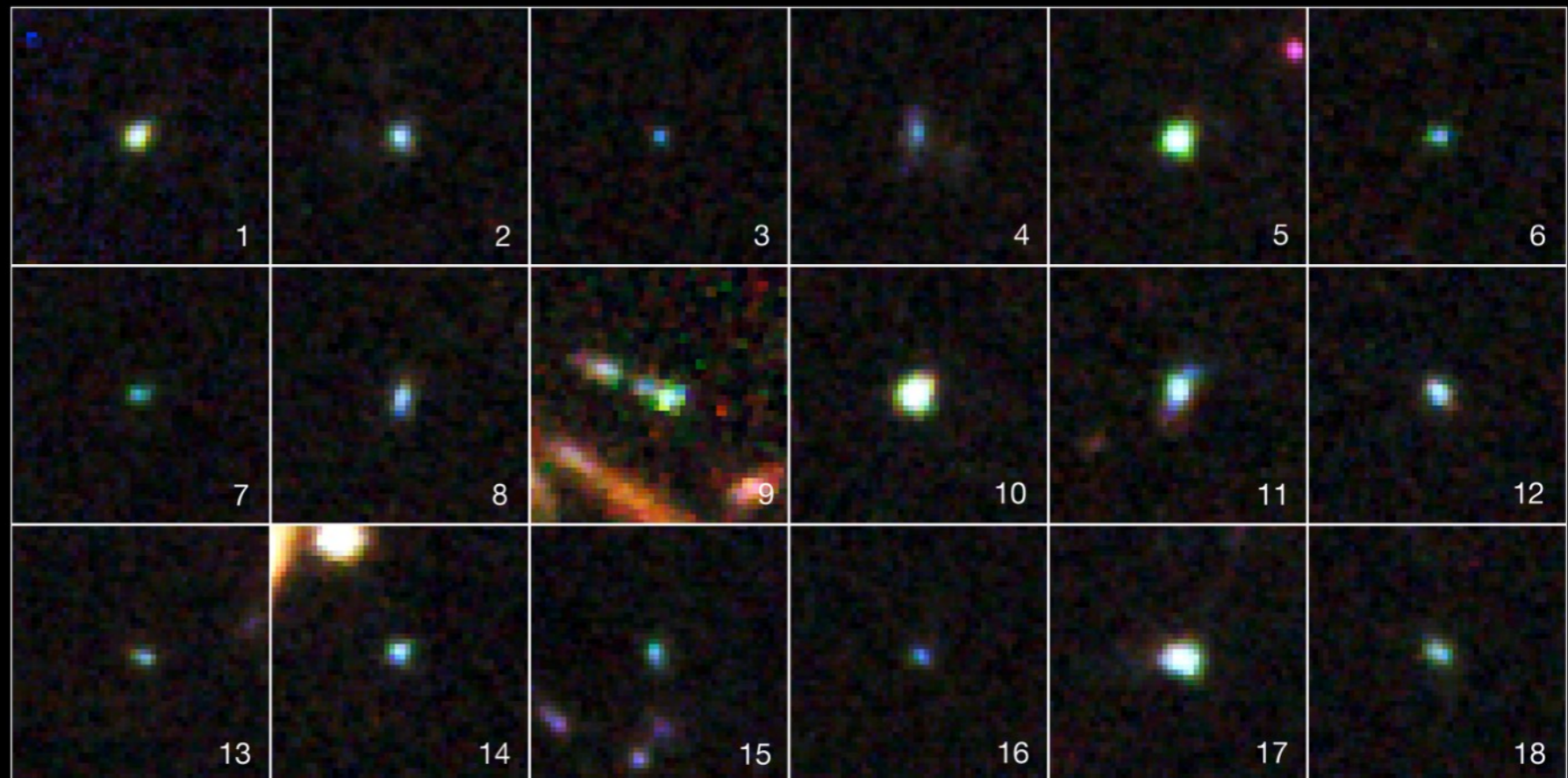
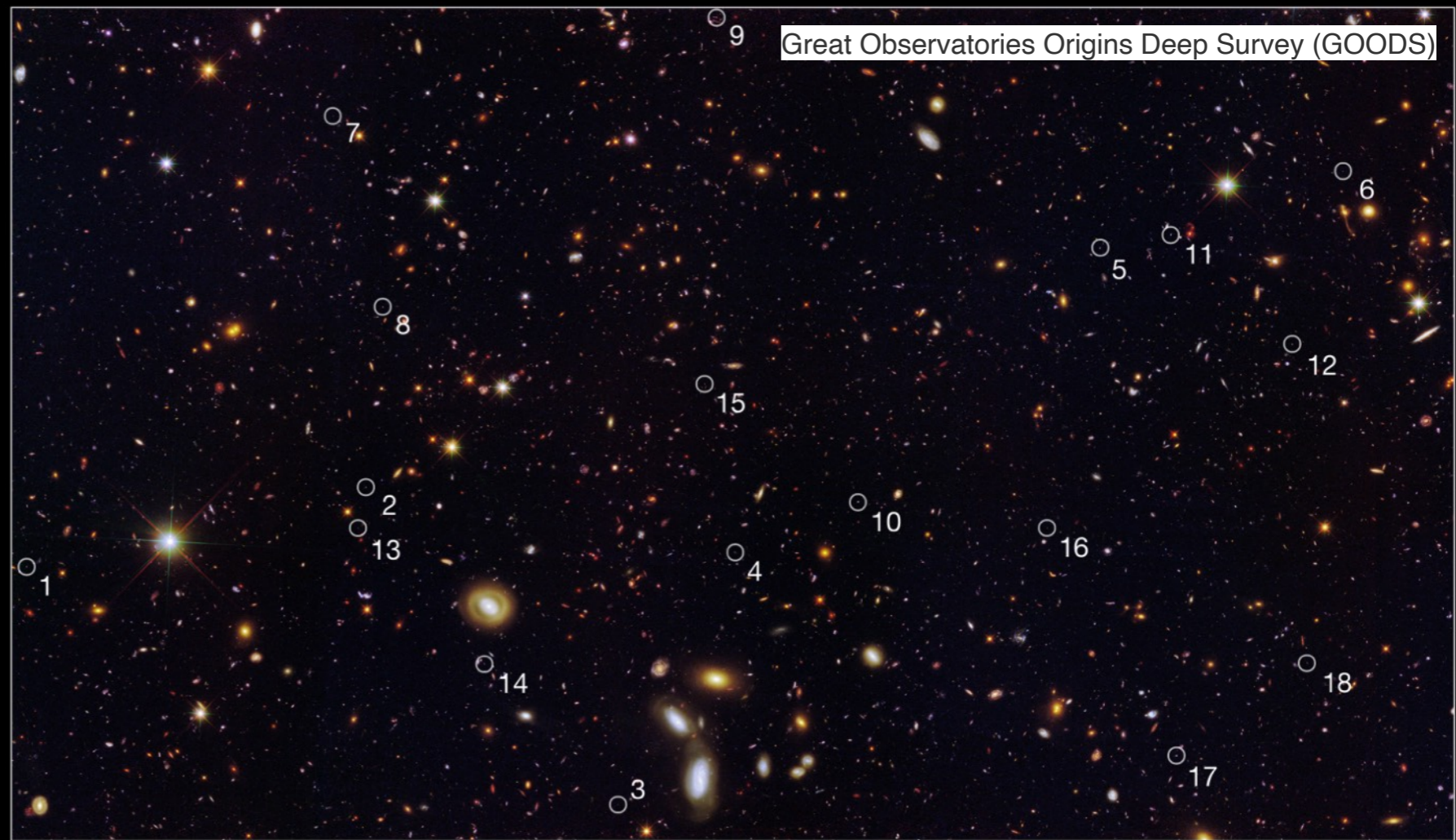


Spectral estimates of the mass-to-light ratio of quiescent and active (star-forming) galaxies

The masses are estimated from spectral fitting with CSP models, but the M/L can be applied on galaxies that have only photometry data and **photometric redshifts**



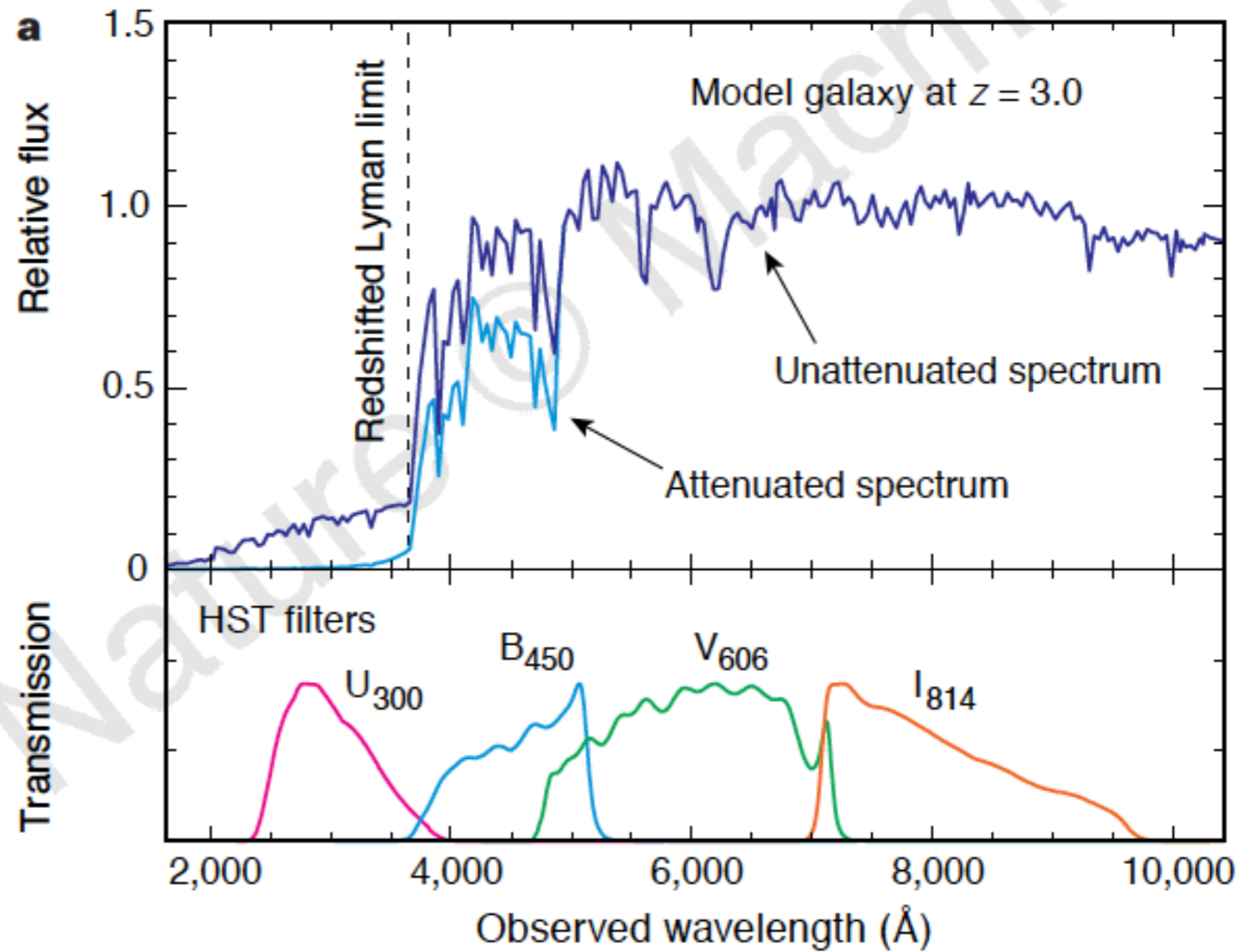
Photometric redshifts is critical, because spectroscopy of large samples of faint, distant galaxies is prohibitively expensive



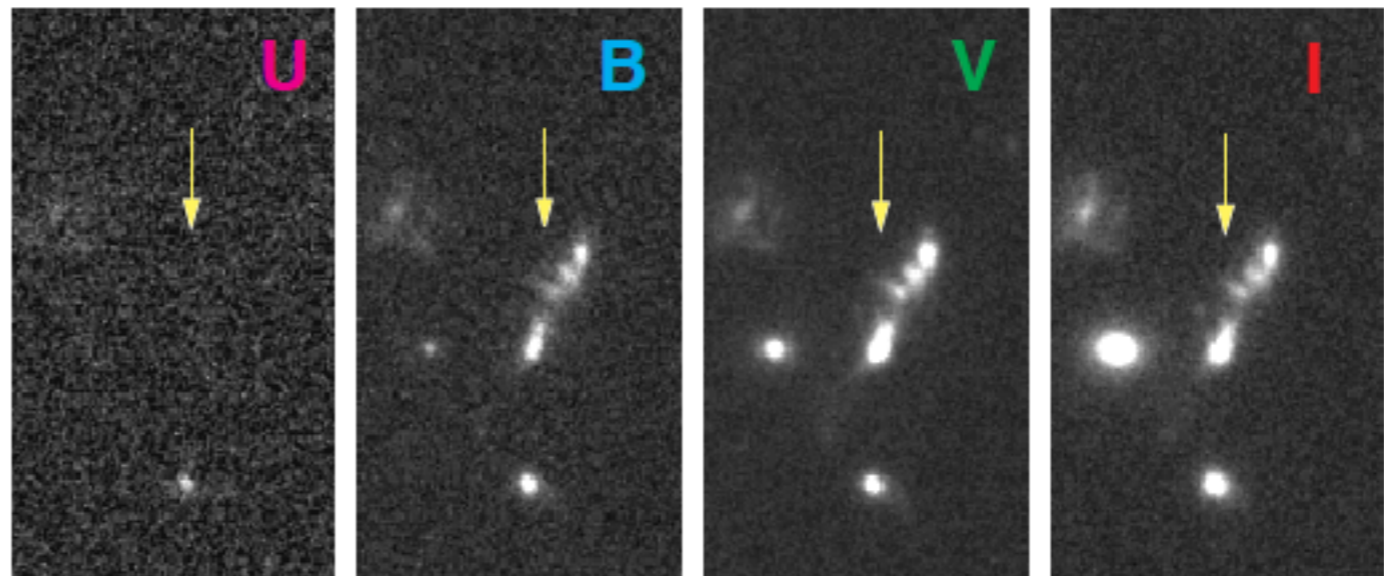
example $z=1.5$ galaxies

The Lyman Break:

Most Lyman continuum photons ($\lambda_{\text{rest}} < 912\text{\AA}$) are absorbed by either the ISM or the IGM



b



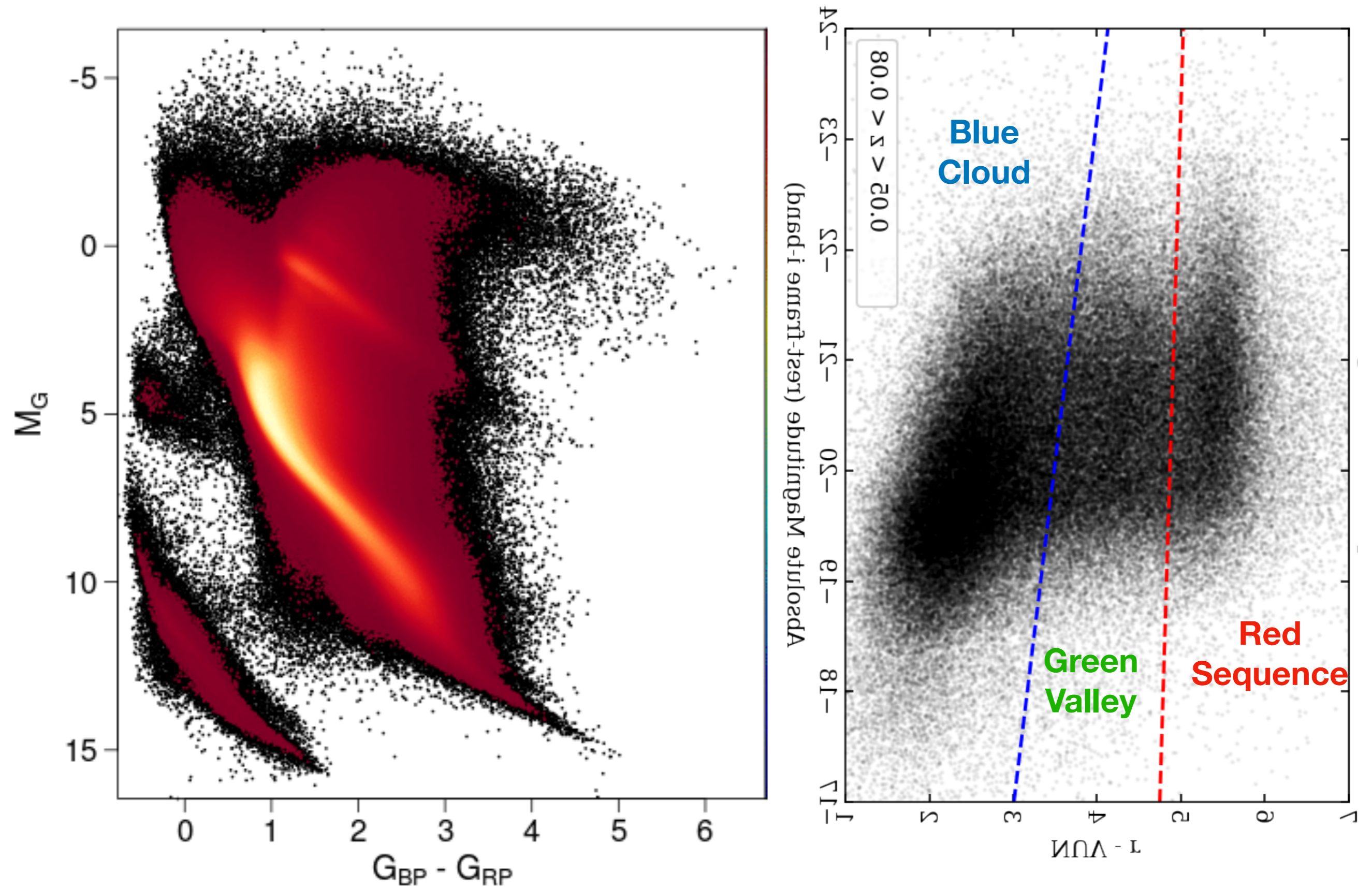
Steidel 98, 03

Ellis 98

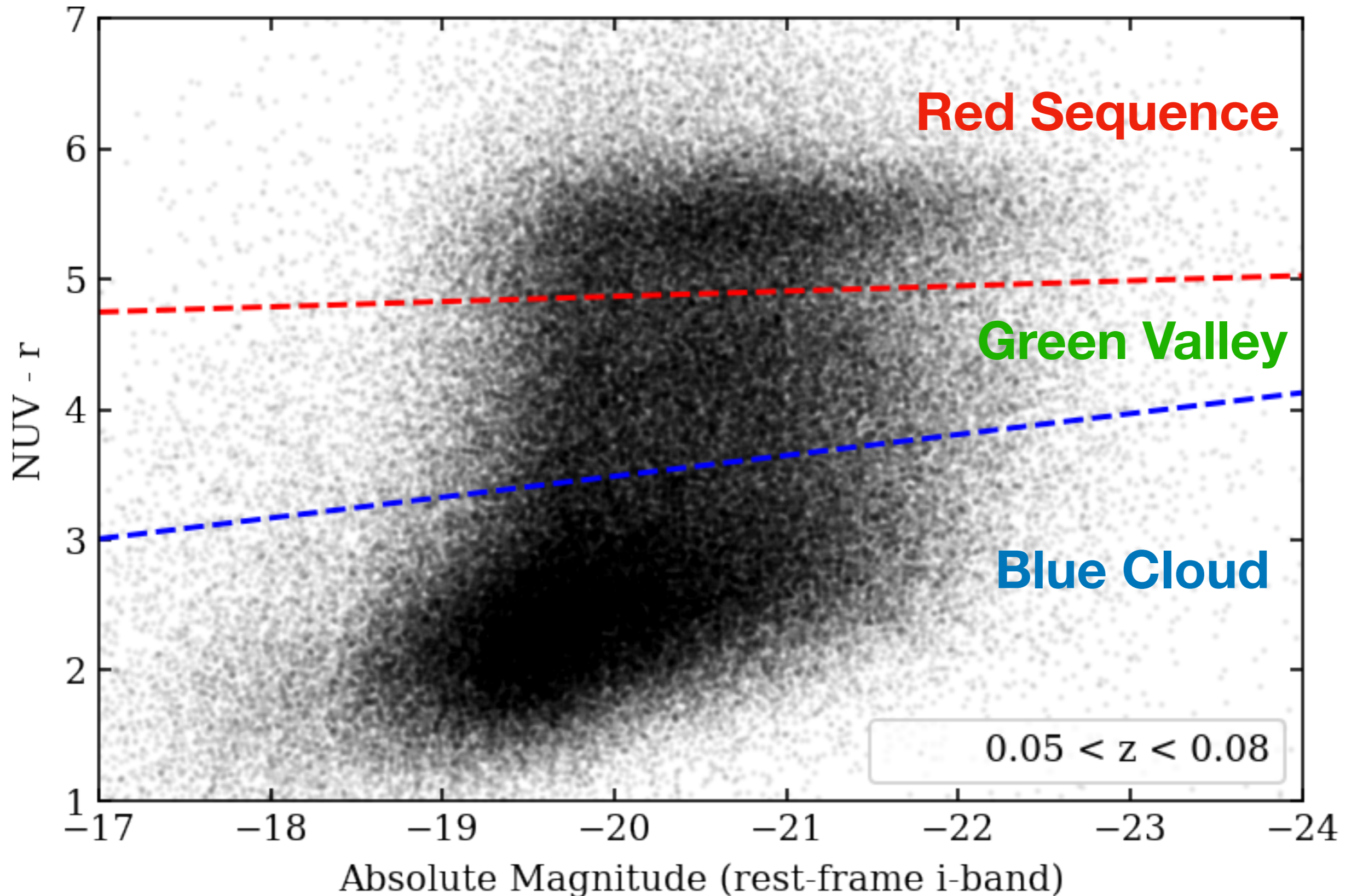
Adelberger+04

Separation of quiescent and active star-forming galaxies on the Color-Magnitude Diagram

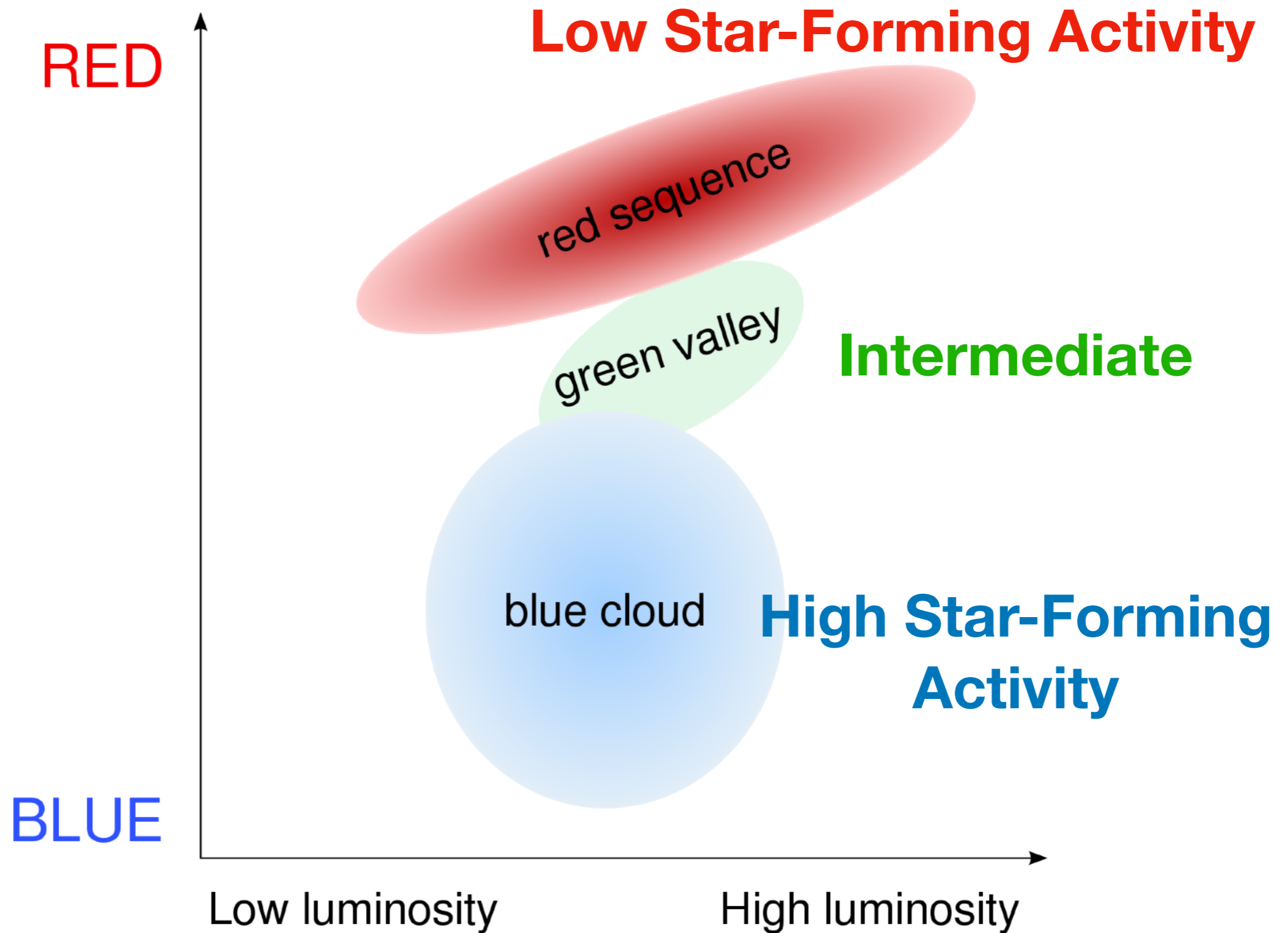
HR Diagram of Stars vs. CM Diagram of Galaxies



Color-Magnitude Diagram of Galaxies



Color-Magnitude Diagram of Galaxies

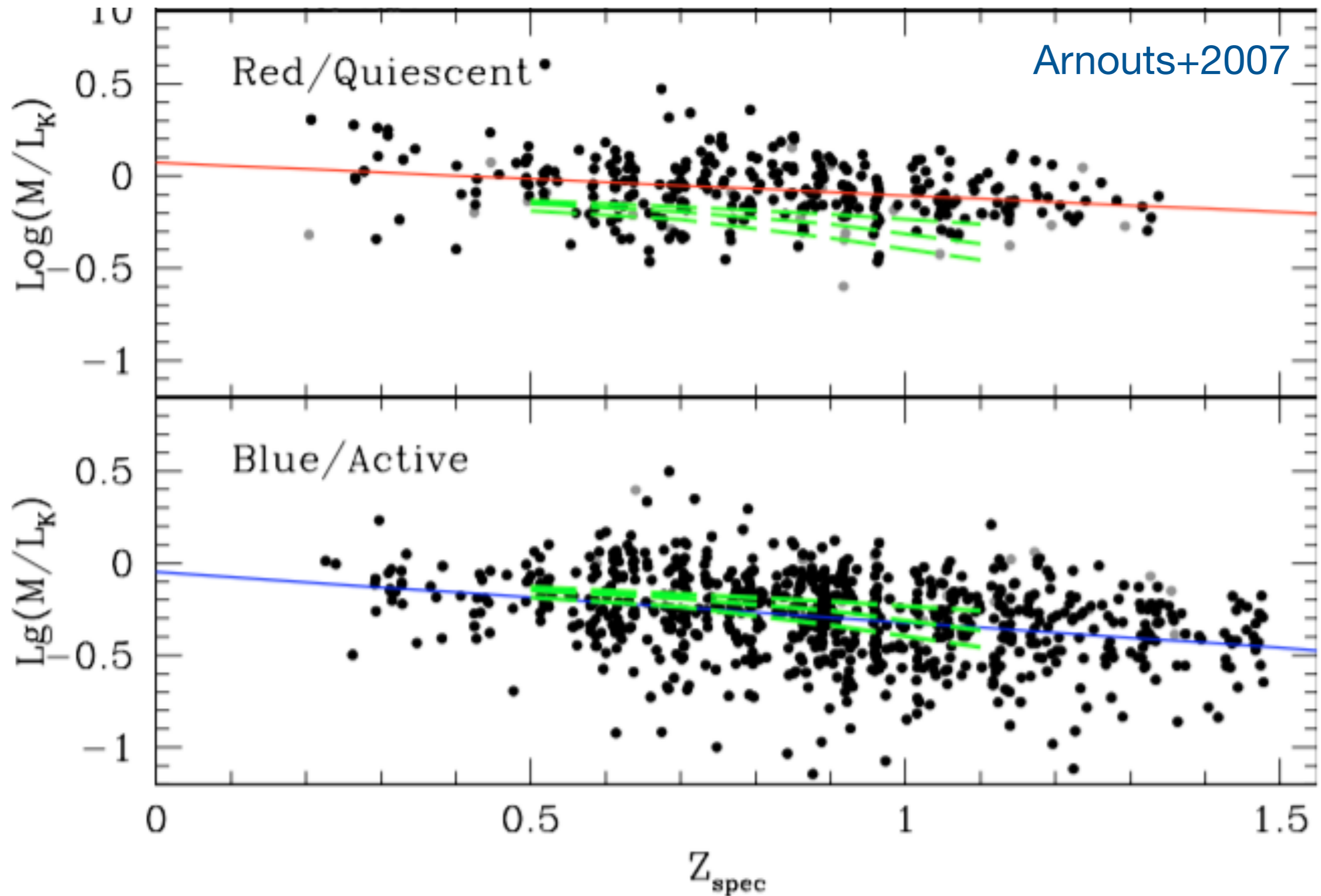


Integrated Color Naturally Separates Spirals and Ellipticals



Spectral estimates of the mass-to-light ratio of quiescent and active (star-forming) galaxies

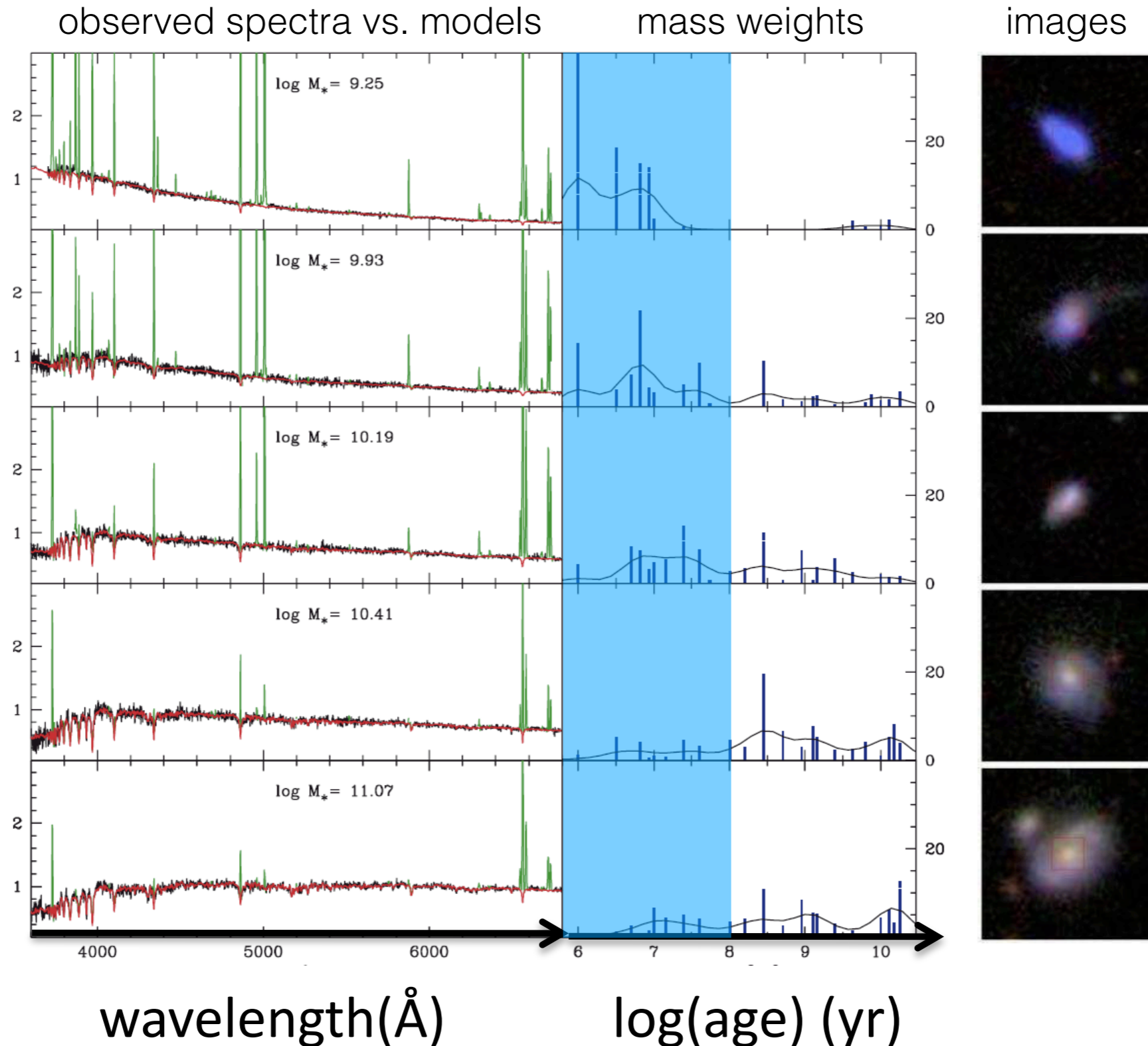
The masses are estimated from spectral fitting with CSP models, but the M/L can be applied on galaxies that have only photometry data and **photometric redshifts**



Star Formation Rates

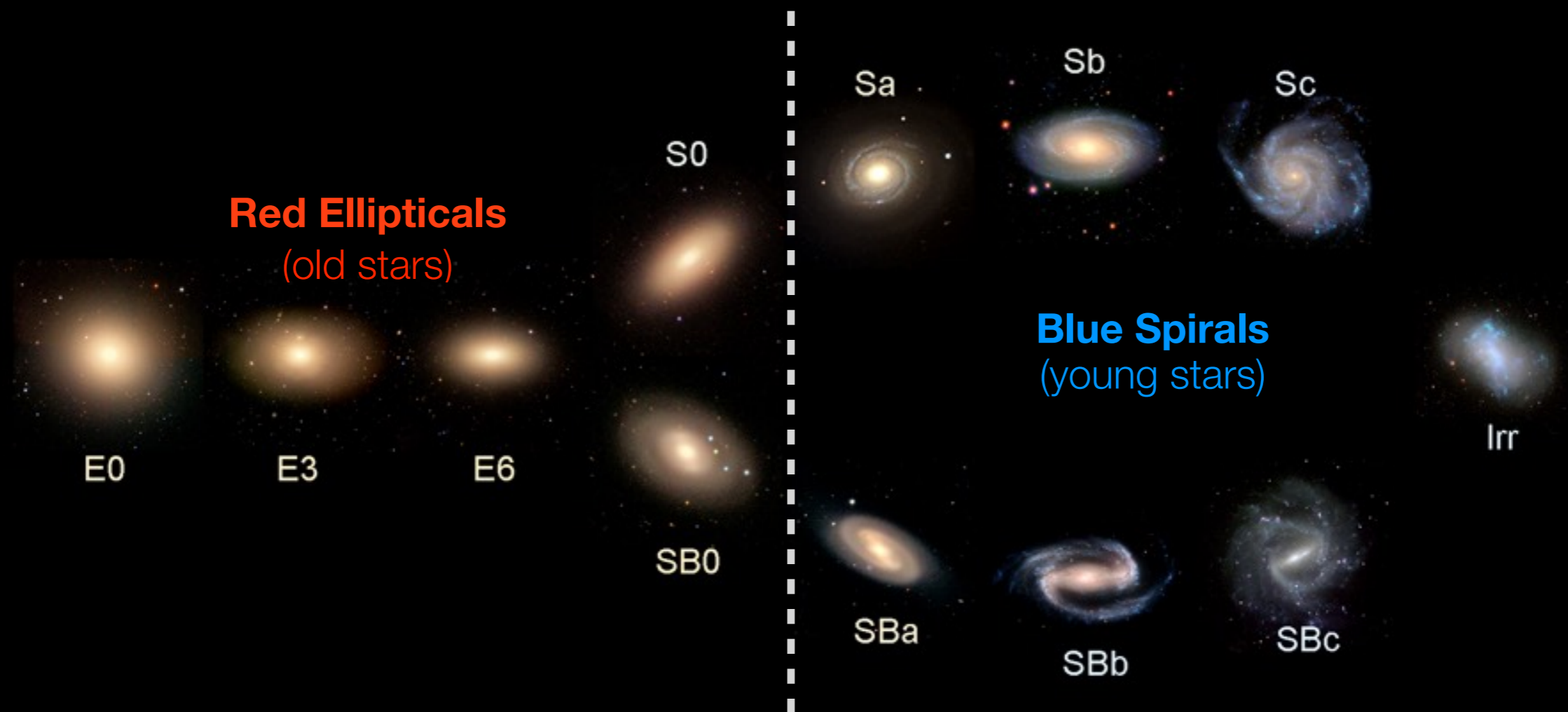
Star Formation Rate using Mass Weights from CSP Modeling:

$$\text{SFR} = \frac{M}{\tau} \int_{-3}^1 \int_0^{\tau} p(t) p([M/H]) dt d[M/H]$$



To measure SFR, we may want to focus on **blue continuum** and **emission lines**

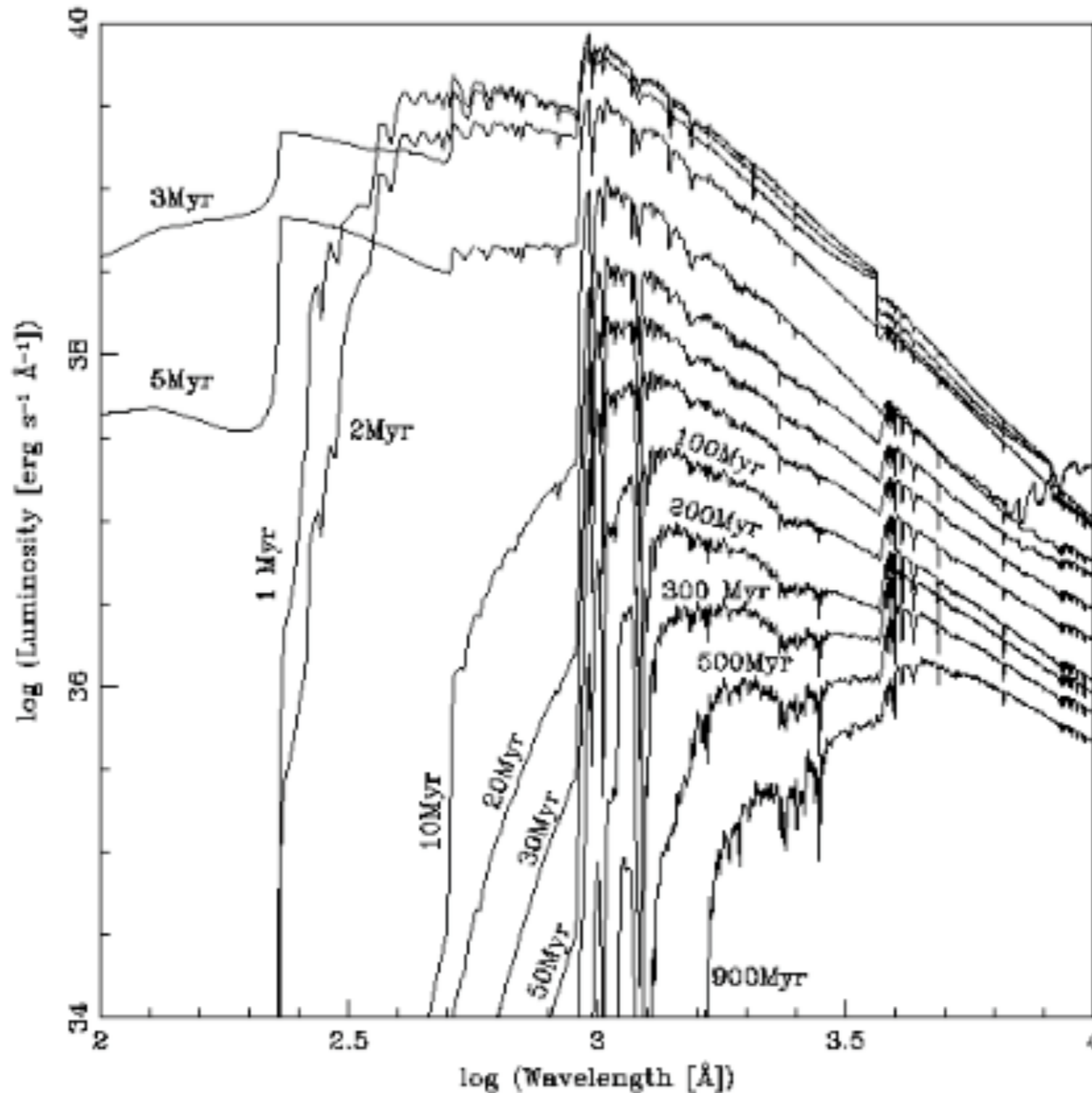
Hubble's Galaxy Classification Scheme



Nearby Galaxies

Single-Burst SFH: $b(t) = \delta(t - t_0)$

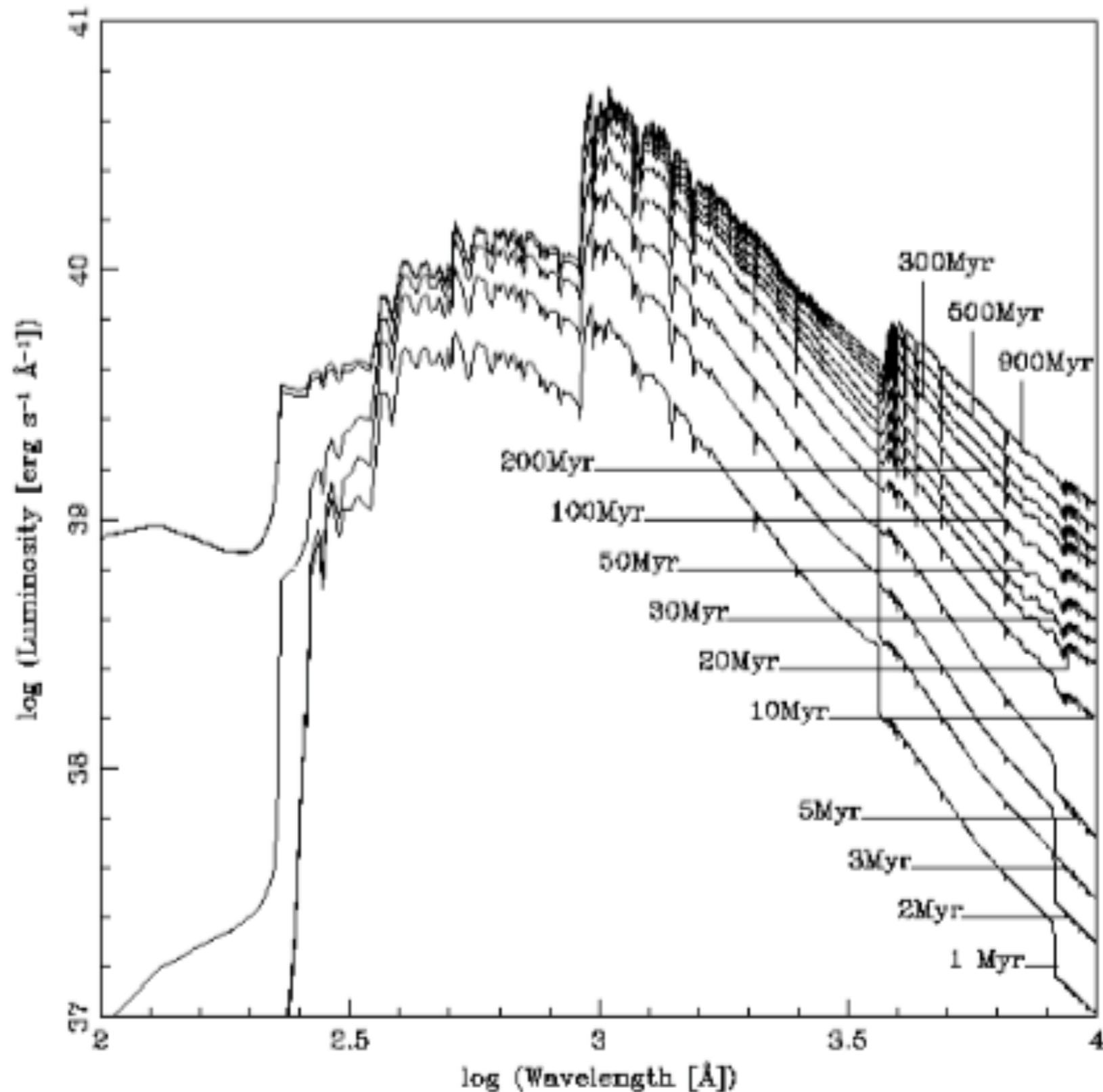
Luminosity declines as the stellar population ages



Leitherer+99:
single-burst
SF w/ ages
of 1 Myr to 1
Gyr

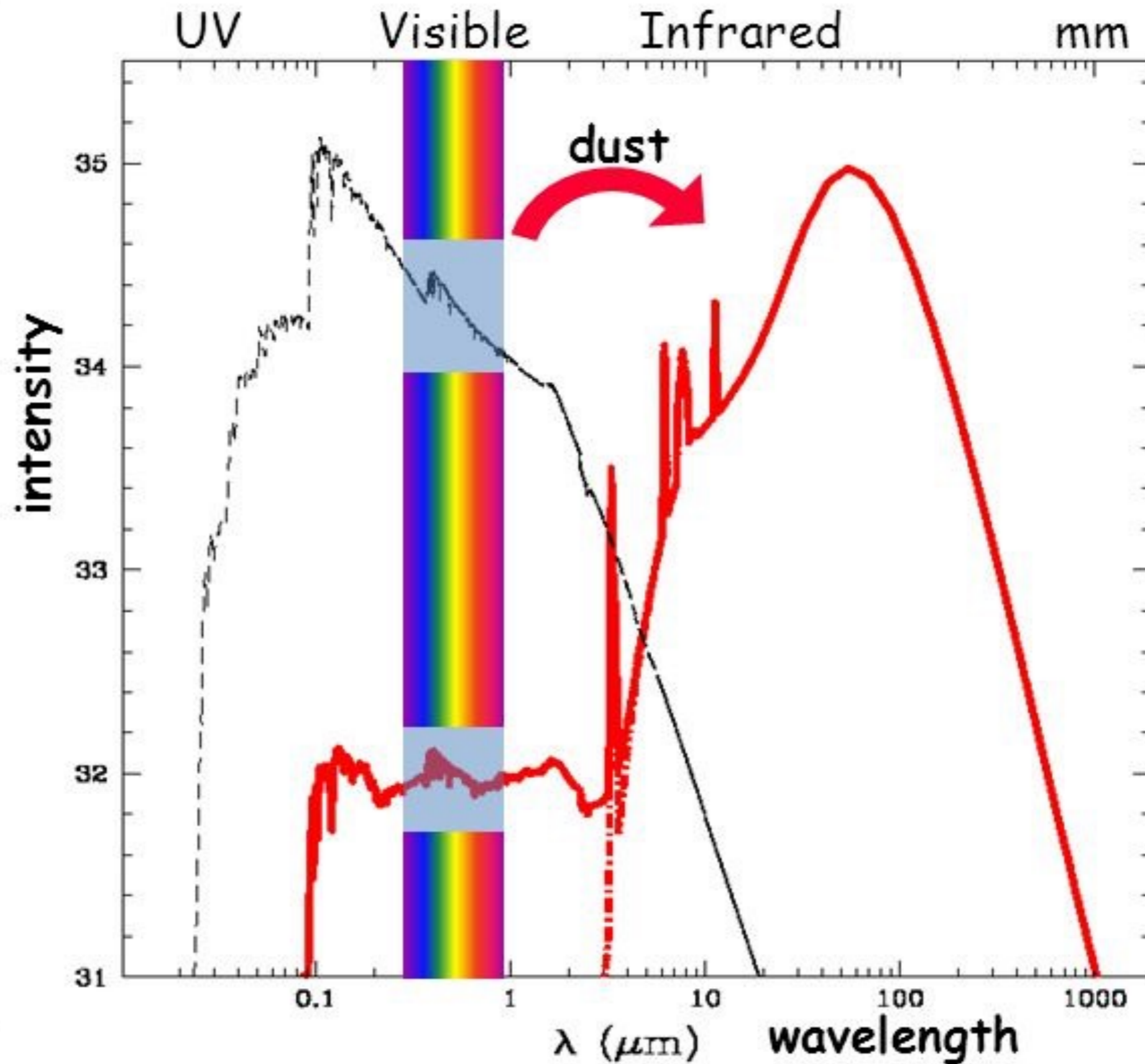
Continuous, Constant SFH: $b(t) = 1$

Once the stellar types responsible for the photon contribution to a wavelength interval have reached **equilibrium (birth rate = death rate)**, the **luminosity** at the wavelength becomes **age independent**.



Leitherer+99:
constant SF
w/ durations
of 1 Myr to
1 Gyr

Dust attenuated galaxies: use UV + IR luminosities



Commonly Used SFR estimators

Murphy+11: using the Kroupa IMF and Starburst99 SPS models

the following relation between the SFR and production rate of ionizing photons, $Q(H^0)$, at an age of ~ 100 Myr:

$$\left(\frac{\text{SFR}}{M_{\odot} \text{ yr}^{-1}} \right) = 7.29 \times 10^{-54} \left[\frac{Q(H^0)}{\text{s}^{-1}} \right]. \quad (1)$$

$$\left(\frac{\text{SFR}_{\text{H}\alpha}}{M_{\odot} \text{ yr}^{-1}} \right) = 5.37 \times 10^{-42} \left(\frac{L_{\text{H}\alpha}}{\text{erg s}^{-1}} \right). \quad (2)$$

$$\left(\frac{\text{SFR}_{\text{FUV}}}{M_{\odot} \text{ yr}^{-1}} \right) = 4.42 \times 10^{-44} \left(\frac{L_{\text{FUV}}}{\text{erg s}^{-1}} \right). \quad (3)$$

$$\left(\frac{\text{SFR}_{\text{IR}}}{M_{\odot} \text{ yr}^{-1}} \right) = 3.88 \times 10^{-44} \left(\frac{L_{\text{IR}}}{\text{erg s}^{-1}} \right). \quad (4)$$

Commonly used SFR estimators

(Murphy+11)

SPS Models

derive corresponding calibrations using Starburst99 (Leitherer et al. 1999) for a common IMF. We choose a Kroupa (Kroupa 2001) IMF, having a slope of -1.3 for stellar masses between $0.1-0.5 M_{\odot}$ and -2.3 for stellar masses ranging between 0.5 and $100 M_{\odot}$.

Luminosity of Recombination Lines

Assuming a solar metallicity and continuous star formation (i.e., a fixed SFR), Starburst99 stellar population models yield the following relation between the SFR and production rate of ionizing photons, $Q(H^0)$, at an age of ~ 100 Myr:

$$\left(\frac{\text{SFR}}{M_{\odot} \text{ yr}^{-1}} \right) = 7.29 \times 10^{-54} \left[\frac{Q(H^0)}{\text{s}^{-1}} \right]. \quad (1)$$

The ionizing photon rate can of course be expressed as an (extinction corrected) H recombination line flux, such that for Case B recombination, and assuming an electron temperature $T_e = 10^4$ K, the $H\alpha$ recombination line strength is related to the SFR by

$$\left(\frac{\text{SFR}_{H\alpha}}{M_{\odot} \text{ yr}^{-1}} \right) = 5.37 \times 10^{-42} \left(\frac{L_{H\alpha}}{\text{erg s}^{-1}} \right). \quad (2)$$

UV+IR Continuum Luminosities

The integrated UV spectrum is dominated by young stars, making it a sensitive probe of recent ($\sim 10-100$ Myr; Kennicutt 1998; Calzetti et al. 2005; Salim et al. 2007) star formation activity. We convolve the output Starburst99 spectrum with the *GALEX* FUV transmission curve to obtain the following conversion between SFR and FUV luminosity,

$$\left(\frac{\text{SFR}_{\text{FUV}}}{M_{\odot} \text{ yr}^{-1}} \right) = 4.42 \times 10^{-44} \left(\frac{L_{\text{FUV}}}{\text{erg s}^{-1}} \right). \quad (3)$$

To derive a calibration for the total infrared (IR; $8-1000 \mu\text{m}$), we make the assumption that the entire Balmer continuum is absorbed and re-radiated by dust and that the dust emission is optically thin. Integrating the output Starburst99 spectrum over this wavelength range (i.e., $912 \text{ \AA} < \lambda < 3646 \text{ \AA}$) results in the following (predicted) relation between the IR emission and current SFR:

$$\left(\frac{\text{SFR}_{\text{IR}}}{M_{\odot} \text{ yr}^{-1}} \right) = 3.88 \times 10^{-44} \left(\frac{L_{\text{IR}}}{\text{erg s}^{-1}} \right). \quad (4)$$

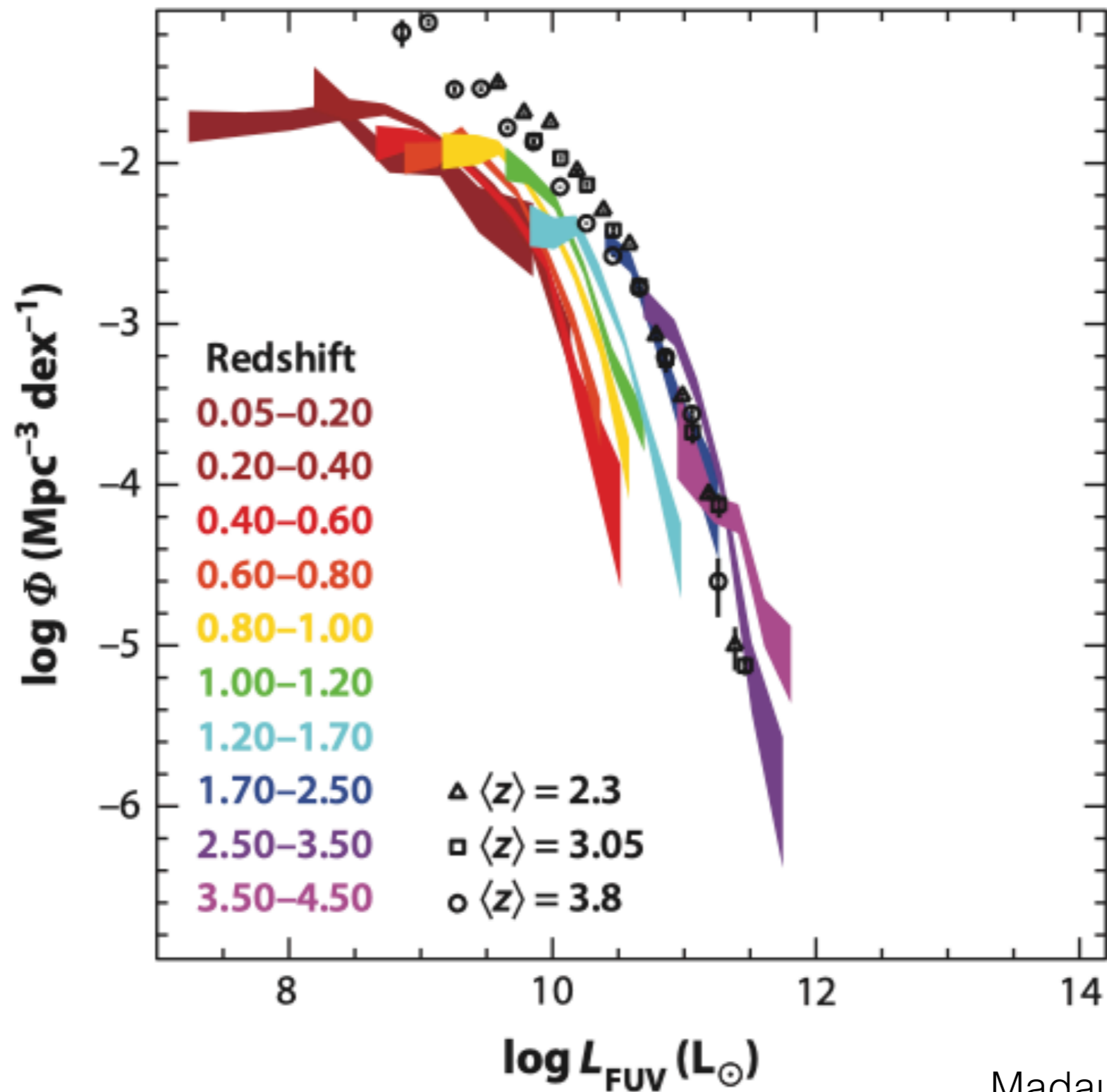
$$\text{SFR}_{\text{tot}} = \text{SFR}_{\text{FUV}} + \text{SFR}_{\text{IR}}. \quad (8)$$

Using the above calibrations, this relation can be expressed as a linear combination of the UV and total IR emission such that

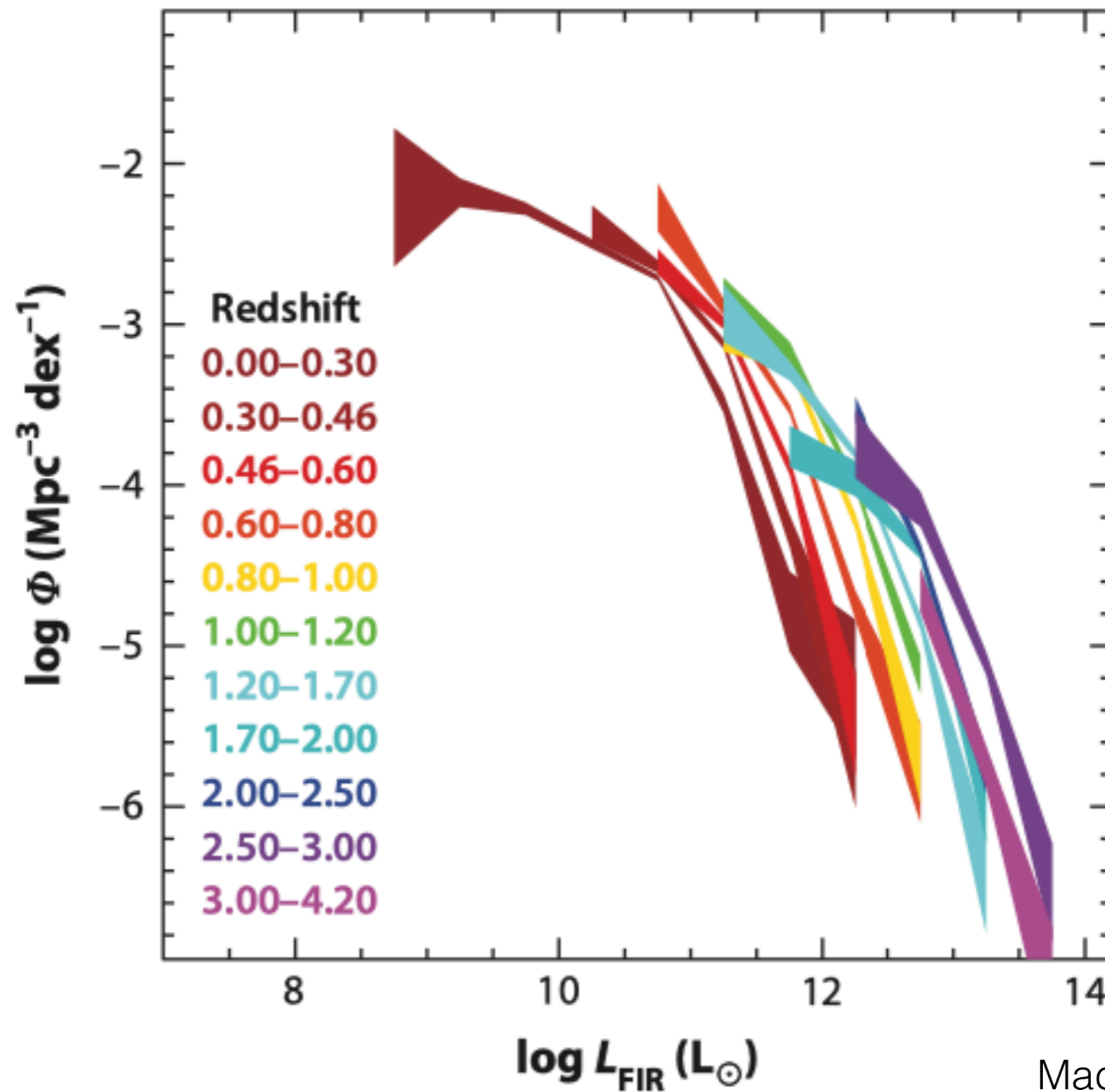
$$\left(\frac{\text{SFR}_{\text{tot}}}{M_{\odot} \text{ yr}^{-1}} \right) = 4.42 \times 10^{-44} \left(\frac{L_{\text{FUV}} + 0.88 L_{\text{IR}}}{\text{erg s}^{-1}} \right). \quad (9)$$

UV and IR Luminosity Functions and Cosmic Star Formation History

Evolution of UV Luminosity Function



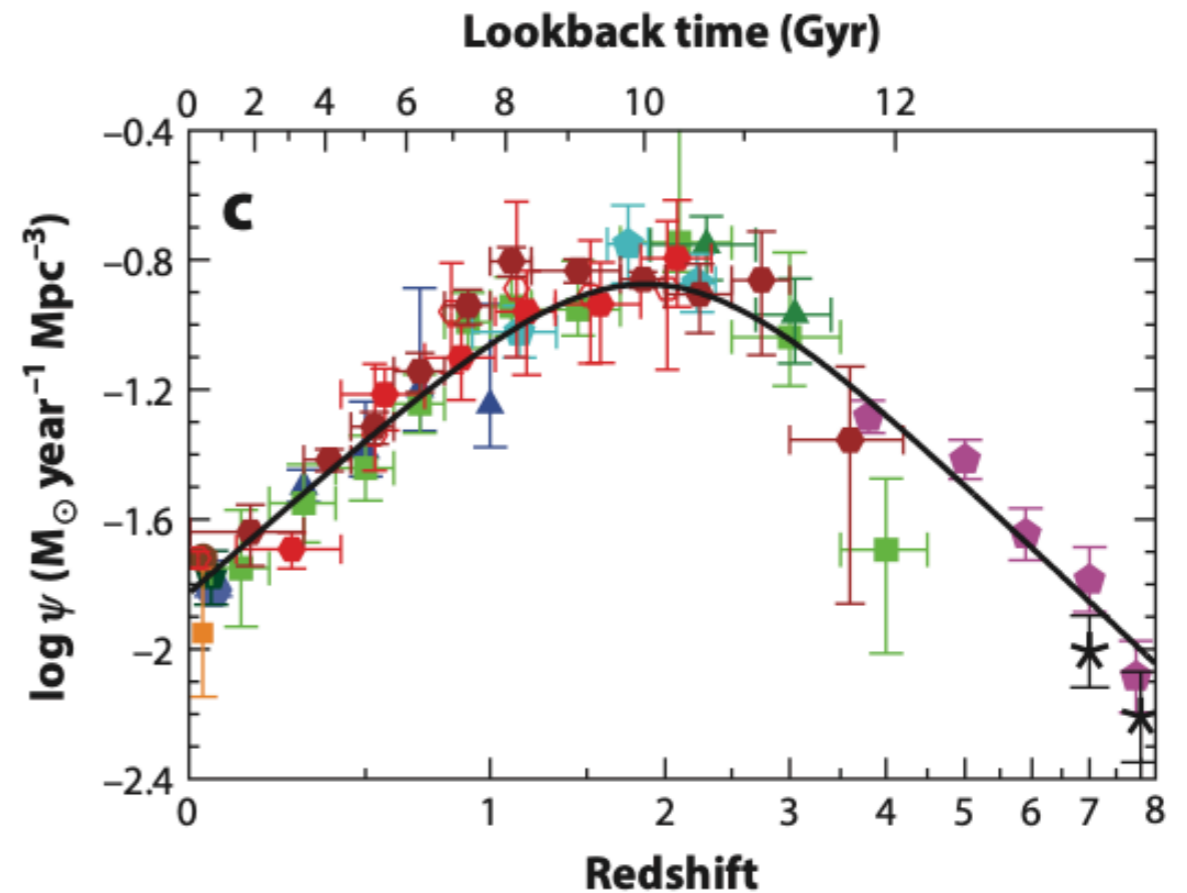
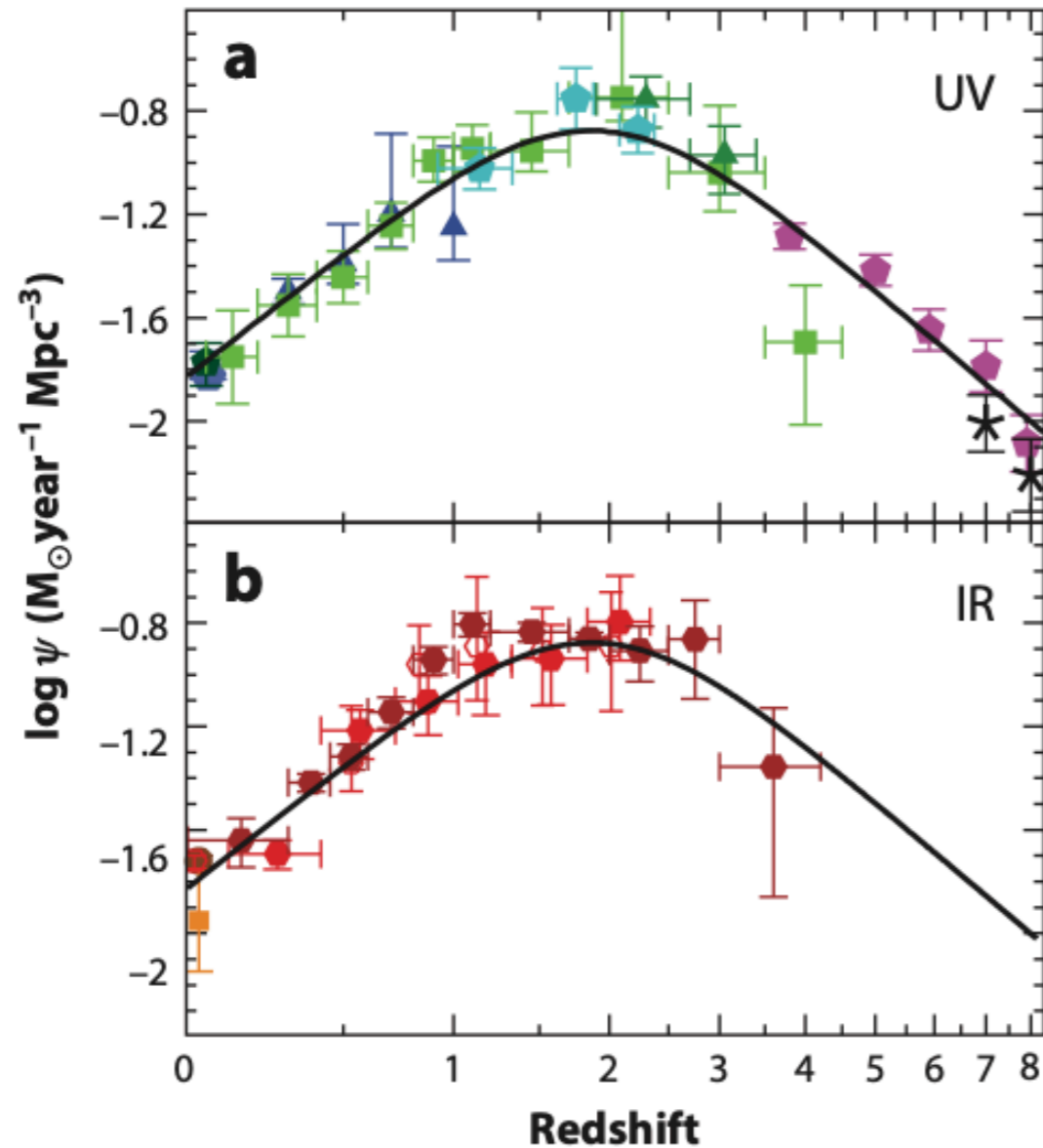
Evolution of Far-IR Luminosity Function



Integrated UV+FIR LFs -> Cosmic SF History

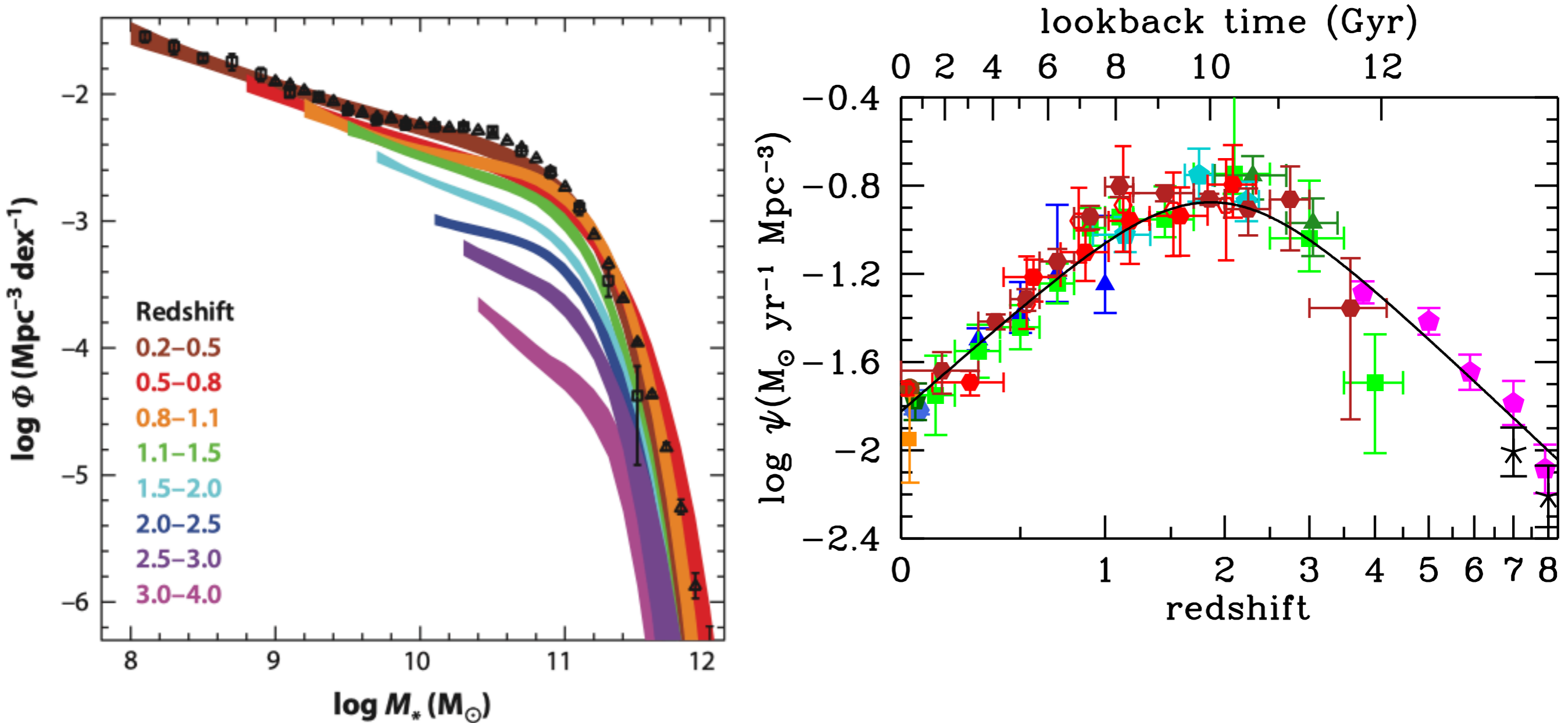
$$\psi(z) = 0.015 \frac{(1+z)^{2.7}}{1 + [(1+z)/2.9]^{5.6}} M_{\odot} \text{ year}^{-1} \text{ Mpc}^{-3}. \quad (15)$$

solid line is a fit to the data points

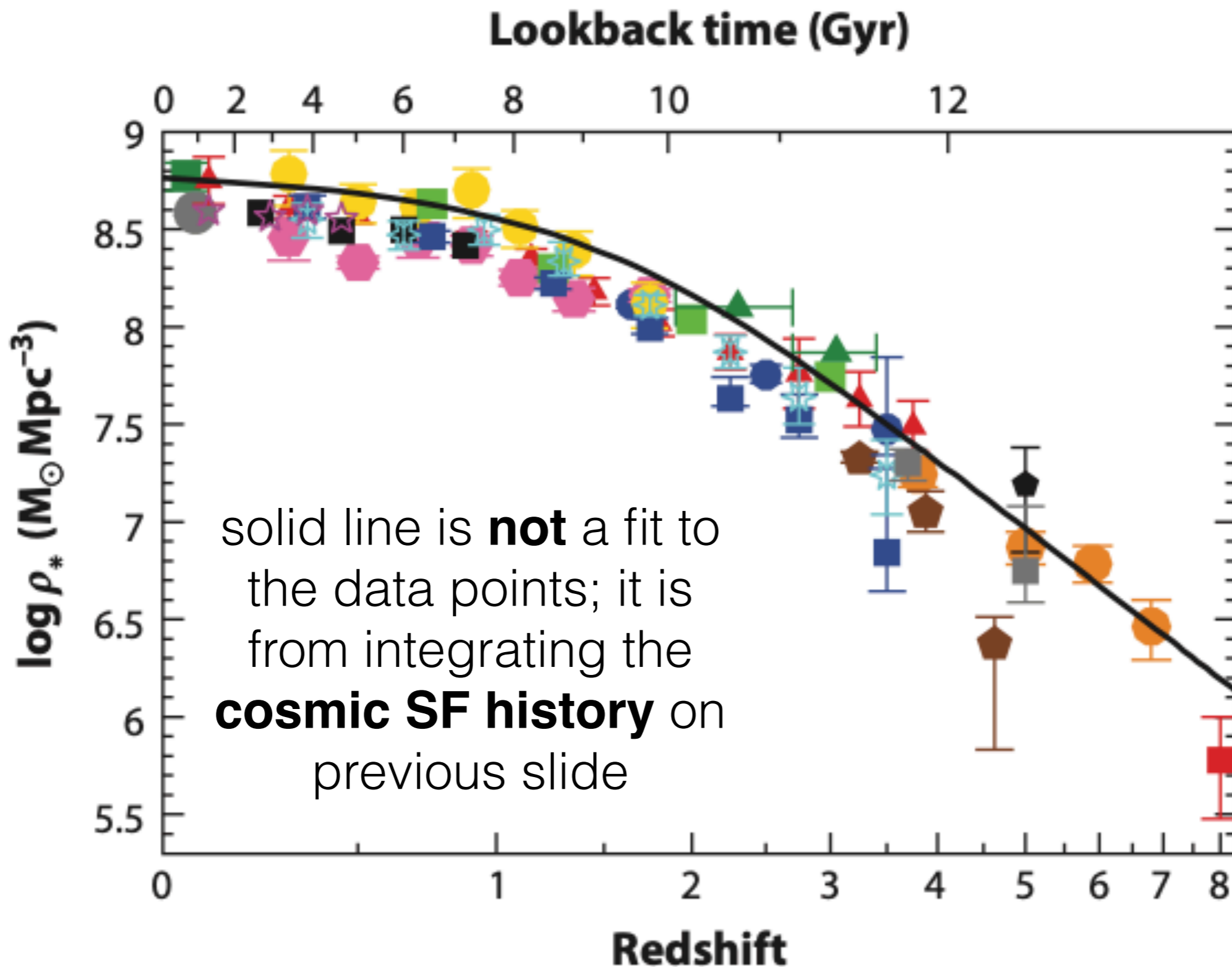


Sanity Check:

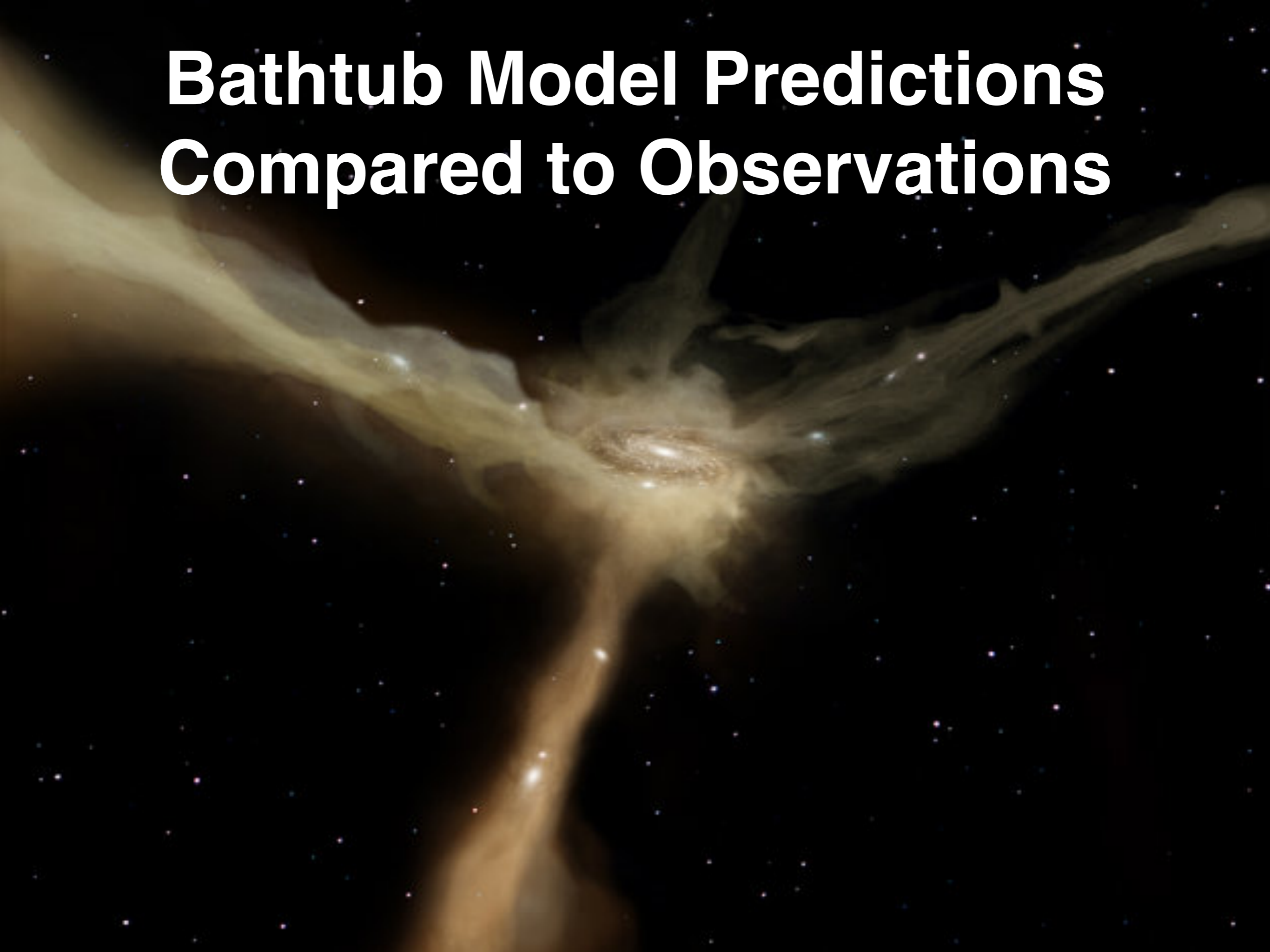
are stellar mass functions consistent with cosmic SF history?



Integrated MF vs. Integrated SFH



Bathtub Model Predictions Compared to Observations



The "Bathtub" Model: Accretion-Driven Star Formation

a continuity equation coupled with
a halo growth history and a star formation law

Change in Cold Gas Reservoir \propto **Accretion Rate** \propto **Halo Growth Rate**

Gas Consumption Rate \propto **Star Formation Rate**

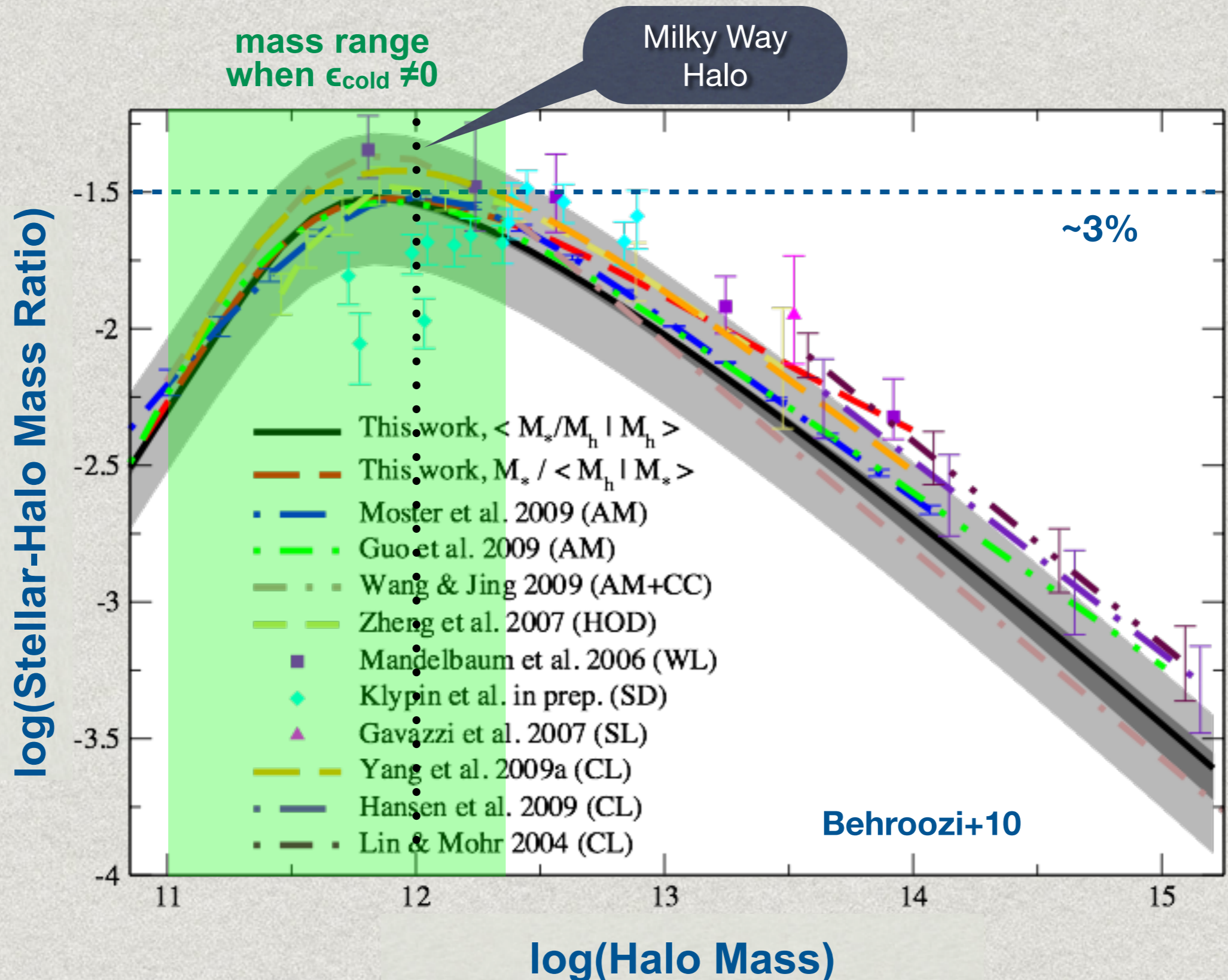
$$\left\{ \begin{array}{l} \frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \frac{dM_{\text{star}}}{dt} \\ \frac{dM_{\text{halo}}}{dt} \propto M_{\text{halo}}^{1.1} (1+z)^{2.2} \quad \leftarrow \text{Halo Growth Rate from EPS} \\ \frac{dM_{\text{star}}}{dt} = \text{SFR} = \epsilon_{\text{SF}} \frac{M_{\text{gas}}}{\tau_{\text{dyn}}} \quad \leftarrow \text{Kennicutt-Schmidt Relation} \end{array} \right.$$

cold gas accretion efficiency:

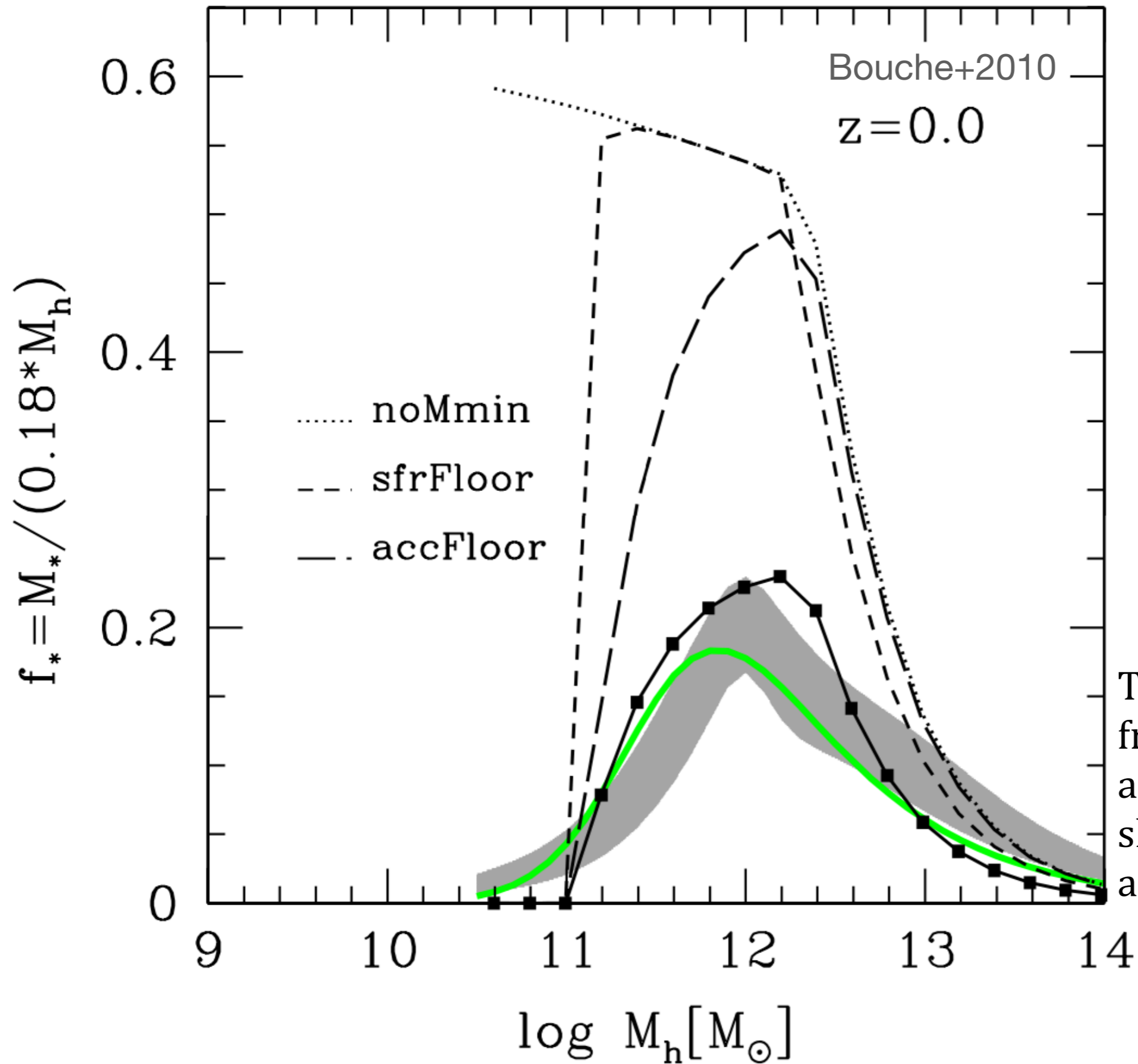
recycle & feedback:

$$\left\{ \begin{array}{l} \epsilon_{\text{cold}} = 0.0 \text{ if } M_{\text{halo}} < 10^{11} M_{\odot} \\ \epsilon_{\text{cold}} = 0.7 \text{ if } 10^{11} < M_{\text{halo}} < 10^{12.3} M_{\odot} \\ \epsilon_{\text{cold}} = 0.0 \text{ if } M_{\text{halo}} > 10^{12.3} M_{\odot} \end{array} \right. \quad \left\{ \begin{array}{l} f_{\text{recycle}} = 0.5 \\ f_{\text{outflow}} = 0.6 \end{array} \right.$$

Observed Stellar Mass Fraction Today

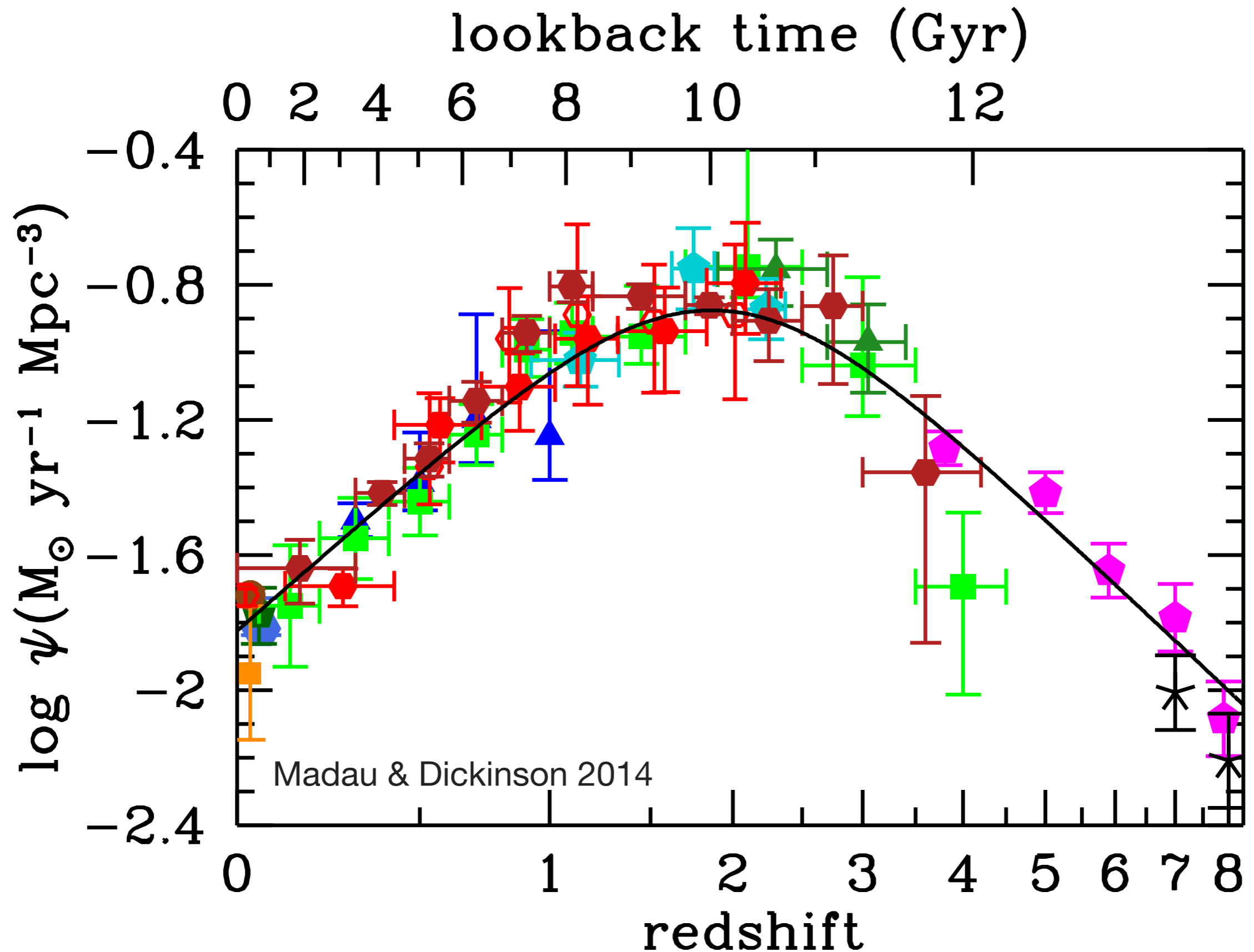


Stellar mass fraction

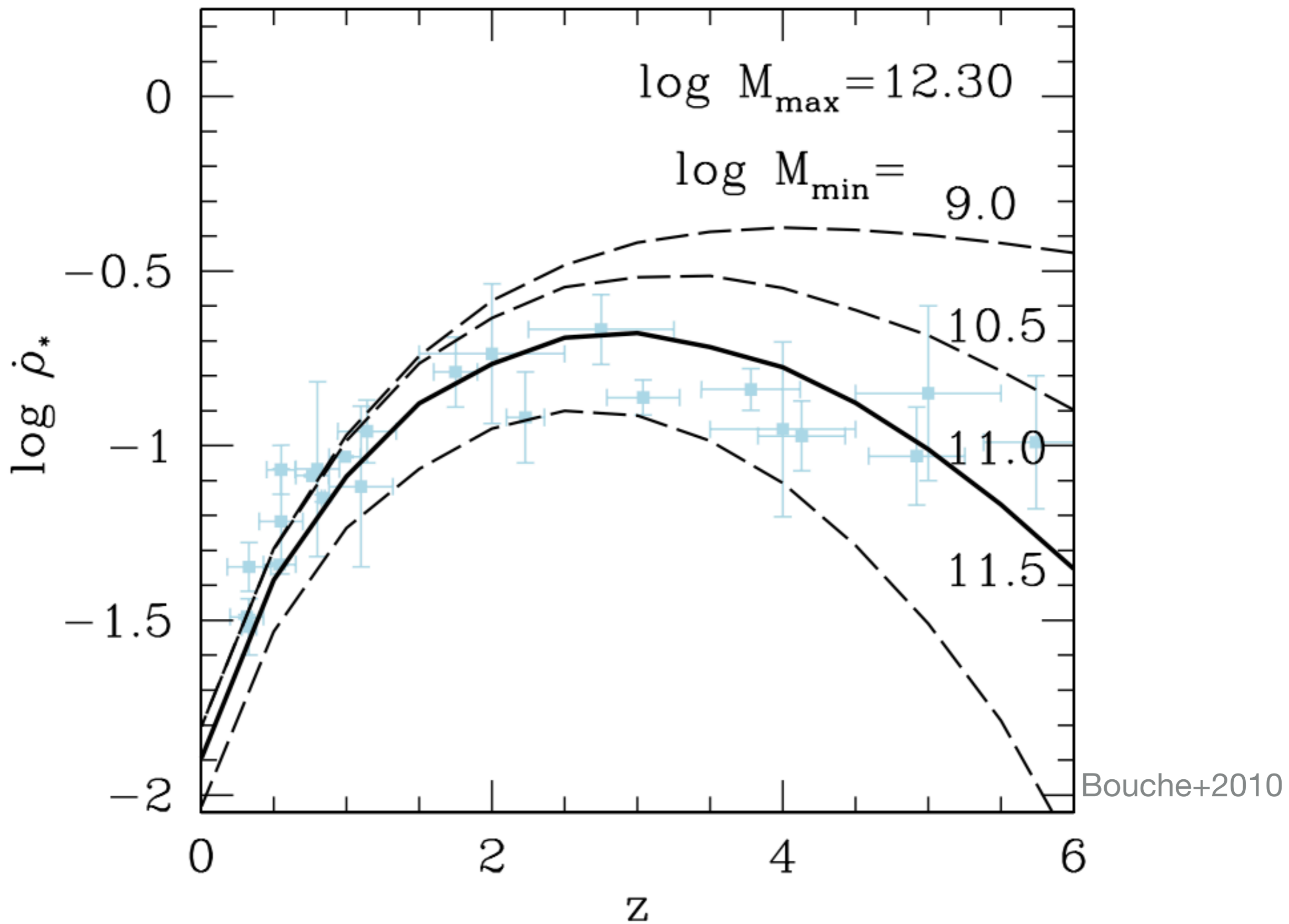


The $z = 0$ stellar fractions from Moster et al. (2010) and Guo et al. (2010) are shown as the shaded area and thick line, respectively.

Cosmic Star Formation History



Stellar mass fraction

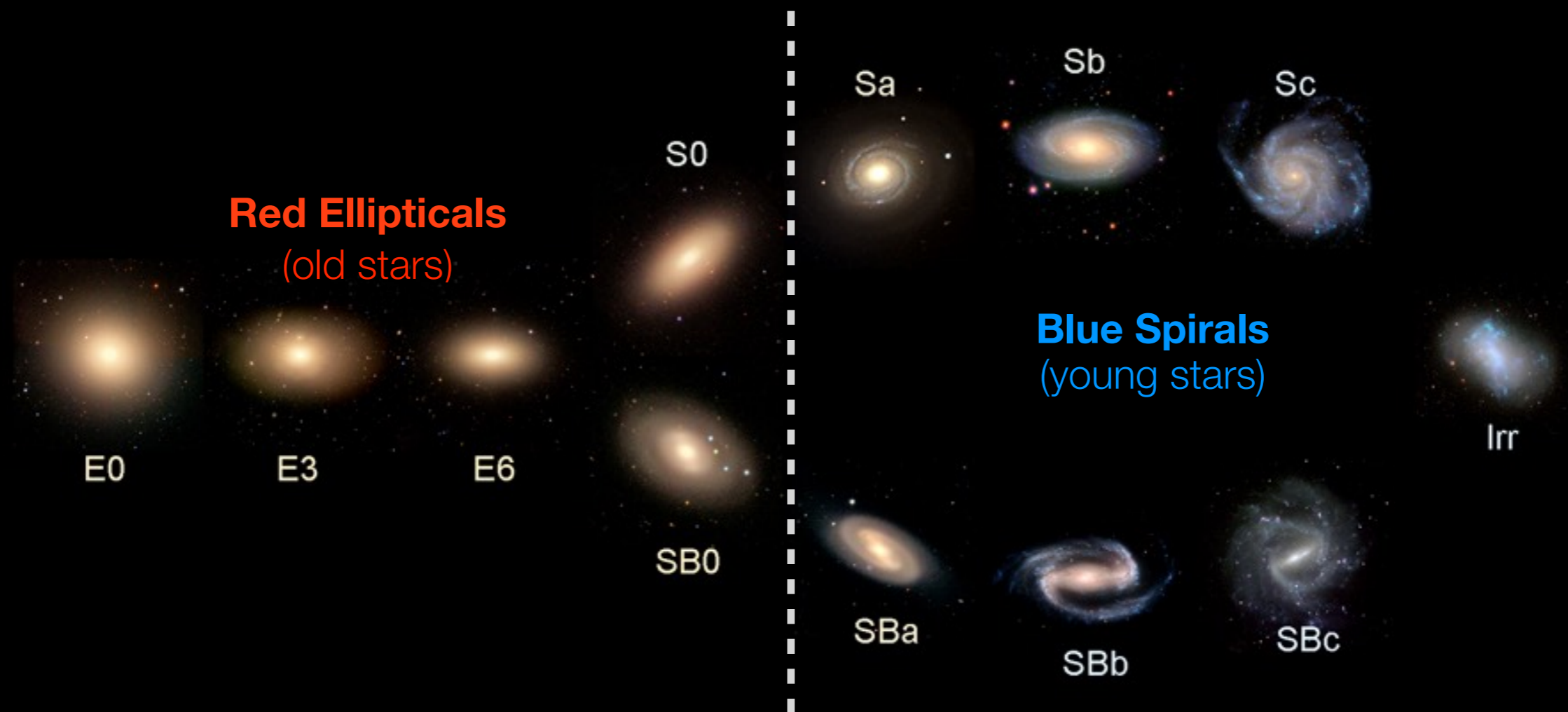


Unresolved Issue #1: Bimodal color distribution



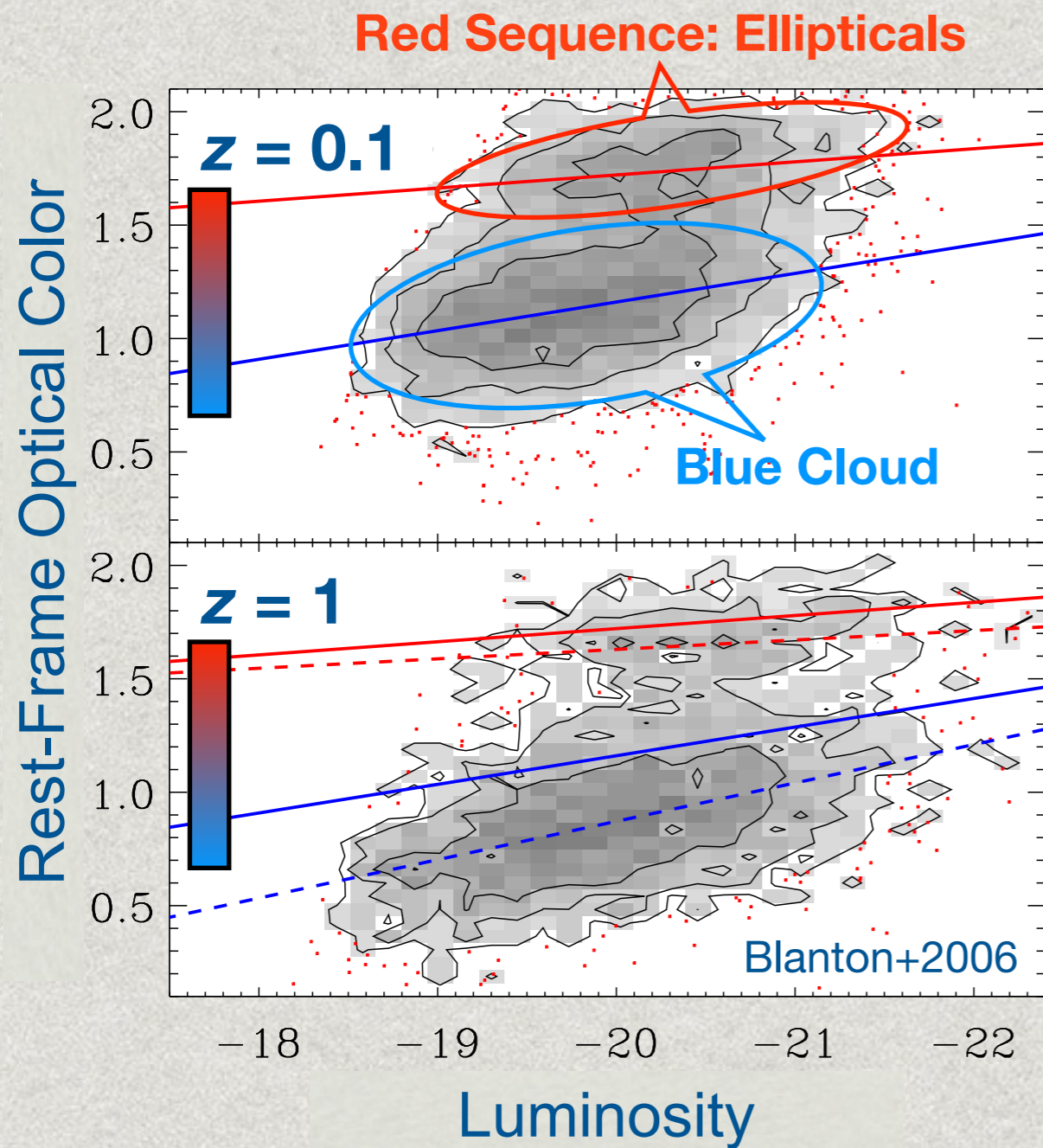
Color Bimodality: Galaxies are either **blue** or **red**

Hubble's Galaxy Classification Scheme

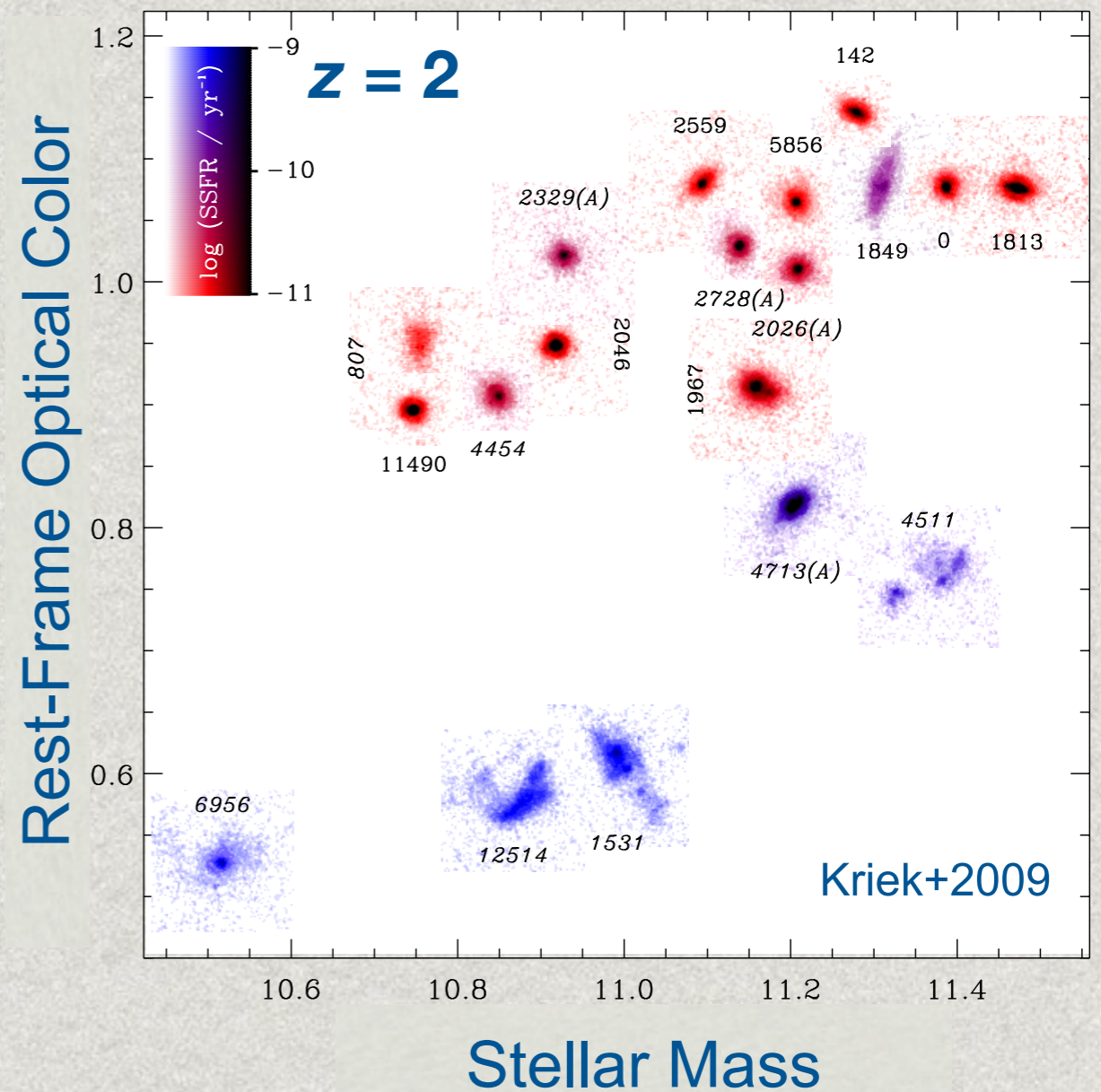


Galaxies in the Current universe

Color Bimodality



The Color Bimodality already existed **10 Gyr ago**

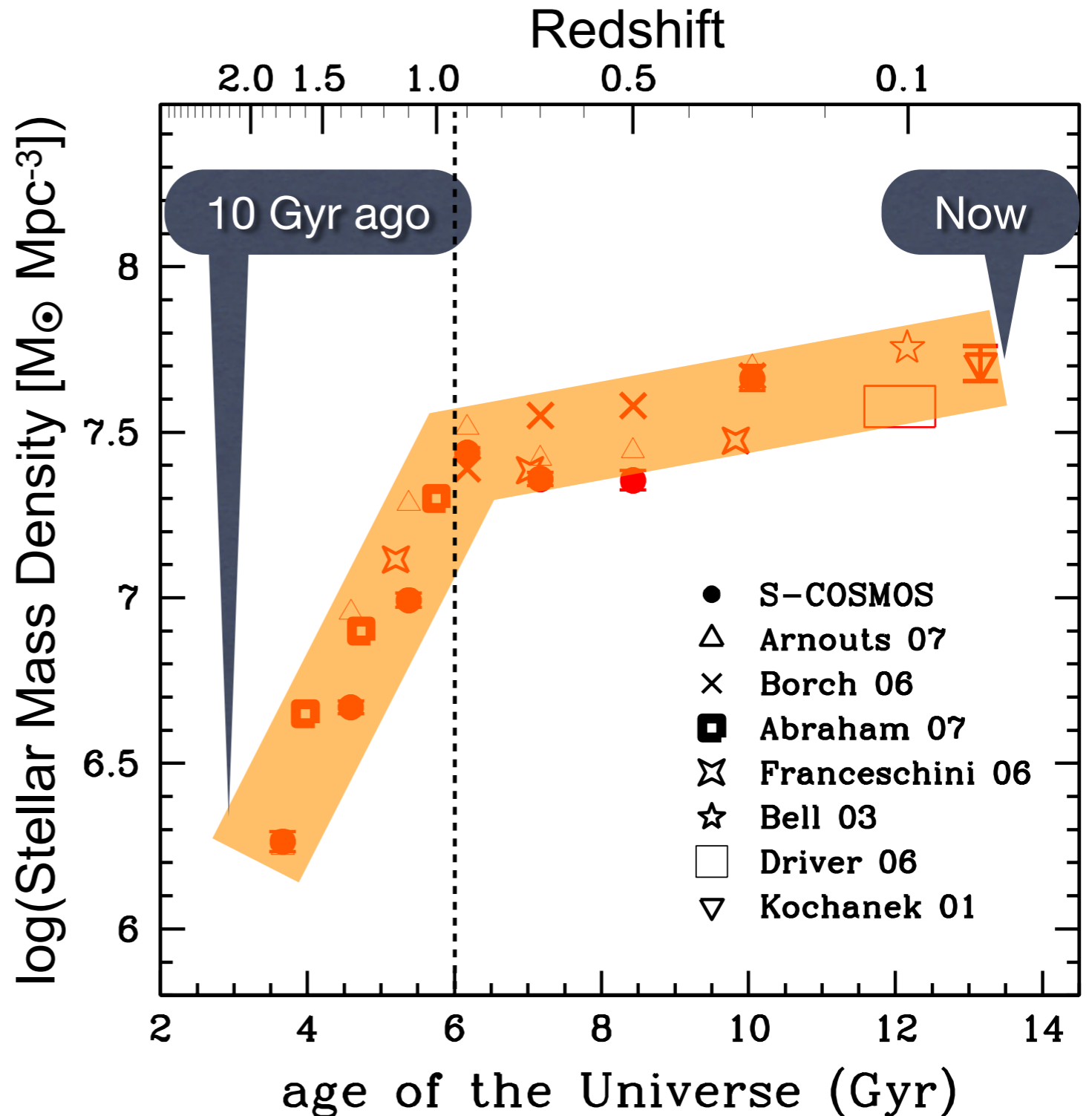


The early & rapid build-up of the red sequence

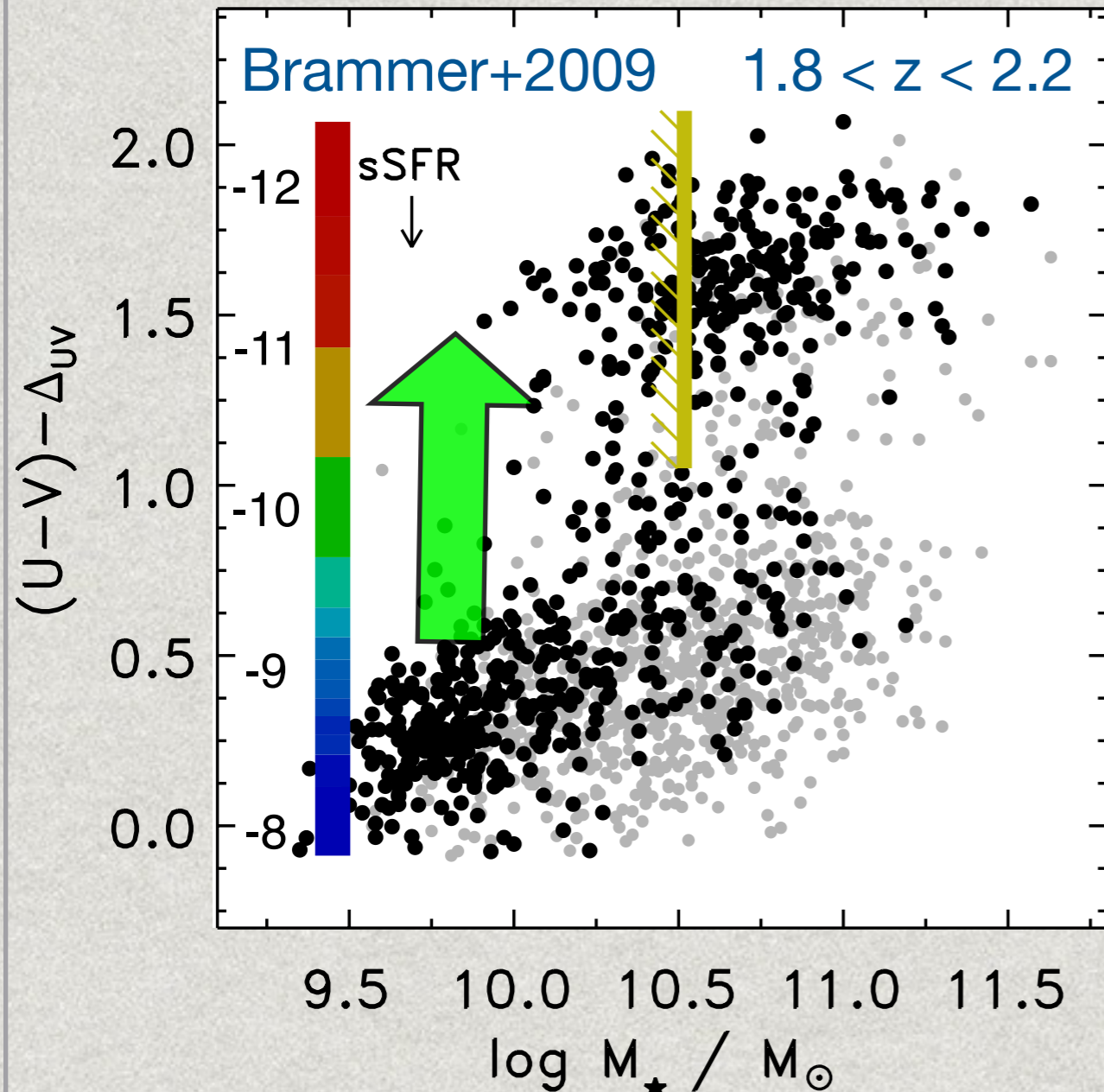
the evolution of the total comoving stellar mass density of quiescent galaxies

- **Early Completion:**
Most of the stellar mass in the red sequence is already in place by $z = 1$
- **Rapid Build-Up:**
Stellar mass density increased more than 20x in just 2.5 Gyr ($1 < z < 2$).

Ilbert+2010



Color bimodality at high-redshift requires rapid quenching



The lack of galaxies between **blue cloud** and **red sequence** requires very rapid transition:

* It takes ~ 5 e-folding time to cross the green valley ($e^5 = 150$)

* red-sequence e-folding timescale of 1 Gyr indicates an SFR e-folding time **<0.2 Gyr** (consistent w/ Goncalves+2012)

This is **10x** shorter than the gas exhaustion time (\sim **2 Gyr**)!

$$\tau = \frac{\tau_{\text{dyn}}}{\epsilon_{\text{SF}}(1 - f_{\text{recycle}} + f_{\text{outflow}})}$$

When cold gas accretion stops: drain the tub

SFR exponentially declines with an e-folding time of 2 Gyr

$$\left\{ \begin{array}{l} \frac{dM_{\text{gas}}}{dt} = \epsilon_{\text{cold}} f_{\text{baryon}} \frac{dM_{\text{halo}}}{dt} - (1 - f_{\text{recycle}} + f_{\text{outflow}}) \text{SFR} \\ \text{SFR} = \epsilon_{\text{SF}} \frac{M_{\text{gas}}}{\tau_{\text{dyn}}} \quad \leftarrow \text{KS Star Formation Law} \end{array} \right.$$

when $\epsilon_{\text{cold}} = 0$ we have :

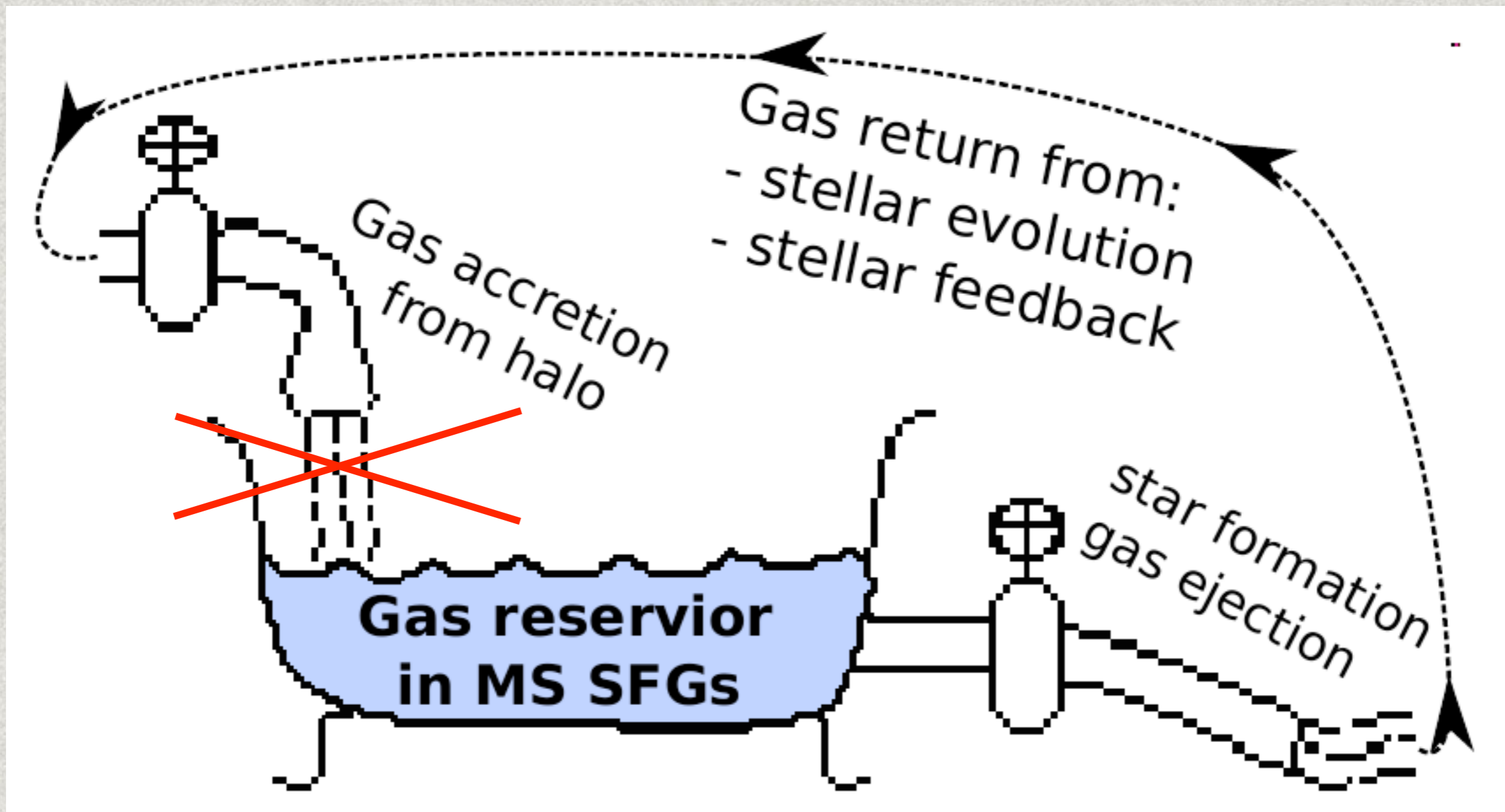
$$\frac{d\text{SFR}}{dt} = - \frac{\epsilon_{\text{SF}} (1 - f_{\text{recycle}} + f_{\text{outflow}})}{\tau_{\text{dyn}}} \text{SFR}$$

Solving this equation, we get an exponentially declining SFR :

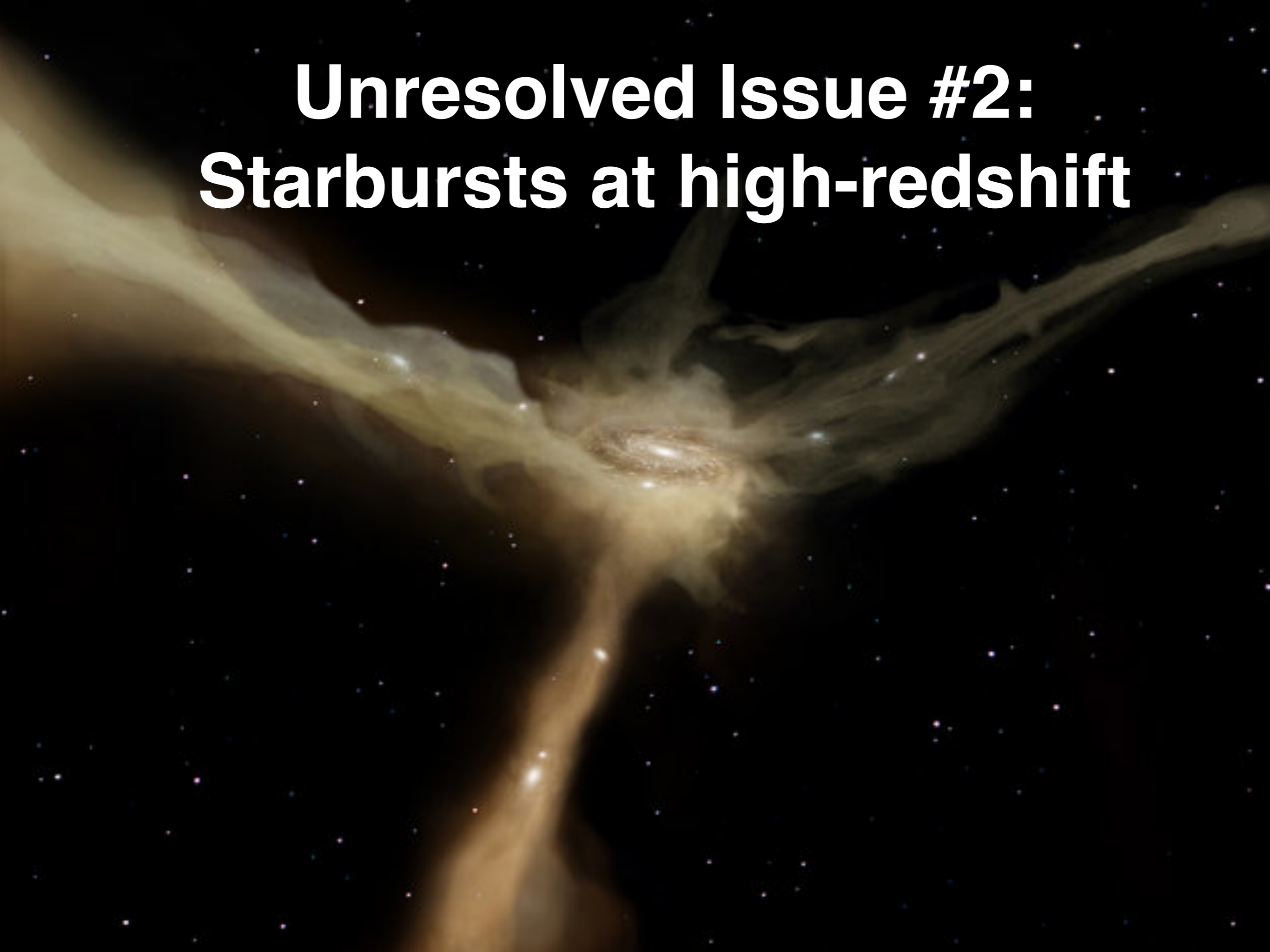
$$\text{SFR} \propto \exp\left(-\frac{t}{\tau}\right) \text{ and } \tau = \frac{\tau_{\text{dyn}}}{\epsilon_{\text{SF}} (1 - f_{\text{recycle}} + f_{\text{outflow}})} \simeq 2 \text{ Gyr}$$

How to quench star formation? (i.e. reduce the e-folding time by 10x)

$$\text{SFR} \propto \exp\left(-\frac{t}{\tau}\right) \text{ and } \tau = \frac{\tau_{\text{dyn}}}{\epsilon_{\text{SF}}(1 - f_{\text{recycle}} + f_{\text{outflow}})} \simeq 2 \text{ Gyr}$$

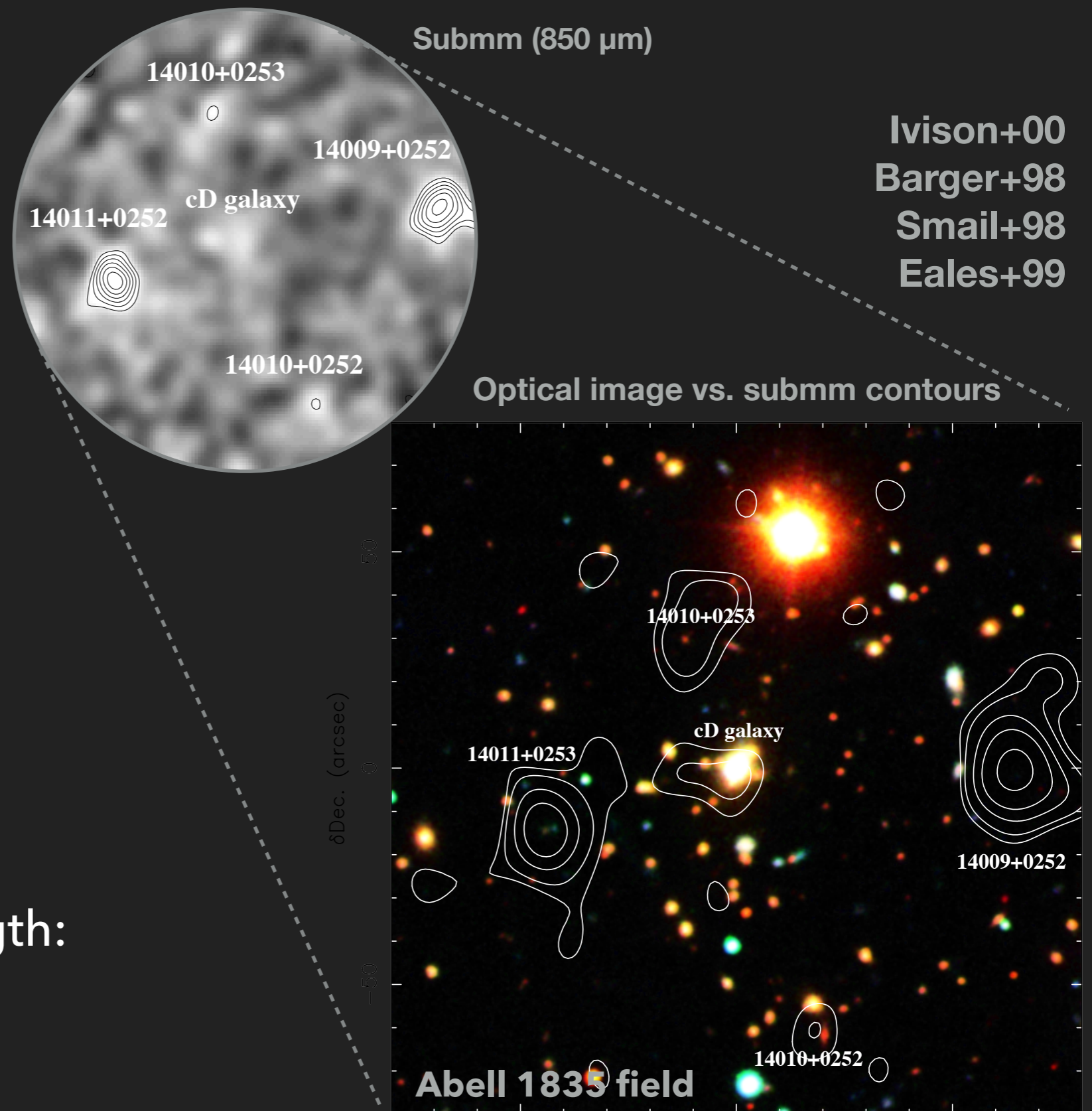


Unresolved Issue #2: Starbursts at high-redshift

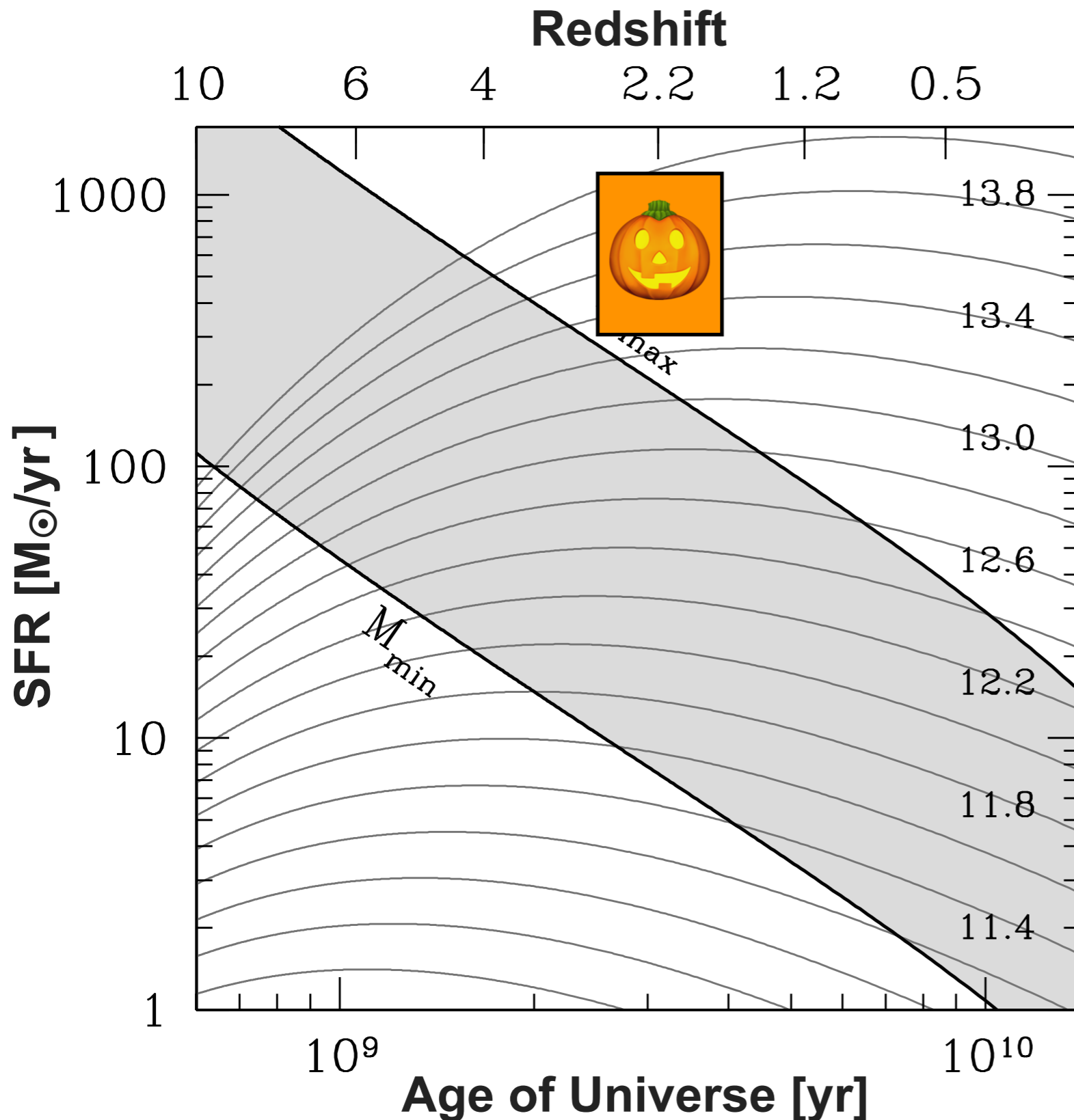


Submm-Bright Galaxies (SMGs) at $z \sim 2.5$

- ▶ SMG definition:
 $S(850\mu\text{m}) > 2\text{-}3 \text{ mJy}$
- ▶ Bright in submm,
but extremely faint
in optical
- ▶ Median properties:
 $\langle z \rangle \sim 2.5$
 $\langle L_{\text{IR}} \rangle \sim 5 \times 10^{12} L_{\odot}$
 $\langle \text{SFR} \rangle \sim 500 M_{\odot}/\text{yr}$
- ▶ Strong clustering strength:
 $M_{\text{halo}} \sim 10^{13} M_{\odot}$
similar to $z \sim 2$ QSOs



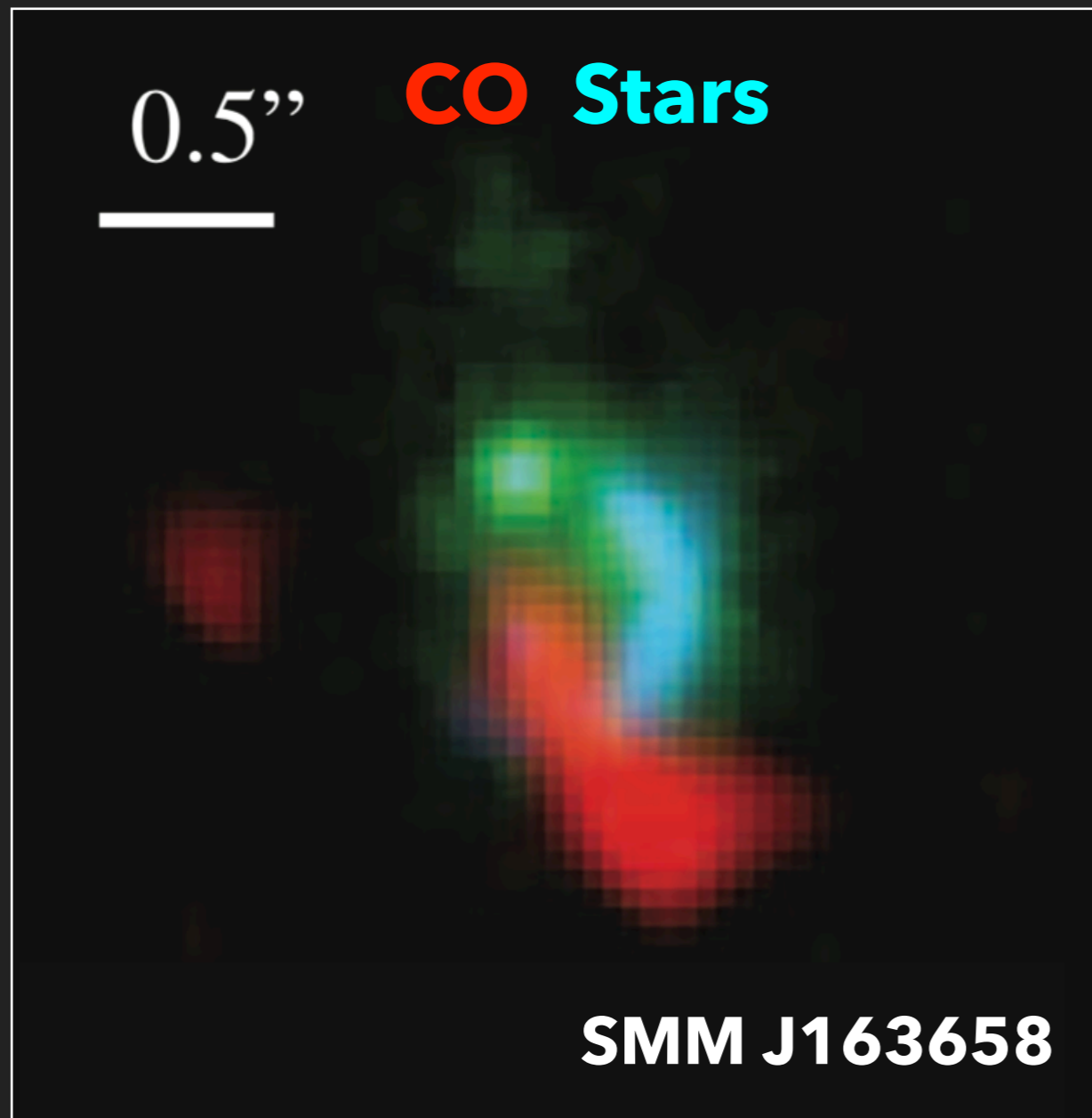
Intense Starburst Galaxies at $z \sim 2$



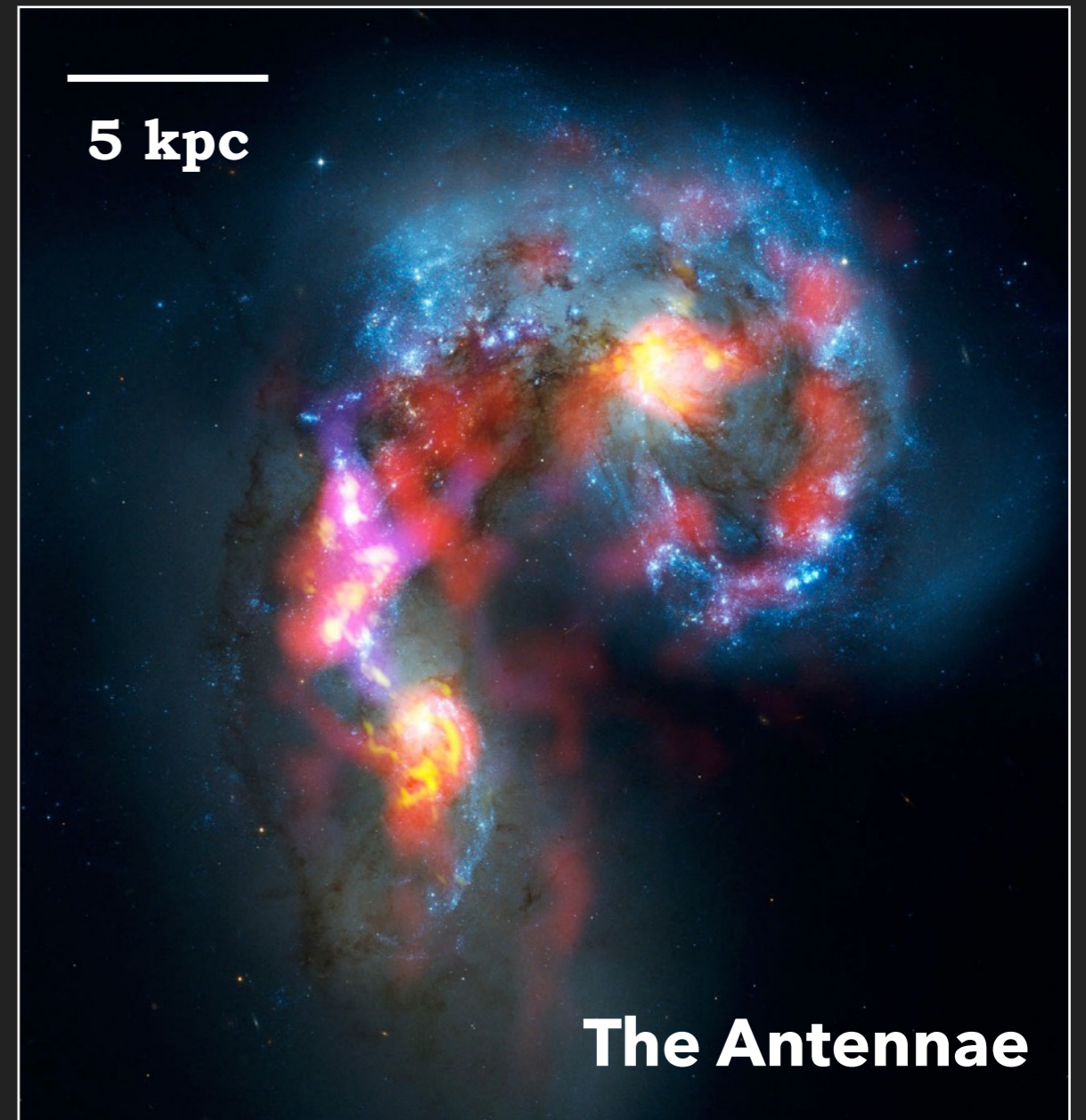
- ▶ **Green region:** star formation tracks of all halos less than $10^{14} M_{\odot}$ at $z = 0$.
- ▶ **Orange:** The SFRs of these galaxies appear too high for any halos at their epoch.

Misaligned stellar and ISM emission

typical offsets: a few kpc ($0.5'' = 4 \text{ kpc @ } z = 2.5$)



Tacconi+2008

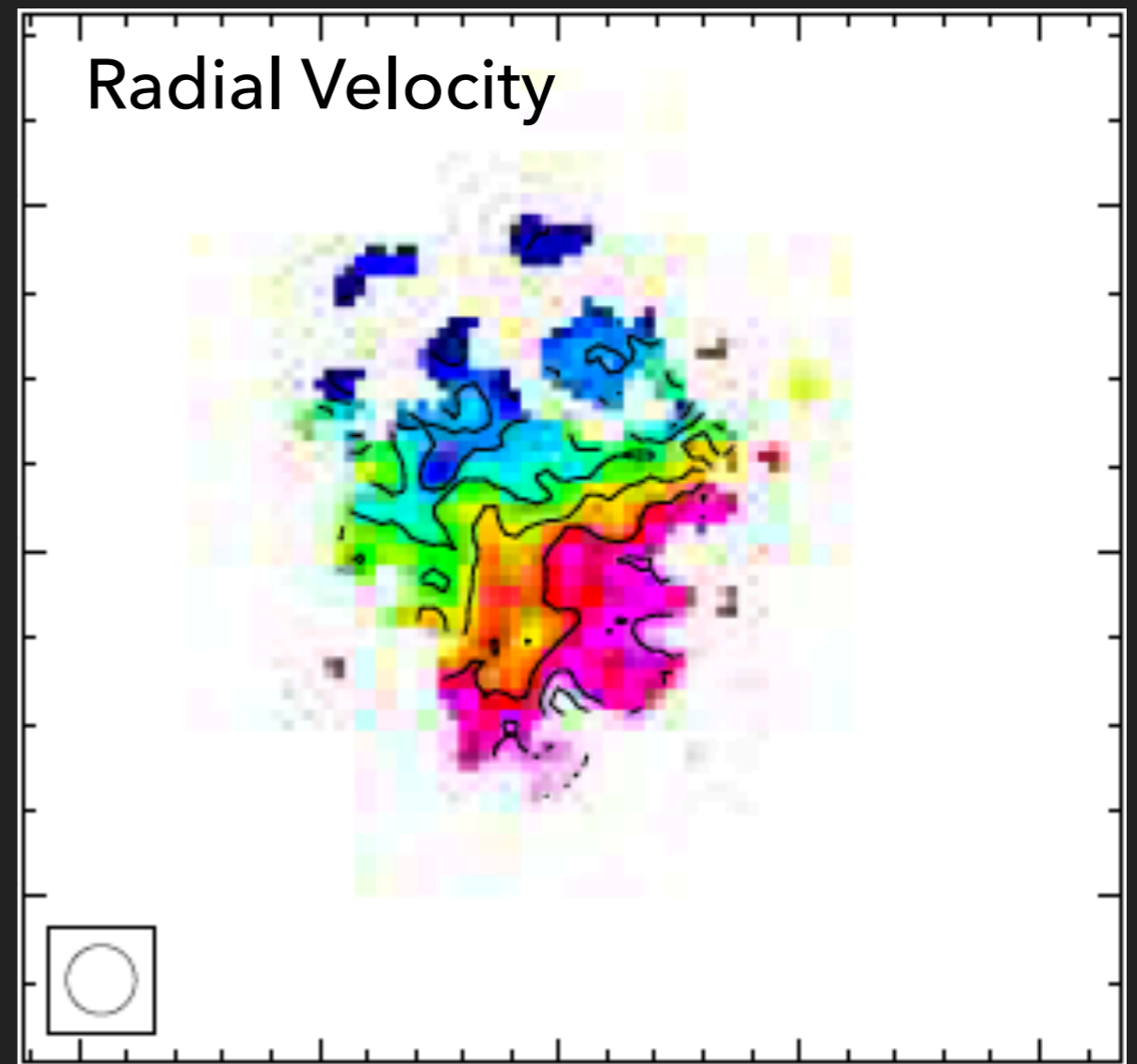
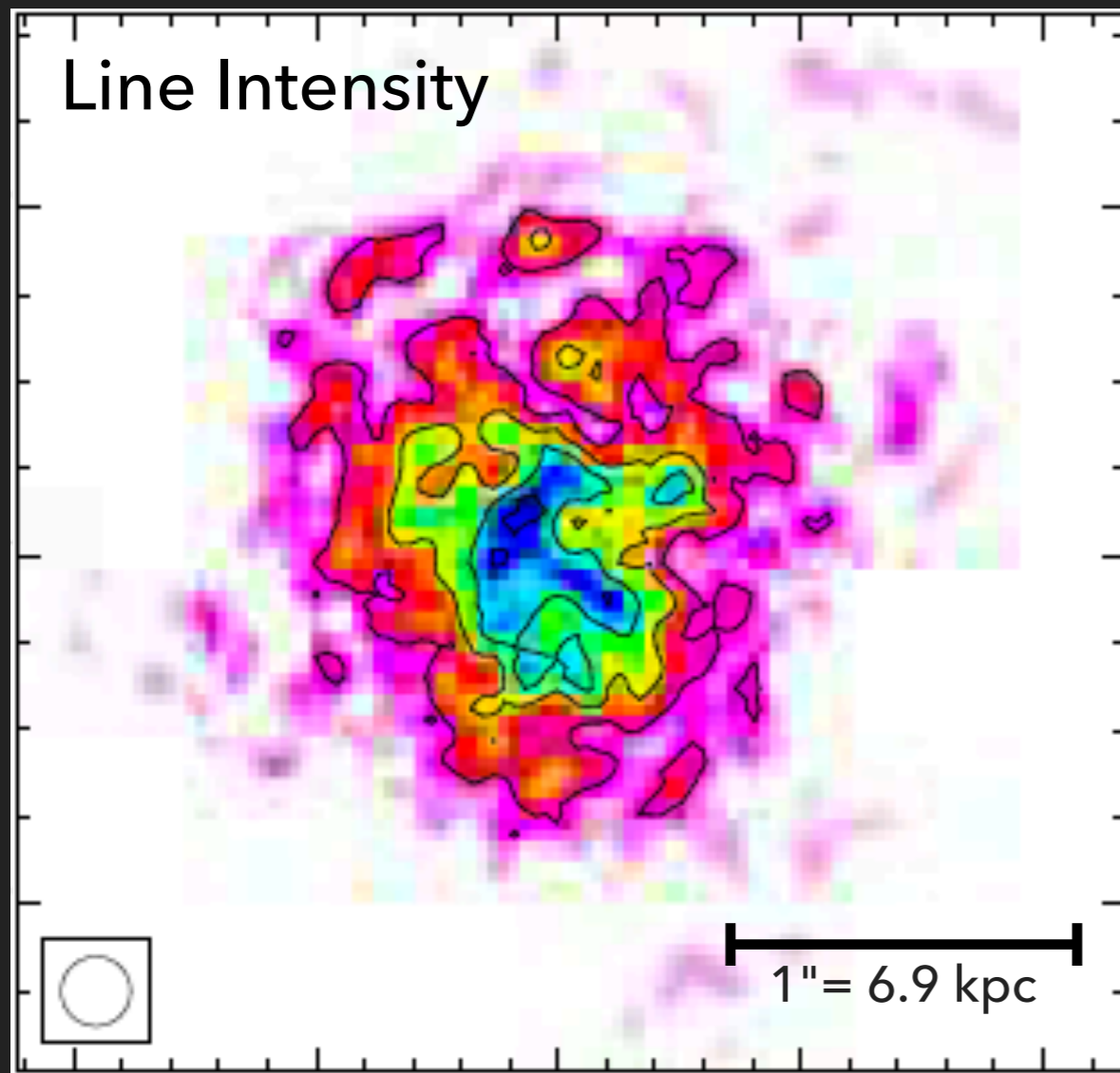


Calistro Rivera+2018

A clumpy, rotating gas disk in an SMG

GN20, CO J=2-1 @ $z = 4.05$, VLA observations

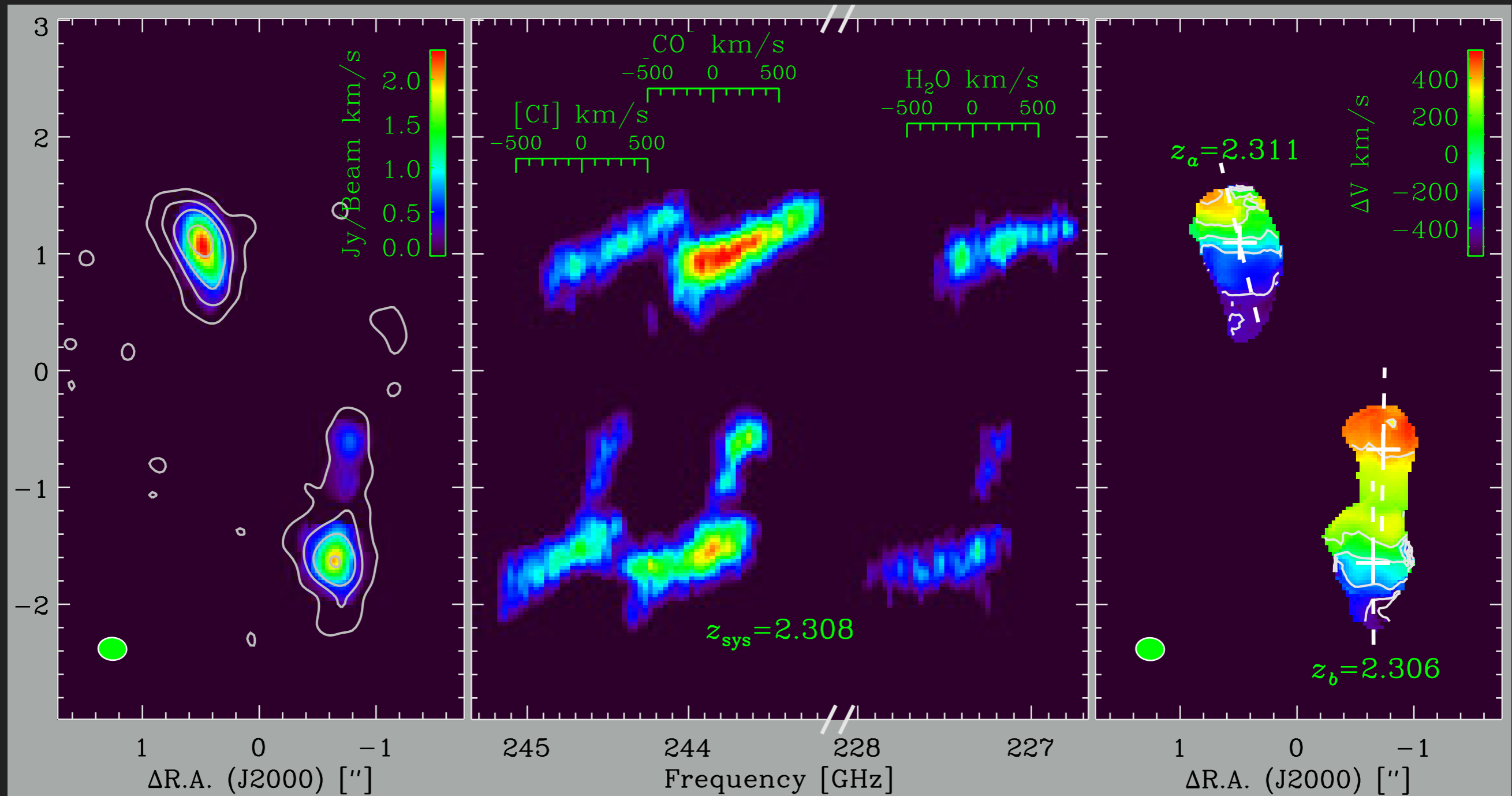
$M_{\text{dyn}} = 5 \times 10^{11} M_{\text{sun}}$, disk diameter ~ 14 kpc



Resolved gas kinematics in an SMG merger

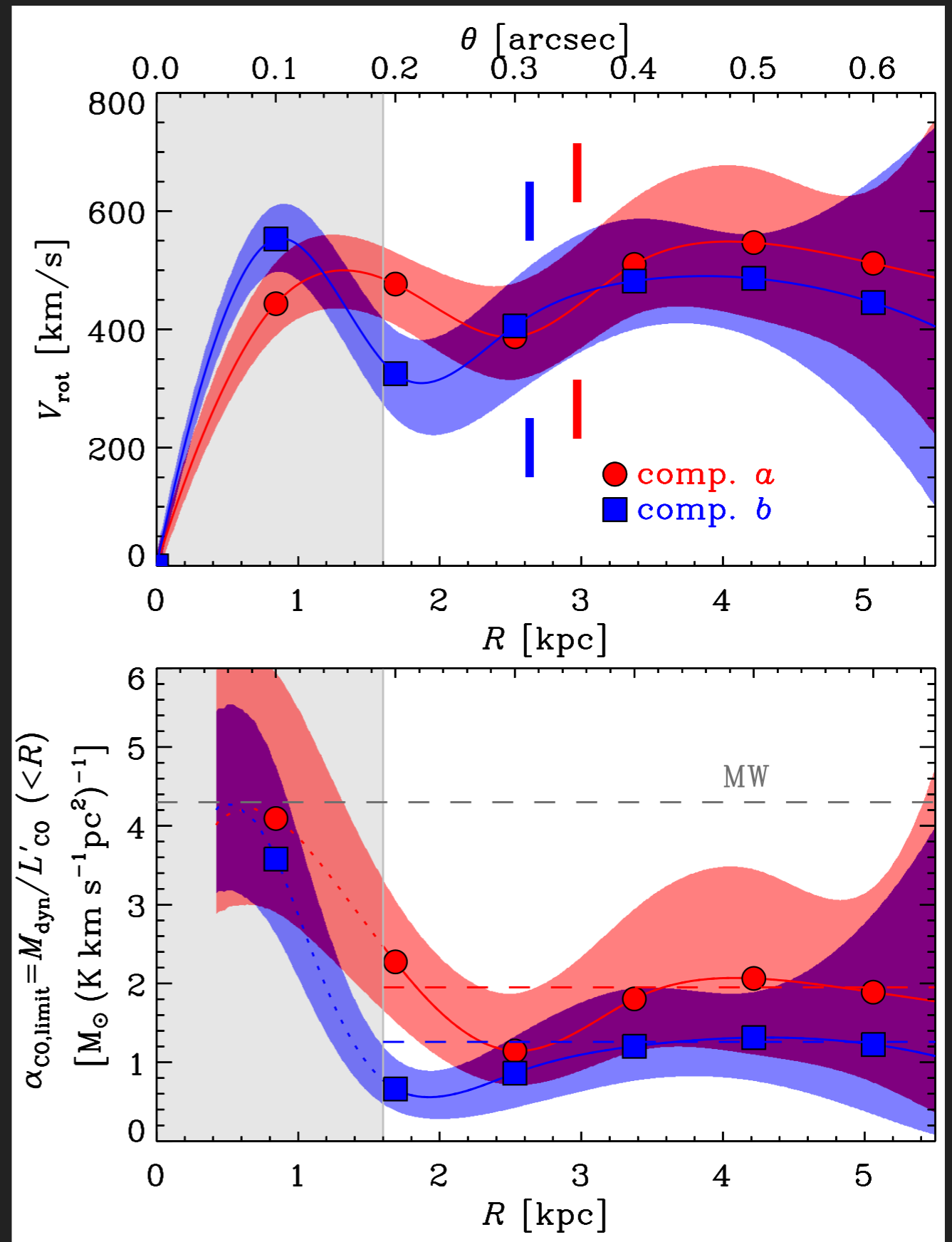
ALMA Cycle 3, 2.6 hr on-source, 0.2" spatial resolution, 240 GHz (band 6, $z = 2.308$)

CO J=7-6 @ 806.7 GHz, [C I] $^3P_2 - ^3P_1$ @ 809.3 GHz, H₂O 2₁₁ - 2₀₂ @ 752.0 GHz



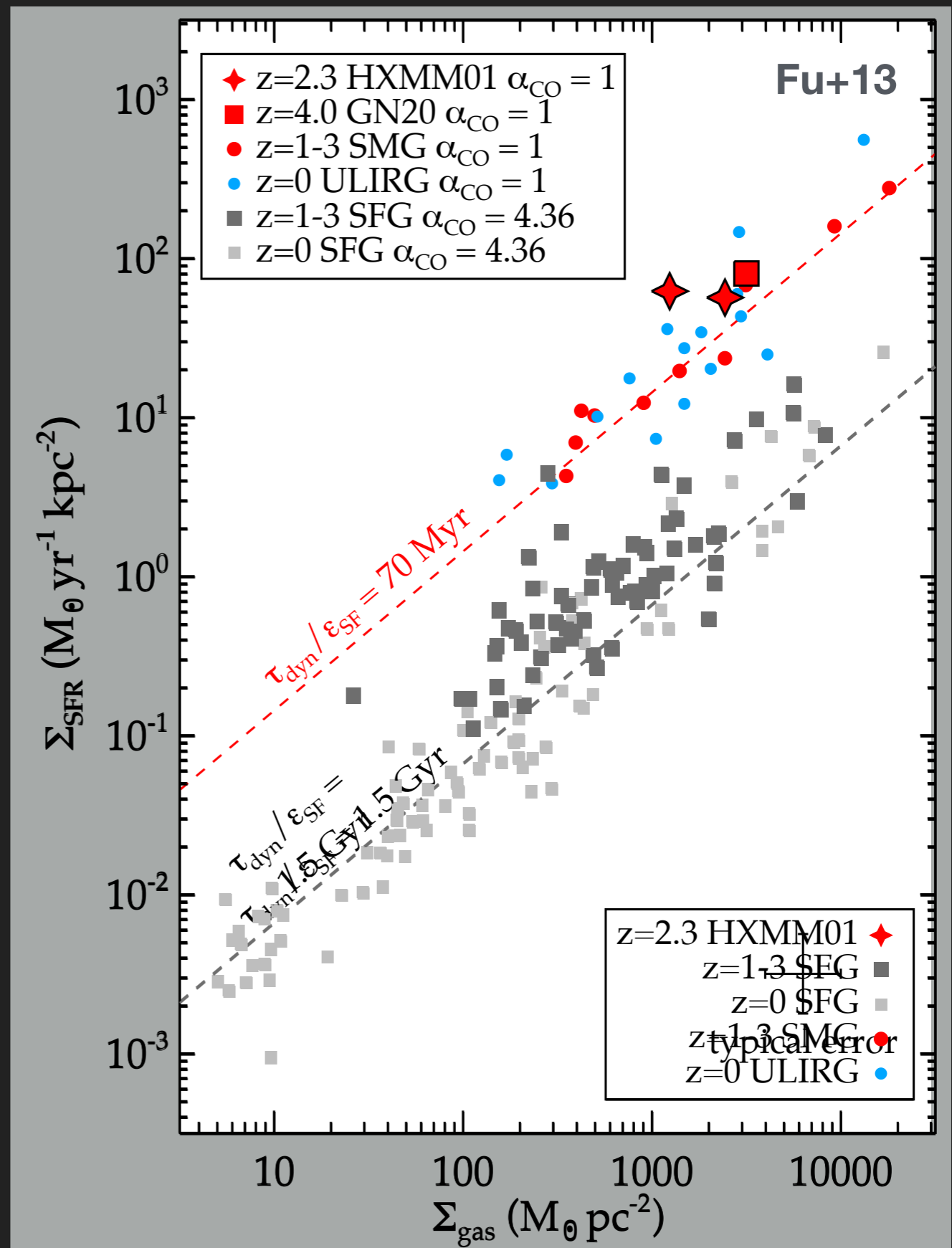
Dynamical mass estimates

- ▶ Rotation velocities reach 500 km/s (inclination corrected), with a dispersion ~ 160 km/s
- ▶ Dynamical masses:
 $M_{\text{dyn}} \sim 2 \times 10^{11} M_{\text{sun}}$ within 5 kpc
- ▶ CO(1-0) luminosity:
 $L'_{\text{co}} \sim 1.5 \times 10^{11} \text{ K km/s pc}^2$
- ▶ Upper limits on the CO-to-H₂ conversion factor:
 $M_{\text{H}_2}/L'_{\text{co}} < 1.5$, much lower than the Galactic GMC value of 4.3.

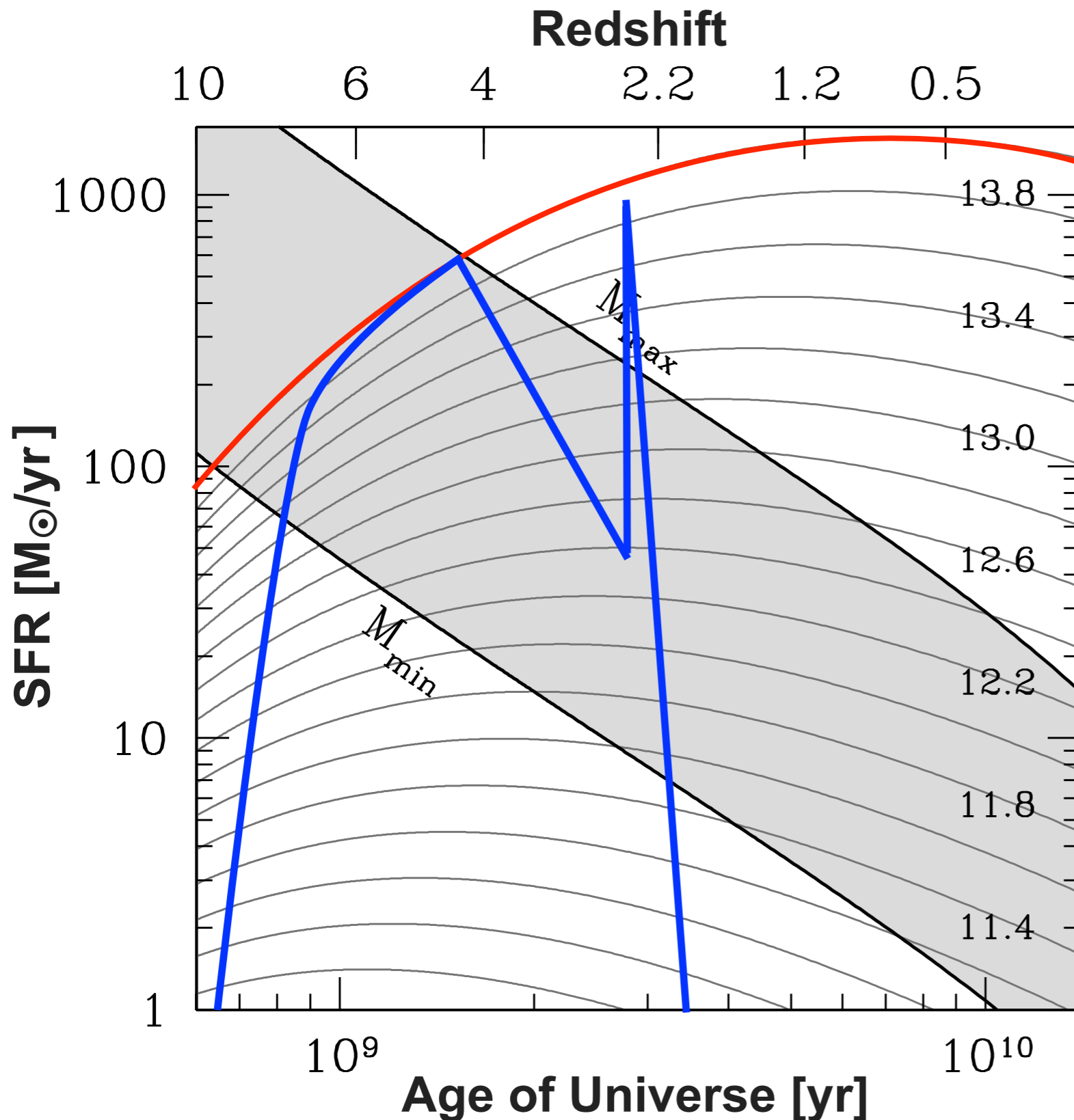


The Unsustainable Growth of SMGs

- ▶ $M_{\text{gas}}/\text{SFR} \sim 100 \text{ Myr}$
- ▶ 10x greater SFR for any given gas mass
- ▶ 10x shorter gas depletion timescale than normal star-forming galaxies
- ▶ Without continuous gas supply, SFR will decline with an e-folding timescale of $\sim 200 \text{ Myr}$



So, what's up with the SMGs?



✓: Burst: Star formation efficiency increases 10x in $10^{13} M_{\odot}$ halos.

Implications:

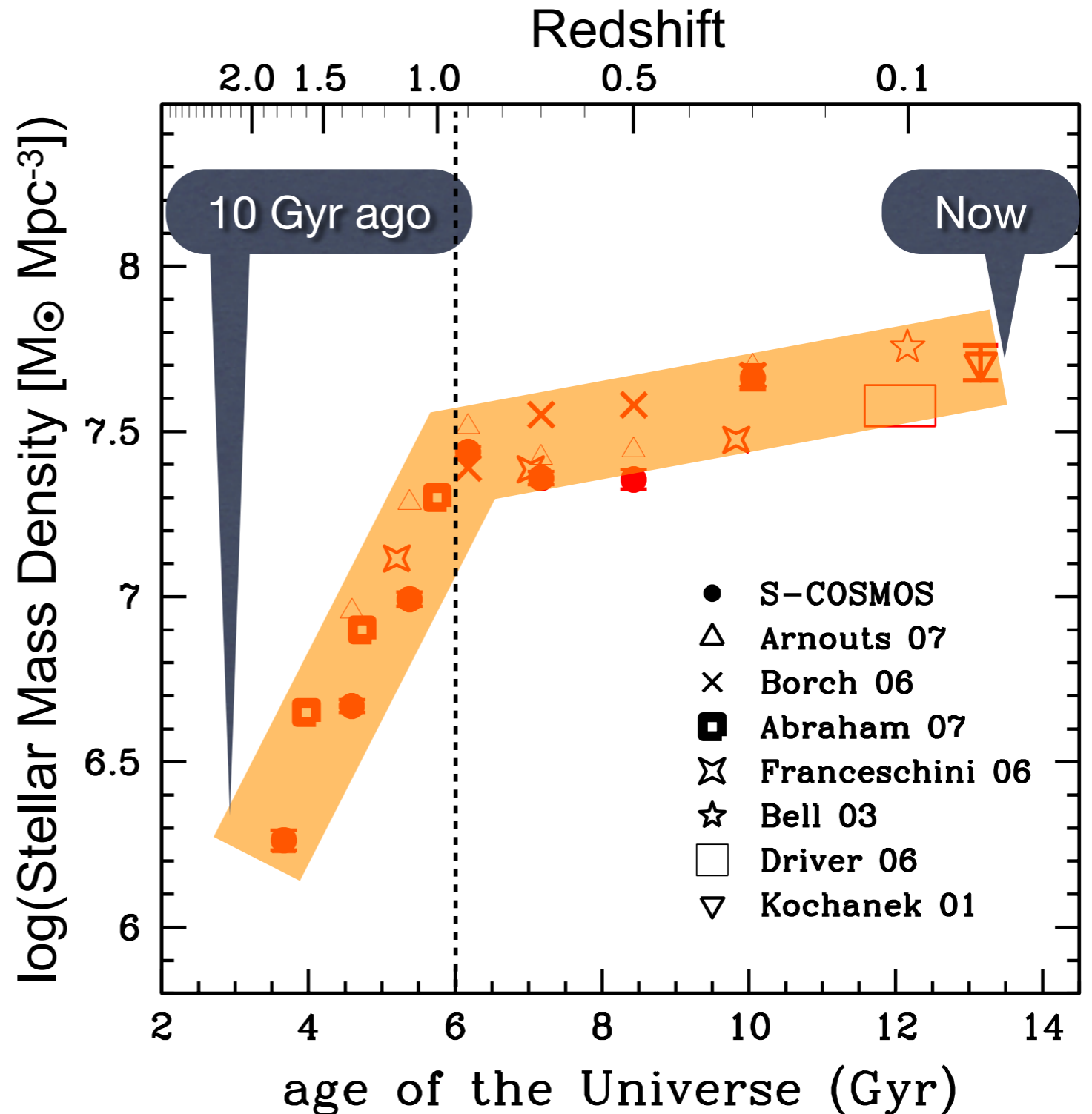
- two distinct populations of SMGs: $z > 4$ and $z \sim 2$
- high stellar masses ($\sim 2 \times 10^{11} M_{\text{sun}}$)
- relatively low gas fraction
- helps explain the early, rapid formation of massive quiescent galaxies

The early & rapid build-up of the red sequence

the evolution of the total comoving stellar mass density of quiescent galaxies

- **Early Completion:**
Most of the stellar mass in the red sequence is already in place by $z = 1$
- **Rapid Build-Up:**
Stellar mass density increased more than 20x in just 2.5 Gyr ($1 < z < 2$).
- *Not observed in star-forming galaxies*

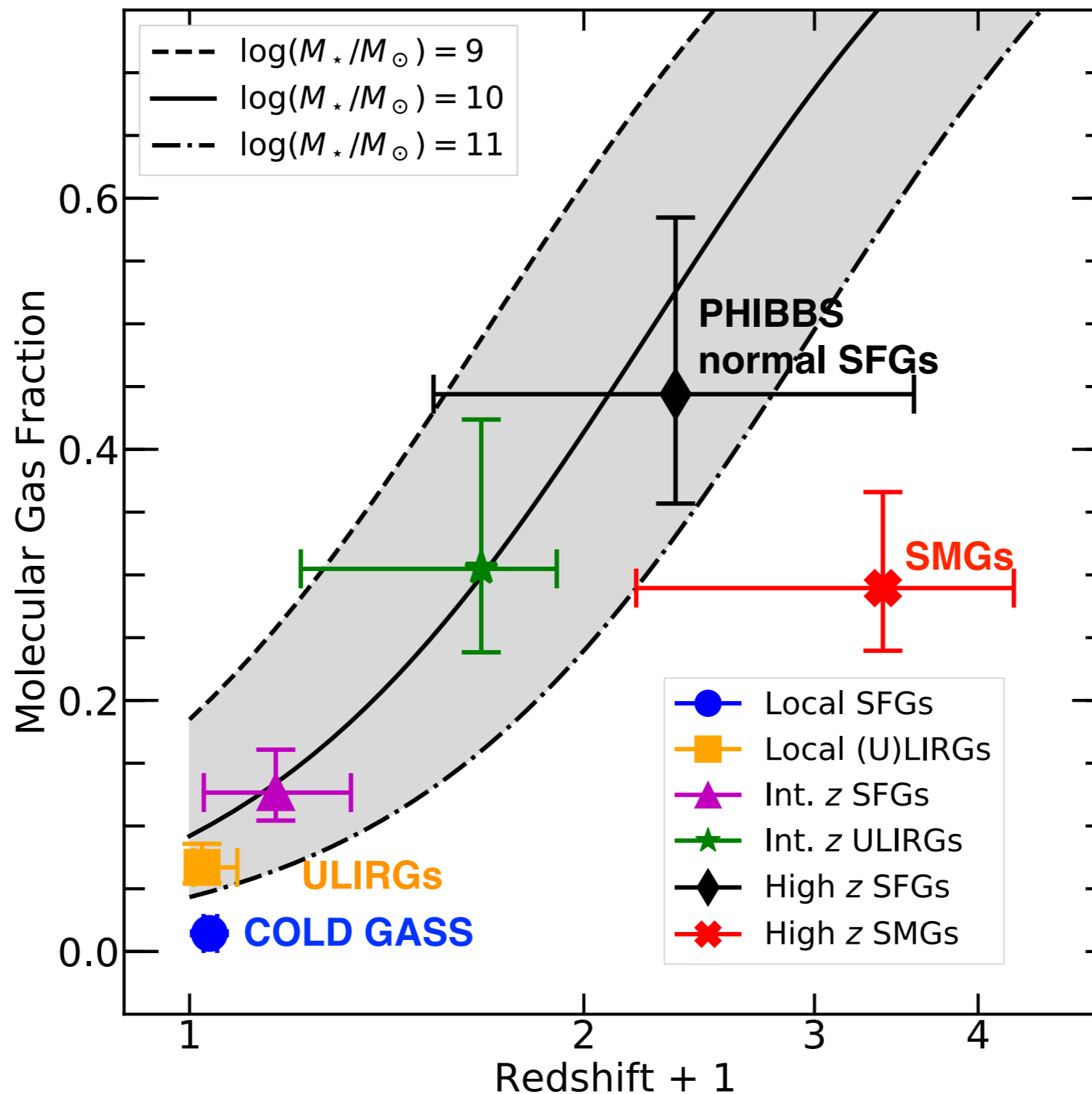
Ilbert+2010



SMGs have lower gas fraction than normal SFGs?

Data Points: gas fractions measured w/ Tully-Fisher relation & $\alpha_{\text{CO}} = 1$

Curves: gas fractions inferred from sSFR(z) of different stellar masses



one stone two birds

- SMGs have $\sim 10x$ higher SF efficiency than normal galaxies, i.e., they are massive starbursts
- Starbursts can stop star formation by rapidly exhausting the gas reservoir, providing a quenching mechanism to turn **blue starforming galaxies** into **red passive galaxies**.
- Starbursts are a universal phase in the formation of massive red galaxies. All galaxy formation models should be able to reproduce this important phase.
- ▶ *What triggers the high star formation efficiency? Why every massive galaxy goes through a burst phase?*